Given $(x-3)^{2} + (y+4)^{2} = 2$, find (1) center (3,-4)A. (3,4) B. (-3,4) (C)(3,-4)(2) radius = $\sqrt{2}$

A. 2 (B.VZ C. none

Write the equation of circle with center (2,0) and radius 3. (X-2)² + (y-0)² = 3²
 (A) (x-2)² + y² = 9 B (x-2)² + (y-2)² = 9 C. X² + (y-2)² = 9
 (A) (A.
 (5) B.

The axis, or axis of symmetry, runs through the focus and is perpendicular to the directrix.

The *vertex* is the point **halfway between** the focus and the directrix.

We won't be working with slanted parabolas, just with "horizontal" and "vertical" parabolas.



From now on: get used to this new definition. Basic "Vertical" Parabola: = functions Equation: $x^2 = 4py$ Focus: (0, p) we can find Directrix: y = -pFocal Width: 4p 1 + is importantbecause it gives the opening of parabola Note: This are homistry on x^2 this function (conservation line and)

Note: This can be written as $y = f(x) = \frac{x^2}{4p}$. It is a function (passes vertical line test). Do not forget $x^2 = 4py$ $x = \frac{y}{4p}$ a function.

The line segment that passes through the focus and perpendicular to the axis with endpoints on the parabola is called the <u>focal chord</u>. Its length (called the <u>focal width</u>) is 4p.

Vertical parabolas with vertex (0,0) focal chord ► X V(d. 0) y = -pdirectrix

Example: Graph the parabola x2-16y=0. Steps: () If equation contains x², then it is a vertical parabola. $x^{2}-16y = 0 \iff vertical$ (It is a function $y = \frac{x^{2}}{16}$) (2) Bring it in standard form. x=4py x²=<mark>16</mark> y 3 Find the fours point 16=4p => p=4 => Focus (0,4) on y-axis. @ give directrix line: y = -p = -4 = y = -4⑤ Vertex ↔ (0, 0) 6 Focal width <> 4.p = 4.4 = 16 (-8,4) (8,4) -4 directrix line y=-4

Note: You have this steps for parabolas of vertex (0,0) on page 4.



Note: This is not a function (fails vertical line test). However, the top half $y = \sqrt{x}$ is a function and the bottom half $y = -\sqrt{x}$ is also a function.

Graphing parabolas with vertex at the origin:

- When you have an equation, look for x^2 or y^2
- If it has x^2 , it's a "vertical" parabola. If it has y^2 , it's a "horizontal" parabola.
- Rearrange to look like $y^2 = 4px$ or $x^2 = 4py$. In other words, isolate the squared variable.
- Determine p. find p.
- Determine the direction it opens.
 - If *p* is positive, it opens right or up.
 - \circ If p is negative, it opens left or down.
- Starting at the origin, place the focus *p* units to the inside of the parabola. Place the directrix *p* units to the outside of the parabola.
- Use the focal width 4p (2p on each side) to make the parabola the correct width at the focus.

or x=4px (> parabolos with rettex (0,0) y=4px 2 2 units right $(x-2)^2$ = (y-1)

Graphing parabolas with vertex not at the origin:

- Rearrange (complete the square) to look like $(y-k)^2 = 4p(x-h)$ or $(x-h)^2 = 4p(y-k)$.
- Vertex is (h,k). Draw it the same way, except start at this vertex.



Graph of the parabola $(x-h)^2 = 4p(y-k)$.

What to keep in rind:
•
$$(y-k)^2 = 4p(x-h)$$
 (- to graph this, is same as $y^2 = 4px$,
by shifting the vertex (0,0) to (h, k).

•
$$(x-h)^2 = 4p(y-k) \ll to graph this, is some as $x^2 = 4px$
by shifting the vertex (0,0) to (h,k) .$$





Example 2: Write $6x^2 + 24y = 0$ in standard form and graph it.









Example 3: Write $y^2 - 6y = 8x + 7$ in standard form and graph it. herizontal

$$y^{2} - 6y + 1 = 8x + 7 + 1$$

$$(\frac{4}{5} - 3)^{2} = \frac{8}{5}(x + 2)$$

$$8 - 4p \Rightarrow p = 2$$
Potent
$$y^{2} = 6x$$

$$(y - 3)^{2} = 8(x + 2)$$

$$2 = 6x$$

$$(y - 3)^{2} = 8(x + 2)$$

$$2 = 6(x + 2)$$

$$3 = -2$$

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$$\begin{aligned} y_{0}al : (x-h)^{2} = 4p(y-k) \quad or \quad (y-k)^{2} = 4p(x-h) \\ \end{aligned}$$

$$\begin{aligned} & \text{Example 4: Suppose you know that the vertex of a parabola is stat. 3.5.5.0 and its (ccro) is at (.5.5.0 Write an equation for the parabola in standard form. Since vertex and focus are on a horizontal line. Then we have a horizontal parabola:
$$(y-k)^{2} = 4p(x-h) \\ (h,k) = \text{Vertex} = (-3,5) \\ p = \text{distance bitw vertex & focus = 4} \\ \text{form in the vertex} = (-3,5) \\ p = \text{distance bitw vertex & focus = 4} \\ \text{form in the vertex} = (-3,5) \\ p = \text{distance bitw vertex & focus = 4} \\ \text{form in the vertex} = (-3,5) \\ p = \text{distance bitw vertex & focus = 4} \\ \text{form in the vertex} = (-3,5) \\ p = \text{distance bitw vertex & focus = 4} \\ \text{form in the vertex} = (-3,5) \\ p = \text{distance bitw vertex & focus = 4} \\ \text{form in the line } y = 1 \\ \text{Write an equation for the parabola is (1,3) and the directrix is the line } \\ \text{form in the line } y = 1 \\ \text{Write an equation for the parabola is (1,3) and the directrix is the line } \\ \text{form in the line } y = 1 \\ \text{Write an equation for the parabola is (1, 3) and the directrix is the line } \\ \text{form in the line } y = 1 \\ \text{Write an equation for the parabola is (1, 3) and the directrix is the line } \\ \text{form in the line } y = 1 \\ \text{form in th$$$$