

HW4 Solutions  
Math 3338-10853: Probability (Fall 2006), Dr. Jiwen He

67.

a. Since the events are independent, then  $A'$  and  $B'$  are independent, too. (See paragraph below equation 2.7.)  $P(B'|A') = P(B') = 1 - .7 = .3$

b.  $P(A \cup B) = P(A) + P(B) - P(A) \cdot P(B) = .4 + .7 - (.4)(.7) = .82$

c.  $P(AB'|A \cup B) = \frac{P(AB' \cap (A \cup B))}{P(A \cup B)} = \frac{P(AB')}{P(A \cup B)} = \frac{.12}{.82} = .146$

71.  $P(\text{no error on any particular question}) = .9$ , so  $P(\text{no error on any of the 10 questions}) = (.9)^{10} = .3487$ . Then  $P(\text{at least one error}) = 1 - (.9)^{10} = .6513$ . For  $\mathbf{p}$  replacing  $.1$ , the two probabilities are  $(1-\mathbf{p})^n$  and  $1 - (1-\mathbf{p})^n$ .

77. Event A:  $\{ (3,1)(3,2)(3,3)(3,4)(3,5)(3,6) \}$ ,  $P(A) = \frac{1}{6}$ ;

Event B:  $\{ (1,4)(2,4)(3,4)(4,4)(5,4)(6,4) \}$ ,  $P(B) = \frac{1}{6}$ ;

Event C:  $\{ (1,6)(2,5)(3,4)(4,3)(5,2)(6,1) \}$ ,  $P(C) = \frac{1}{6}$ ;

Event  $A \cap B$ :  $\{ (3,4) \}$ ;  $P(A \cap B) = \frac{1}{36}$ ;

Event  $A \cap C$ :  $\{ (3,4) \}$ ;  $P(A \cap C) = \frac{1}{36}$ ;

Event  $B \cap C$ :  $\{ (3,4) \}$ ;  $P(B \cap C) = \frac{1}{36}$ ;

Event  $A \cap B \cap C$ :  $\{ (3,4) \}$ ;  $P(A \cap B \cap C) = \frac{1}{36}$ ;

$P(A) \cdot P(B) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} = P(A \cap B)$

$P(A) \cdot P(C) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} = P(A \cap C)$

$P(B) \cdot P(C) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} = P(B \cap C)$

The events are pairwise independent.

$P(A) \cdot P(B) \cdot P(C) = \frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{216} \neq \frac{1}{36} = P(A \cap B \cap C)$

The events are not mutually independent

1.

S:	FFF	SFF	FSF	FFS	FSS	SFS	SSF	SSS
X:	0	1	1	1	2	2	2	3

5. No. In the experiment in which a coin is tossed repeatedly until a H results, let  $Y = 1$  if the experiment terminates with at most 5 tosses and  $Y = 0$  otherwise. The sample space is infinite, yet  $Y$  has only two possible values.

7.

- a. Possible values are  $0, 1, 2, \dots, 12$ ; discrete
- b. With  $N = \#$  on the list, values are  $0, 1, 2, \dots, N$ ; discrete
- c. Possible values are  $1, 2, 3, 4, \dots$ ; discrete
- d.  $\{x: 0 < x < \infty\}$  if we assume that a rattlesnake can be arbitrarily short or long; not discrete
- e. With  $c =$  amount earned per book sold, possible values are  $0, c, 2c, 3c, \dots, 10,000c$ ; discrete
- f.  $\{y: 0 < y < 14\}$  since 0 is the smallest possible pH and 14 is the largest possible pH; not discrete
- g. With  $m$  and  $M$  denoting the minimum and maximum possible tension, respectively, possible values are  $\{x: m < x < M\}$ ; not discrete
- h. Possible values are  $3, 6, 9, 12, 15, \dots$  -- i.e.  $3(1), 3(2), 3(3), 3(4), \dots$  giving a first element, etc.; discrete