Department of Mathematics

University of Houston

Analysis Seminar

FRIDAY, November 17, 2017

13:00-14:00 – Room 646 PGH

Speaker: Mark Wilde (Louisiana State University)

Title: Optimized quantum f-divergences and data processing

Abstract: The quantum relative entropy is a measure of the distinguishability of two quantum states, and it is a unifying concept in quantum information theory (QIT): many information measures such as entropy, conditional entropy, mutual information, and entanglement measures can be realized from it. As such, there has been broad interest in generalizing the notion to further understand its most basic properties, one of which is the data processing inequality. The quantum f-divergence of Petz is one generalization of the quantum relative entropy, and it also leads to other relative entropies, such as the Petz-Renyi relative entropies. In this talk, I introduce the optimized quantum f-divergence as a related generalization of quantum relative entropy. I prove that it satisfies the data processing inequality, and the method of proof relies upon the operator Jensen inequality, similar to Petz's original approach. Interestingly, the sandwiched Renyi relative entropies, a relatively recent development in QIT, are particular examples of the optimized f-divergence. Thus, one benefit of this result is that there is now a single, unified approach for establishing the data processing inequality for both the Petz-Renyi and sandwiched Renyi relative entropies, for the full range of parameters for which it is known to hold. I will also discuss other aspects of the optimized f-divergence, such as the classical case, the classical-quantum case, and how to construct optimized f-information measures.