## Math 1311 Homework 11 (Section 6.1- Section 6.5)

Record your answers to all the problems in the EMCF titled "Homework 11".

- 1. A car is driving at a constant velocity of 74 miles per hour. A perspective has been chosen so that directed distance is increasing. Since the velocity is constant, we know that directed distance is a linear function. What is the slope of that linear function?
  - a. 74 miles per hour
  - b. 37 miles per hour
  - c. -74 miles per hour
  - d. -37 miles per hour
- 2. The price P of gasoline increases to a maximum and then stays at a fixed price. What is the rate of change  $\frac{dP}{dt}$  and how is it changing at the time when the price reaches a maximum?
  - a.  $\frac{dP}{dt}$  is negative at the maximum and is decreasing.
  - b.  $\frac{dP}{dt}$  is equal to zero at the maximum and remains the same.
  - c.  $\frac{dP}{dt}$  is positive at the maximum and is decreasing.
  - d.  $\frac{dP}{dt}$  is negative at the maximum and is increasing.
- 3. What is rate of change in directed distance?
  - a. Speedb. Accelerationc. Velocity
  - d. Displacement
- 4. When the graph of directed distance is decreasing, is the graph of velocity above or below the horizontal axis?
  - a. Below the Horizontal Axis
  - b. Above the Horizontal Axis
  - c. At the Horizontal Axis
  - d. This is not the correct answer

- 5. A graph of directed distance reaches a maximum. What is the velocity there?
  - a. Positive
  - b. Negative
  - c. Zero
  - d. This is not the correct answer
- 6. A car is driving at a constant velocity of 60 miles per hour. A perspective has been chosen so that directed distance is increasing. Since velocity is constant, we know that the directed distance is a linear function. What is the slope of that linear function?
  - a. 40 miles per hourb. 50 miles per hourc. 60 miles per hourd. 70 miles per hour
- 7. If from ground level we toss a rock upward with a velocity of 30 feet per second, we can use elementary physics to show that the height in feet of the rock above the ground t seconds after the toss is given by  $S = 30t 16t^2$ . How high does the rock go?
  - a. 18.06 b. 17.06 c.15.06 d. 14.06
- 8. If from ground level we toss a rock upward with a velocity of 30 feet per second, we can use elementary physics to show that the height in feet of the rock above the ground t seconds after the toss is given by  $S = 30t 16t^2$ . When does the rock strike the ground?
  - a. 3.88 seconds after it is tossed
  - b. 2.88 seconds after it is tossed
  - c. 1.88 seconds after it is tossed
  - d. 0.88 seconds after it is tossed

 The following table shows the cumulative number of cases of SARS (severe acute respiratory syndrome) on selected days during the outbreak in 2003. Here t is time in days since the beginning of April and N is the cumulative number of cases reported by time t.

t	19	22	24	29
Ν	3547	3947	4439	5642

Approximate the value of  $\frac{dN}{dt}$  at t=19 using the average rate of change from t=19 to t=22.

- a. 155.55 cases per day
- b. 144.44 cases per day
- c. 133.33 cases per day
- d. 122.22 cases per day
- 10. If  $\frac{df}{dx}$  has a constant value of 10, we know that f is a linear function. What is the slope of f?
  - a. 10
  - b. 20
  - c. 30
  - d. 40
- 11. Suppose f = f(x) satisfies f(3) = 8 and f(3.005) = 7.972. Estimate the value of  $\frac{df}{dt}$  at x=3.
  - a. 7.6 b. - 6.6 c. - 5.6
  - d. 4.6
- 12. By direct calculation, estimate the value of  $\frac{df}{dt}$  for  $f(x) = \frac{1}{x^2}$  at x=4. Use an increment of 0.0001.
  - a. 0.01 b. - 0.02
  - c. 0.03
  - d. 0.04

- 13. If f satisfies the equation of change  $\frac{df}{dt} = 5$ , then f is a linear function. What is the slope of f?
  - a. 5
  - b. 6
  - c. 7
  - d. 8
- 14. The water level in a tank rises 4 feet every minute. Write an equation of change that describes the height H, in feet, of the water level at time t in minutes.

a. 
$$\frac{dH}{dt} = 3$$
  
b.  $\frac{dH}{dt} = 4$   
c.  $\frac{dH}{dt} = 5$ 

d. 
$$\frac{dH}{dt} = 6$$

15. A balloon leaks air (changes in volume) at a rate of one-third the volume per minute. Write an equation of change that describes the volume V of air in balloon at time *t* in minutes.

a. 
$$\frac{dV}{dt} = \frac{-1}{3}V$$
  
b. 
$$\frac{dV}{dt} = \frac{-1}{4}V$$
  
c. 
$$\frac{dV}{dt} = \frac{-1}{5}V$$
  
d. 
$$\frac{dV}{dt} = \frac{-1}{6}V$$

- 16. What is the common mathematical term for an equation of change?
  - a. Constant Equation
  - b. Differential Equation
  - c. Irrational Equation
  - d. This is not the correct answer

17. Solve the equation of change  $\frac{df}{dx} = 3$  if the initial value of *f* is 7.

a. f = 4x + 8b. f = 3x + 7c. f = 2x + 6d. f = x + 5

18. Find an equilibrium solution  $\frac{df}{dx} = 2f - 6$ .

- a. f = 2b. f = 3c. f = 4d. f = 5
- 19. Water flows into a tank, and a certain part of it drains out through a valve. The volume v in cubic feet of water in the tank at time t satisfies the equation  $\frac{dv}{dt} = 5 (\frac{v}{3})$ . If the process continues for a long time, how much water will be in the tank?
  - a. 13 cubic feet
  - b. 14 cubic feet
  - c. 15 cubic feet
  - d. 16 cubic feet

20. For the equation of change  $\frac{df}{dx} = 5f - 7$ , determine whether f is increasing or decreasing when f = 1.

- a. Increasing
- b. Decreasing
- c. Stays the same
- d. This is not the correct answer