## Homework \#1

You must justify all steps to get credit for your work
Please submit the HW via CASA or email your completed assignment as a single PDF file to jshi24@CougarNet.UH.EDU.
(1) [3Pts] Consider the differential equation

$$
y^{\prime \prime}-16 y=0
$$

Is any of the following functions a solution for the differential equation?
$y=\sin 4 x, y=\sinh 4 x, y=e^{-4 x}$
(2) [3Pts] Find the real numbers $r$ such that $y=e^{r x}$ is a solution of

$$
y^{\prime \prime}-6 y^{\prime}+9 y=0
$$

(3)[3Pts] Verify that $y=c_{1} e^{2 x}+c_{2} e^{-3 x}$ is the general solution of $y^{\prime \prime}+y^{\prime}-6 y=0$ and find the solution of the IVP with initial conditions $y(0)=1, y^{\prime}(0)=1$.
(4) [3Pts] Find the general solution of

$$
y^{\prime}-4 y=e^{-x}
$$

(5)[4Pts] Find the general solution of

$$
x^{2} y^{\prime}+5 x y=x^{-3} \cos (3 x)
$$

(6)[4Pts] Find the general solution of

$$
x y^{\prime}-y=\frac{5}{2} x \ln x
$$

