## HW 1

Please, write clearly and justify your arguments using the theory covered in class to get credit for your work.
(1) [3Pts] Prove that

$$
\sum_{i=1}^{n} i^{2}=\frac{1}{6} n(n+1)(2 n+1) \quad n \in \mathbb{N} .
$$

(2) [3Pts] Prove that, for any $n \in \mathbb{N}$, the number $9^{n}-4^{n}$ is divisible by 5 .
(3) [3Pts] Prove that, for any $n \geq 4$ the following inequality holds

$$
n^{2} \leq 2^{n}
$$

(4) [1Pts] Let $x, y \in \mathbb{R}$ and $\epsilon>0$. Prove that is $|x-y| \leq \epsilon$, then $|x| \leq|y|+\epsilon$.

