

Homework 20 (5.4, models)

Problem 5.4.46 refers to problem 46 in Chapter 5, Section 4 of the online text. Record your answers to all the problems in the EMCF titled “**Homework 20.**”

1. Problem 5.4.46

- A. -5 ; $\frac{2}{3}$
- B. 5 ; $-\frac{2}{3}$
- C. doesn't exist; $\frac{2}{3}$
- D. -5 ; doesn't exist
- E. doesn't exist; doesn't exist

2. Problem 5.4.48

- A. -0.3 ; 0.5
- B. 0.3 ; doesn't exist
- C. doesn't exist; 0.5
- D. -0.3 ; $\frac{\pi}{6}$
- E. doesn't exist; doesn't exist

3. Problem 5.4.50

- A. $\frac{5}{13}$; $\frac{7}{24}$
- B. $\frac{12}{5}$; $\frac{\sqrt{674}}{7}$
- C. $\frac{5}{13}$; $\frac{24}{7}$
- D. $\frac{5\sqrt{119}}{119}$; $\frac{7}{25}$
- E. None of the above

4. Problem 5.4.52

A. $\sqrt{17}$; $\frac{4\sqrt{33}}{33}$

B. $\sqrt{17}$; $\frac{\sqrt{33}}{4}$

C. $\sqrt{15}$; $\frac{7}{4}$

D. $\frac{\sqrt{17}}{4}$; $\frac{\sqrt{33}}{7}$

E. None of the above

5. Problem 5.4.54

A. $-\frac{5\sqrt{2}}{7}$; $-\frac{3\sqrt{10}}{20}$

B. $\frac{\sqrt{2}}{10}$; $-\frac{2\sqrt{10}}{3}$

C. $\frac{7\sqrt{2}}{10}$; $-\frac{2\sqrt{10}}{3}$

D. $-\frac{7\sqrt{2}}{10}$; $-\frac{3\sqrt{10}}{20}$

E. None of the above

6. Problem 5.4.64: Which of the following points lies on the graph of the function that is given?

A. $\left(\frac{\pi}{4}, 0\right)$ B. $\left(0, \frac{\pi}{4}\right)$ C. $\left(-2, \frac{\pi}{4}\right)$ D. $\left(\frac{\pi}{4}, -2\right)$ E. $\left(-2, \frac{3\pi}{4}\right)$

7. Determine the equation of the sine function which has amplitude 2 and period 4.

A. $y = 4 \sin\left(\frac{\pi}{4}x\right)$

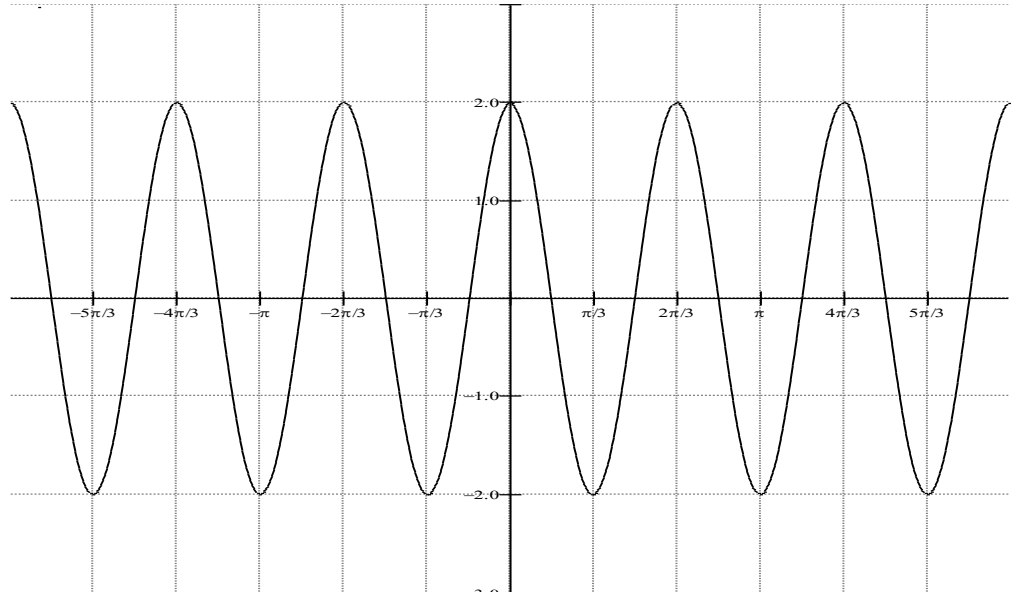
B. $y = 2 \sin(4x)$

C. $y = 4 \sin(2x)$

D. $y = 2 \sin\left(\frac{\pi}{2}x\right)$

8. Determine the period of the given graph.

- A. $\frac{\pi}{3}$
- B. 6
- C. 3
- D. π
- E. $\frac{2\pi}{3}$



9. Given the following, determine the maximum, minimum, and x-intercepts in the interval $[-2\pi, 2\pi]$.

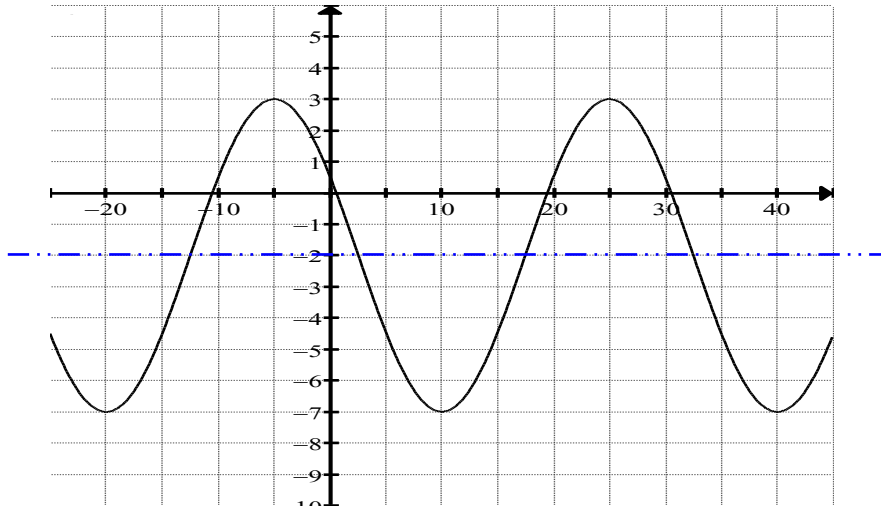
$$y = 3\cos\frac{x}{2}$$

- A. Maximum: 3 Minimum: -3 x-intercepts: $(\pm\pi, 0)$
- B. Maximum: $3/2$ Minimum: $-3/2$ x-intercepts: $(\pm\frac{\pi}{2}, 0), (\pm\frac{3\pi}{2}, 0)$
- C. Maximum: 3 Minimum: -3 x-intercepts: $(0, \pm\frac{\pi}{2}), (0, \pm\frac{3\pi}{2})$
- D. Maximum: 3 Minimum: -3 x-intercepts: $(\pm\frac{\pi}{2}, 0), (\pm\frac{3\pi}{2}, 0)$

10. The voltage V produced by an alternating current generator is $V(t) = 229\sin(120\pi t)$. What are the amplitude and period of $V(t)$?

- A. amplitude: 114.5 period: $1/60$
- B. amplitude: 229 period: $1/60$
- C. amplitude: 229 period: 120π
- D. amplitude: 229 period: 60
- E. amplitude: 458 period: $1/60$

11. Determine an equation of the form $y = A \cos B(x - C) + D$ for the following graph:



- A. $y = -5 \cos \frac{\pi}{15}(x + 10) - 2$
- B. $y = -5 \cos \frac{\pi}{30}(x - 10) - 2$
- C. $y = -5 \cos \frac{\pi}{15}(x - 10) - 2$
- D. $y = 5 \cos \frac{\pi}{15}(x - 10) - 2$
- E. $y = -5 \cos 15\pi(x - 10) - 2$
12. Assume that you are aboard a research submarine doing submerged training exercises in the Pacific Ocean. At time $t = 0$ you start porpoising (alternately deeper and then shallower). At time $t = 4$ min you are at your deepest, $y = -800$ m. At time $t = 9$ min you next reach your shallowest, $y = -200$ m. Assume that y varies sinusoidally with time. Find an equation expressing y as a function of t .
- A. $y(t) = -500 \cos \frac{\pi}{5}(t - 4) - 300$
- B. $y(t) = -300 \cos \frac{\pi}{15}(t - 9) - 500$
- C. $y(t) = -300 \cos \frac{\pi}{5}(t - 4) - 500$
- D. $y(t) = -500 \cos \frac{\pi}{15}(t - 9) - 300$
- E. None of the above (not the right answer)

13. The Pressure, P (in lbs/ft^2), in a pipe varies over time. Five times an hour, the pressure oscillates from a low of 90 to a high of 230 and then back to a low of 90. The pressure at $t = 0$ is 90. What is the period of this function in minutes?
- A. 60 minutes B. 15 minutes
C. 12 minutes D. 10 minutes
E. 5 minutes
14. Write a sine function with a positive vertical dilation, given the amplitude is 6, the phase shift is 5 to the left, the vertical shift is 4 down, and the period is 3.
- A. $y(t) = 6 \sin \frac{2\pi}{3}(x+5) - 4$
B. $y(t) = 5 \sin \frac{2\pi}{3}(x+6) - 4$
C. $y(t) = 6 \sin \frac{2\pi}{3}(x-5) - 4$
D. $y(t) = 6 \sin 3(x+5) - 4$
E. $y(t) = 6 \sin 3(x-5) - 4$
15. A signal buoy in the Gulf of Mexico bobs up and down with the height h of its transmitter (in feet) above sea level modeled by $h(t) = a \sin(bt) + 5$, where t represents seconds. During a small squall its height varies from 1 ft to 9 ft and there are 3 seconds from one 9-ft height to the next. What are the values of the constants a and b ?
- A. $a = 4; b = 3$
B. $a = 4; b = \frac{\pi}{3}$
C. $a = 9; b = \frac{2\pi}{3}$
D. $a = 4; b = \frac{2\pi}{3}$
E. $a = 1; b = \frac{2\pi}{3}$