

HW2 Solutions  
Math 3338-10853: Probability (Fall 2006), Dr. Jiwen He

- 14.
- a.  $P(A \cup B) = .50 + .40 - .25 = .65$
  - b.  $P((A \cup B)') = 1 - P(A \cup B) = 1 - .65 = .35$
  - c.  $A \cap B'$ ;  $P(A \cap B') = P(A) - P(A \cap B) = .50 - .25 = .25$
- 17.
- a. Let event E be the event that at most one purchases an electric dryer. Then E' is the event that at least two purchase electric dryers.  
 $P(E') = 1 - P(E) = 1 - .428 = .572$
  - b. Let event A be the event that all five purchase gas. Let event B be the event that all five purchase electric. All other possible outcomes are those in which at least one of each type is purchased. Thus, the desired probability =  
 $1 - P(A) - P(B) = 1 - .116 - .005 = .879$
20. This situation requires the complement concept. The only way for the desired event NOT to happen is if a 75 W bulb is selected first. Let event A be that a 75 W bulb is selected first, and  $P(A) = \frac{6}{15}$ . Then the desired event is event A'.  
So  $P(A') = 1 - P(A) = 1 - \frac{6}{15} = \frac{9}{15} = .60$
22. Let S1, S2 and S3 represent the swing and night shifts, respectively. Let C1 and C2 represent the unsafe conditions and unrelated to conditions, respectively.
- a. The simple events are {S1,C1}, {S1,C2}, {S2,C1}, {S2,C2}, {S3,C1}, {S3,C2}.
  - b.  $P(\{C1\}) = P(\{S1,C1\}, \{S2,C1\}, \{S3,C1\}) = .10 + .08 + .05 = .23$
  - c.  $P(\{S1\}') = 1 - P(\{S1,C1\}, \{S1,C2\}) = 1 - (.10 + .35) = .55$
- 28.
- a.  $P(A_1') = 1 - P(A_1) = 1 - .12 = .88$
  - b.  $P(A_1 \cap A_2) = P(A_1) + P(A_2) - P(A_1 \cup A_2) = .12 + .07 - .13 = .06$
  - c.  $P(A_1 \cap A_2 \cap A_3') = P(A_1 \cap A_2) - P(A_1 \cap A_2 \cap A_3) = .06 - .01 = .05$
  - d.  $P(\text{at most two errors}) = 1 - P(\text{all three types})$   
 $= 1 - P(A_1 \cap A_2 \cap A_3)$   
 $= 1 - .01 = .99$