

Example:

A box contains 15 quarters, 5 nickels, 7 dimes and 8 pennies.  
You pick a coin at random from the box, what is the average value of the draw?

Solution:

**Alternative 1:** There are 35 coins in total. We want to find the average value of the drawn coin.  
Since the coins have **different values**, then we calculate the value of all in **dollars**.  
Therefore the average value will be as follows:

1 quarter = \$0.25

1 nickel = \$0.05

1 dime = \$0.10

1 cent = \$0.01

$$\frac{0.25*15+0.05*5+0.10*7+0.01*8}{35} \approx 0.14$$

i.e. The average value of the draw is about 14 cents.

**Alternative 2:** Let **X** be the random variable of **the value of the coin in dollars**. The following table gives the probability distribution of X.

X=x(in dollars)	P(X=x)
X=0.25 (coin is a quarter)	P(X=0.25)= 15/35
X=0.05 (coin is a nickel)	P(X=0.05)= 5/35
X=0.10 (coin is a dime)	P(X=0.10)= 7/35
X=0.01 (coin is a penny)	P(X=0.01)= 8/35

Thus, the expected value of the draw is:

$$E(X) = 0.25 * \frac{15}{35} + 0.05 * \frac{5}{35} + 0.10 * \frac{7}{35} + 0.01 * \frac{8}{35} \approx 0.14$$

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