## Homework \#3

You must justify all steps to get credit for your work
Please submit the HW via CASA or email your completed assignment as a single PDF file to jshi24@CougarNet.UH.EDU.
(1)[4Pts] Find the general solution of the following differential equation

$$
y^{\prime \prime}-6 y^{\prime}+9 y=0
$$

(2)[4Pts] Find the general solution of the following differential equation

$$
y^{\prime \prime}-4 y^{\prime}+5 y=0
$$

(3)[4Pts] Find the general solution of the following differential equation

$$
y^{\prime \prime}+y^{\prime}+\frac{1}{4} y=0
$$

(4)[4Pts] Find the general solution of the homogeneous differential equation and solve the following IVP

$$
y^{\prime \prime}+10 y=0, \quad y(0)=5, y^{\prime}(0)=5 / \sqrt{10}
$$

(5)[4Pts] Consider the following linear second order differential equation

$$
y^{\prime \prime}+\frac{1}{x} y^{\prime}-\frac{1}{x^{2}} y=0, \quad x>0
$$

(a) Show that there are 2 solutions of the form $x^{r}$.
(b) Prove that the 2 solutions are linearly independent.
(c) Find the solution satisfying the initial condition $y(1)=0, Y^{\prime}(1)=1$

