

Department of Mathematics

University of Houston

# Analysis Seminar

Thursday, November 17, 2016

11:00-12:00 – Room 646 PGH

**Speaker:** Nishant Suri (University of Houston)

**Title:** Naimark's problem for AF graph  $C^*$ -algebras

**Abstract:** Naimark's problem asks whether a  $C^*$ -algebra that has only one irreducible  $*$ -representation up to unitary equivalence is isomorphic to the  $C^*$ -algebra of compact operators on some (not necessarily separable) Hilbert space. This problem has been solved in special cases, including that of separable  $C^*$ -algebras and of Type I  $C^*$ -algebras. However, in 2004 Akemann and Weaver used the diamond principle to construct a  $C^*$ -algebra with  $\aleph_1$  generators that is a counterexample to Naimark's problem. More precisely, they showed that the statement "There exists a counterexample to Naimark's problem that is generated by  $\aleph_1$  elements." is independent of the axioms of ZFC. Whether Naimark's problem itself is independent of ZFC remains unknown. In this talk we examine Naimark's problem in the setting of graph  $C^*$ -algebras and show that it has an affirmative answer for (not necessarily separable) AF graph  $C^*$ -algebras. This is joint work with Mark Tomforde.