

**Math 3325 Spring 2018 - Exam 2 Review**  
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Exam 2 will cover the material in Sections 2.5, 3.1–3.4\*, 4.1–4.4\* of A Transition to Advanced Mathematics (Seventh Edition) by Smith, Eggen, and St. Andre. Possible exercise types include true/false questions; statements of axioms, definitions, and major results; computational exercises; and exercises requiring theoretical arguments (proofs). The following are the most important concepts you should concentrate on while preparing yourselves for Exam 2. **Do not forget that your homework assignments serve as review exercises for your Exam.**

1. DEFINITIONS AND AXIOMS

You should be able to define and use the following.

- (1) Cartesian product of sets
- (2) Relation
- (3) Domain and range of a relation
- (4) Reflexive relation, symmetric relation, transitive relation
- (5) Equivalence relation, equivalence class
- (6) Congruence modulo  $m$  on  $\mathbb{Z}$ ,  $\mathbb{Z}_m$
- (7) Partition of a Set
- (8) Antisymmetric relation
- (9) Partial order, partially ordered set
- (10) Upper bound - supremum, lower bound - infimum
- (11) Functions: domain, codomain, range
- (12) Equality of functions
- (13) One-to-one functions; Onto functions; Bijective functions

2. COMPUTATIONAL TECHNIQUES

- (1) Compute the partition (given an equivalence relation)
- (2) Describe the equivalence relation (given a partition)
- (3) Find  $\sup(S)$ ,  $\inf(S)$ , and upper and lower bounds for  $S$ , where  $S$  is a subset of a poset.
- (4) Compute domain and range of a function.
- (5) Find composition of functions

3. PROOF TECHNIQUES

- (1) Strong (complete) induction PCI
- (2) Prove that a relation is an equivalence relation
- (3) Prove that a relation is a partial order
- (4) Prove that a relation is a function
- (5) Prove that a function is 1-1/onto.

## 4. THEORETICAL RESULTS

You should know and be able to apply the following.

- (1) Well-ordering principle for  $\mathbb{N}$
- (2) Division algorithm
- (3) Theorem 3.2.2
- (4) Theorem 3.2.3
- (5) If  $R$  is an equivalence relation on a nonempty set  $A$ , then  $\{[x] : x \in A\}$  is a partition of  $A$ .

## 5. PROOFS

- (1) Every natural number greater than 1 has a prime factor.  
(You should be able to prove by PCI method or by using Well-Ordering Principle.)
- (2) For every fixed positive integer  $m$ ,  $\equiv_m$  is an equivalence relation on  $\mathbb{Z}$  (Theorem 3.2.2).
- (3) If  $R$  is an equivalence relation on a nonempty set  $A$ , then  $\{[x] : x \in A\}$  is a partition of  $A$ .

## 6. SUGGESTED PROBLEMS

<b>2.5: 2, 5b</b>	<b>3.1: 2e</b>
<b>3.2: 2e, 5c</b>	<b>3.3: 3ef, 8a</b>
<b>3.4: 1d, 4b</b>	4.1: 6a, 11d, 18

All your homework problems are a good source of practice for your exam.