Name:

## <u>HW 1</u>

Please, write clearly and justify your arguments using the theory covered in class to get credit for your work.

(1) [3Pts] Prove that

$$\sum_{i=1}^{n} i^2 = \frac{1}{6}n(n+1)(2n+1) \quad n \in \mathbb{N}.$$

(2) [3Pts] Prove that, for any  $n \in \mathbb{N}$ , the number  $9^n - 4^n$  is divisible by 5.

- (3) [3Pts] Prove that, for any  $n \ge 4$  the following inequality holds  $n^2 \le 2^n$ .
- (4) [1Pts] Let  $x, y \in \mathbb{R}$  and  $\epsilon > 0$ . Prove that is  $|x-y| \leq \epsilon$ , then  $|x| \leq |y| + \epsilon$ .