## Math 2311

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Class webpage: http://www.math.uh.edu/~bekki/Math2311.html

What is the difference between a discrete random variable and a continuous random variable?

How do we know when we are working with $\bar{X}$ vs. $X$ ?

What is $\hat{p}$ ? The statistic $\hat{p}$ is an estimate of the parameter $p . \hat{p}=\mathrm{X} / \mathrm{n}$ Since values of X and $\hat{p}$ vary in repeated samples, they are both random variables. $X$ will follow a binomial distribution (provided that the population is more than 10 times the sample) BUT $\hat{p}$ does not. The sampling distribution of $\hat{p}$ will follow the normal distribution with mean $p$ and standard deviation $\sqrt{\frac{p(1-p)}{n}}$ (provided our conditions are met - see last week's notes)

Some more practice:

1. Suppose that you are interested in the proportion of all registered voters who intend to vote in the next election; call this (parameter) proportion $p$. In practice, you would never know $p$, but you could estimate it based on a sample proportion. Assume for now, though, that you know $p=.6$, and suppose that you plan to interview a simple random sample of $\mathrm{n}=750$ registered voters and to ask each whether she or he intends to vote.
a.) What does the Central Limit Theorem say about the sampling distribution of this sample proportion?
b.) Use this result and the table of standard normal probabilities to find the probability that the sample proportion intending to vote would fall within .029 of $p$.
c.) Calculate the probability that the sample proportion intending to vote would fall within .035 of $p$.
d.) Calculate the probability that the sample proportion intending to vote would fall within .046 of $p$.
e.) Find the value k such that the probability of the sample proportion falling between . $6-\mathrm{k}$ and $.6+\mathrm{k}$ would equal .8
2. $43 \%$ of the voters in the 1992 Presidential election voted for Bill Clinton. Suppose that you take a simple random sample of 500 voters from this population.
a.) Is $43 \%$ a parameter or a statistic?
b.) Determine the probability that the sample proportion of Clinton voters turns out to be less than $40 \%$.
c.) Determine the probability that the sample proportion of Clinton voters exceeds $50 \%$.
d.) Determine the probability that the sample proportion of Clinton voters falls between $40 \%$ and $46 \%$.
e.) Determine the probability that the sample proportion of Clinton voters falls between $37 \%$ and $49 \%$.
f.) Determine the probability that the sample proportion of Clinton voters falls between $43 \%$ and $89 \%$.
g.) Without doing the actual calculations, indicate how your answers to $\mathrm{b}-\mathrm{f}$ would change (get smaller, get larger, or stay the same) if the sample size were 1500 instead of 500 .

## Popper 09

1. Find $c$ such that $P(Z>c)=0.8790$
2. Find $c$ such that $P(-c<Z<c)=0.8790$

## Section 5.1 - Bivariate data

Bivariate data is data for two different variables (usually related in some way).
Variables are classified as response variables and explanatory variables. A response variable (dependent) measures the outcome of a study. An explanatory variable (independent) attempts to explain the observed outcomes. Algebraically speaking, your explanatory variable is your " $x$ " and the response variable is your " $y$ ".

Once the explanatory and response variables are identified, we can display the associatior between the two using a scatterplot.

Example: Televisions and Life Expectancy

| Country | Life Exp. | Per TV |
| :--- | :--- | :--- |
| Angola | 44 | 200 |
| Australia | 76.5 | 2 |
| Cambodia | 49.5 | 177 |
| Canada | 76.5 | 1.7 |
| China | 70 | 8 |
| Egypt | 60.5 | 15 |
| France | 78 | 2.6 |
| Haiti | 53.5 | 234 |
| Iraq | 67 | 18 |
| Japan | 79 | 1.8 |
| Madagascar | 52.5 | 92 |
| Mexico | 72 | 6.6 |
| Morocco | 64.5 | 21 |
| Pakistan | 56.5 | 73 |
| Russia | 69 | 3.2 |
| S. Africa | 64 | 11 |
| Sri Lanka | 71.5 | 28 |
| Uganda | 51 | 191 |
| U.K. | 76 | 3 |
| U.S. | 75.5 | 1.3 |
| Vietnam | 65 | 29 |
| Yemen | 50 | 38 |

a) Which of the countries listed has the fewest people per television set? Which has the most? What are those numbers?
b) Use the calculator to produce a scatter plot. Does there appear to be an association'

This example illustrates a very important distinction between association and causation. Two variables may be strongly associated without a cause-and-effect relationship existing between them. Often the explanation is that both variables are related to a third variable not being measured; this variable is often called a lurking or confounding variable.
c) In this case, suggest a confounding variable that is associated with both a country's life expectancy and the prevalence of televisions in the country.

Summary for creating a scatter plot:
R-Studio:

1. Choose variable names.
2. Enter the lists in R: $>x$ ListName=c(...) $>$ yListName=c(...)
3. Now use the plot command: > plot(xListName, yListName)

TI-83/84:

1. Go to STAT - EDIT

2. Enter the explanatory variable under L1 and the response under L2

3. Choose 2ND - QUIT to go back to home screen.
4. Go to 2ND - Y= and select Plot1

5. Choose ON, select the first type and make sure your Xlist is L1 and the Ylist is L2

6. Choose GRAPH then ZOOM and ZoomStat


To interpret a scatter plot we will look at the direction, form and strength.
Positively related:

Negatively related:

Linear relationship:

Popper 09
3. A positive slope indicates that large values of $x$ are associated with $\qquad$ values of $y$.
4. In regression analysis, the independent variable is also called the $\qquad$ variable.

