

MATH 4335
September 25, 2009

Exam 1 Name _____

1. Find a "heat kernel" formula for the solution to the problem:

$$u_t - ku_{xx} + bu = 0, \quad -\infty < x < \infty, \quad 0 < t < \infty$$

$$u(x,0) = \phi(x) \quad -\infty < x < \infty$$

The formula should look like:

$$u(x,t) = \int_{-\infty}^{\infty} S(x-y,t)\phi(y)dy. \quad \text{The problem is to find } S.$$

Hint: What equation is solved by $v(x,t) = e^{bt}u(x,t)$?

2. Now find a "heat kernel" formula for the solution to the problem:

$$u_t - ku_{xx} + bu = f(x,t), \quad -\infty < x < \infty, \quad 0 < t < \infty$$

$$u(x,0) = \phi(x) \quad -\infty < x < \infty$$

Be careful with $f(x,t)$!