

True/False

F 1. For a p-series to converge, p must be less than or equal to 1.

F 2. In the application of the Integral test, the sum is equal to the value of the integral.

T 3. If $\sum_{n=1}^{\infty} (-1)^n a_n$ converges, then $\sum_{n=1}^{\infty} (-1)^{n+1} a_n$ converges.

T 4. If $\lim_{n \rightarrow \infty} a_n \neq 0$, then $\sum_{n=1}^{\infty} a_n$ diverges.

F 5. If $0 \leq a_n \leq b_n$ and $\sum_{n=1}^{\infty} a_n$ converges, then $\sum_{n=1}^{\infty} b_n$ diverges.

Determine the convergence or divergence for each sequence with the given general term. Choose the test used from:

- (A) Nth term test (B) Integral test (C) Geometric Series (D) P-Series
 (E) Telescoping (F) Direct Comparison (G) Limit Comparison (H) Alternating Series test

Series	Test used	Converge or Diverge?	Work:
6. $\sum_{n=4}^{\infty} \frac{1}{3n^2 - 2n - 15}$	G	Converges	Compare to $1/n^2$
7. $\sum_{n=1}^{\infty} \frac{n}{(n^2 + 1)^2}$	B	Converges	
8. $\sum_{n=1}^{\infty} \frac{n}{2n + 3}$	A	Diverges	
9. $\sum_{n=1}^{\infty} \frac{1}{n^3 + 1}$	F	Converges	
10. $\sum_{n=1}^{\infty} \frac{1}{2 + 3^n}$	F	Converges	
11. $\sum_{n=1}^{\infty} \frac{\sqrt{n}}{n}$	D	Diverges	p-series $p < 1$

12.	$\sum_{n=1}^{\infty} \frac{3}{n(n+3)}$	E	Converges	
13.	$\sum_{n=0}^{\infty} 3\left(-\frac{1}{2}\right)^n$	C	Converges	
14.	$\sum_{n=1}^{\infty} \tan\left(\frac{1}{n}\right)$	G	Diverges	Compared with 1/n
15.	$\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n+1}$	H	Converges	

Find the sum of the following convergent series:

16. $\sum_{n=0}^{\infty} \left(\frac{2}{9}\right)^n$ **9/7**

17. $\sum_{n=1}^{\infty} \frac{3}{n(n+3)}$ **1 5/6 (11/6)**

Can you apply the Integral test to the following? (yes or no)

yes 18. $\sum_{n=1}^{\infty} \frac{n}{n^2 + 1}$

no 19. $\sum_{n=1}^{\infty} \frac{\cos \pi n}{n}$

Determine if the following series (A) converge absolutely, (B) converge conditionally or (C) diverge.

B 20. $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} n}{\sqrt{n}}$

A 21. $\sum_{n=1}^{\infty} \frac{\cos \pi n}{n^2}$

— **C** — 22. $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} n!}{2^n}$

— **A** — 23. $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{(n+1)^2}$

Approximate the sum of the series with an error less than 0.001.

— **.316667** — 24. $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{2n!}$

— **1.0368** — 25. $\sum_{n=1}^{\infty} \frac{1}{n^5}$ (HINT: Use the Integral)