## PRINTABLE VERSION

## Practice Test 4

## Question 1

Find the $x$-intercepts of

$$
P(x)=(x-8)^{5}(x-10)^{2}(x+6)^{2}
$$

a) $\{-8,10,6\}$
b) $\{8,10,-6\}$
c) $\{8,-10,6\}$
d) $\{-7,11,-6\}$
е) $\{-8,-10,6\}$
f) None of the above

## Question 2

Find all $y$-intercept(s) of

$$
Q(x)=(x-9)^{3}(x-8)^{2}(x+2)^{5}
$$

a) $\{-9,-8,2\}$
b) $\left\{9^{3}, 8^{2}, 2^{5}\right\}$
c) $\{9,8,-2\}$
d) $9^{3} \cdot 8^{2} \cdot 2^{5}$
e) $-9^{3} \cdot 8^{2} \cdot 2^{5}$
f) None of the above

## Question 3

Which of the following functions could correspond to graph below?

a) $f(x)=-(x-3)^{2}(x+1) x^{3}$
b) $\quad f(x)=-(x+3)^{3}(x-1) x$
c) $f(x)=-(x-3)(x+1)^{2} x^{3}$
d) $f(x)=-(x+3)(x+1) x^{2}$
е) $f(x)=-(x-3)(x+1) x$
f) None of the above

## Question 4

Which of the following functions could correspond to the graph below?

a) $f(x)=-(x-1) x^{2}(x+2)^{3}$
b) $f(x)=-(x+2) x^{2}(x-1)^{3}$
c) $f(x)=-x(x-1)^{2}(x+2)^{3}$
d) $f(x)=(x-1) x^{2}(x+2)^{3}$
e) $f(x)=(x-1)(x+2)^{2} x^{3}$
f) None of the above

## Question 5

Given the polynomial

$$
p(x)=6 x^{4}-9 x^{3}+10 x+7
$$

describe the end behavior of the graph of $p$.
a)

b)

c)

d) $\nearrow \nwarrow$
е) $\swarrow \searrow$
f) None of the above

## Question 6

Given the polynomial

$$
P(x)=(x-3)^{2}(x+1)(x-2)^{3}
$$

, the behavior of the $x$-intercept $x=2$ resembles to the shape of
a) Cubic upward from left to right
b) Cubic downward from left to right
c) Parabola, downward
d) Increasing line
e) Decreasing line
f) None of the above

## Question 7

Given the polynomial

$$
P(x)=2 x^{4}+24 x^{3}+54 x^{2}
$$

, find all $x$-intercepts.
a) $x=3, x=9$
b) $x=0, x=3, x=9$
c) $x=0, x=-12, x=-9$
d) $x=0, x=-3, x=-9$
e) $x=-3, x=-9$
f) None of the above

## Question 8

Use long division to find the quotient and remainder of

$$
\frac{2 x^{3}+7 x^{2}+8 x+5}{x^{2}+x+8}
$$

a) $[\mathrm{Q}=2 x+5, \mathrm{R}=-13 x-35]$
b) $[\mathrm{Q}=2 x+5, \mathrm{R}=17 x-72]$
c) $[\mathrm{Q}=2 x+9, \mathrm{R}=3 x-40]$
d) $[\mathrm{Q}=2 x+5, \mathrm{R}=3 x+40]$
e) $[\mathrm{Q}=2 x+5, \mathrm{R}=17 x-40]$
f) None of the above

## Question 9

Use synthetic division to find the quotient and remainder of

$$
\frac{-x^{2}+x+1}{x+2}
$$

a) $[\mathrm{Q}=-x+3, \mathrm{R}=-5]$
b) $[\mathrm{Q}=-x+3, \mathrm{R}=-9]$
c) $[\mathrm{Q}=-x+5, \mathrm{R}=-5]$
d) $[\mathrm{Q}=-x+3, \mathrm{R}=-8]$
e) $[\mathrm{Q}=-x+2, \mathrm{R}=-5]$
f) None of the above

## Question 10

Use Remainder Theorem to evaluate $P(4)$

$$
P(x)=2 x^{4}-7 x^{3}+6 x-14
$$

a) 69
b) 73
c) 72
d) 74
e) 80
f) None of the above

## Question 11

Given $x=-4$ is a zero of the polynomial

$$
P(x)=x^{3}-2 x^{2}-19 x+20
$$

find the other zero of $P(x)$.
a) $x=1, x=5$
b) $x=-4, x=5$
c) $x=-1, x=4$
d) $x=-4, x=1$
e) $x=-2, x=3$
f) None of the above

## Question 12

Find the zero(s) of the function

$$
P(x)=x^{3}+2 x^{2}-25 x-50
$$

a) $\{-5,5,-2\}$
b) $\{5,-2,2\}$
c) $\{-5,5,2\}$
d) -2
e) $\{5,2\}$
f) None of the above

## Question 13

Find a polynomial with integer coefficients that satisfies the following conditions :
Degree of polynomial : 3
Zeros: 4, $3 i$
Constant coefficient: -72
a) $P(x)=x^{3}-4 x^{2}-18 x-72$
b) $P(x)=x^{3}+8 x^{2}+18 x+72$
c) $P(x)=2 x^{3}-8 x^{2}+18 x-72$
d) $P(x)=3 x^{3}-2 x^{2}+18 x-72$
e) $P(x)=x^{3}-8 x^{2}+18 x-72$
f) None of the above

## Question 14

Factor the polynomial completely and find all its zeros and their multiplicities.

$$
P(x)=x^{5}+12 x^{4}+36 x^{3}
$$

a) The zeros are: 0 of multiplicity $1,-6$ of multiplicity 4
b) The zeros are: 0 of multiplicity $3,-6$ of multiplicity 2
c) The zeros are: 0 of multiplicity 4,6 of multiplicity 1
d) The zeros are: 0 of multiplicity 2, 6 of multiplicity 2
e) The zeros are: 0 of multiplicity $4,-6$ of multiplicity 2
f) None of the above

## Question 15

Find a polynomial of degree 5 with integer coefficients that has zeros $1, \sqrt{2} i, i$, and $y$-intercept of -4 .
a) $P(x)=2(x+1)\left(x^{2}-1\right)\left(x^{2}-2\right)$
b) $P(x)=(x+1)\left(x^{2}-1\right)\left(x^{2}-2\right)$
c) $P(x)=2(x-1)\left(x^{2}-1\right)\left(x^{2}-2\right)$
d) $P(x)=2(x-1)\left(x^{2}+1\right)\left(x^{2}+2\right)$
e) $P(x)=(x-1)\left(x^{2}+1\right)\left(x^{2}+2\right)$
f) None of the above

## Question 16

Factor the polynomial into linear irreducible factors.

$$
P(x)=\left(x^{2}+5\right)\left(x^{2}+10\right)
$$

a) $P(x)=(x-\sqrt{5} i)(x+\sqrt{5} i)(x-\sqrt{10})(x+\sqrt{10})$
b) $P(x)=(x-\sqrt{5})^{2}(x-\sqrt{10})^{2}$
c) $P(x)=(x-\sqrt{5})(x+\sqrt{5})(x-\sqrt{10} i)(x+\sqrt{10} i)$
d) $P(x)=(x-\sqrt{5})(x+\sqrt{5})(x-\sqrt{10})(x+\sqrt{10})$
e) $P(x)=(x-\sqrt{5} i)(x+\sqrt{5} i)(x-\sqrt{10} i)(x+\sqrt{10} i)$
f) None of the above

## Question 17

Find the $x$-intercept(s) of the function

$$
f(x)=\frac{x^{2}-9 x+20}{x^{2}-7 x+10}
$$

a) $x=4$
b) $x=5, x=2$
c) There are no $x$-intercepts.
d) $x=5$
e) $x=2$
f) None of the above

## Question 18

Find the $y$-intercept(s) of the function

$$
f(x)=\frac{14}{x+11}
$$

a) There are no $y$-intercept.
b) 14
c) $\frac{14}{11}$
d) $-\frac{14}{11}$
e) -14
f) None of the above

## Question 19

Find the horizontal asymptote(s), if any, of the function

$$
f(x)=\frac{x-7}{x+3}
$$

a) $y=0$
b) $y=1$
c) $y=-3$
d) $y=7$
e) There are no horizontal asymptotes.
f) None of the above

## Question 20

Find the vertical asymptote(s), if any, of the function

$$
f(x)=\frac{x^{2}-17 x+66}{x^{2}-9 x+18}
$$

a) $x=6, x=3$
b) There are no vertical asymptotes.
c) $x=6$
d) $x=3$
e) $x=11$
f) None of the above

## Question 21

Find any holes of the function

$$
f(x)=\frac{x-4}{x^{2}-x-12}
$$

a) $x=-9$
b) $x=-4$
c) There are no holes.
d) $x=4$
e) $x=-3$
f) None of the above

## Question 22

Find the function, whose graph is shown below

a) $f(x)=\frac{x+2}{x+1}$
b) $f(x)=\frac{x+1}{x-2}$
c) $f(x)=\frac{x-2}{x-1}$
d) $f(x)=\frac{x-2}{x+1}$
e) $f(x)=\frac{x+2}{x-1}$
f) None of the above

## Question 23

Find the function, whose graph is shown below

a) $f(x)=\frac{(x-1)(x-5)}{x-1}$
b) $f(x)=\frac{(x-1)(x+5)}{x-1}$
c) $f(x)=\frac{(x+1)(x-5)}{x+1}$
d) $f(x)=\frac{x-1}{(x-1)(x-5)}$
e) $f(x)=\frac{x-1}{(x-1)(x+5)}$
f) None of the above

## Question 24

Write the equation $10^{x}=15$ in logarithmic form.
a) $e=\ln (15)$
b) $x=\log (15)$
c) $\ln (e x)=\ln (15)$
d) $x=\log (x)$
e) $x=\ln (15)$
f) None of the above

## Question 25

Find the asymptote and the range of the given exponential function

$$
f(x)=-4 \cdot 8^{x-4}-5
$$

a) Asymptote $y=-5$, Range $=(-\infty,-5)$
b) Asymptote $y=5$, Range $=(5, \infty)$
c) Asymptote $y=-5$, Range $=(-5, \infty)$
d) Asymptote $y=5$, Range $=(-\infty, 5)$
e) Asymptote $y=0$, Range $=(0, \infty)$
f) None of the above

## Question 26

Find the asymptote and the domain of the given logarithmic function

$$
f(x)=\ln (7 x+3)+9
$$

a) Asymptote $x=\frac{3}{7}$, Domain $=\left(-\infty, \frac{3}{7}\right)$
b) Asymptote $x=-\frac{3}{7}$, Domain $=\left(-\infty,-\frac{3}{7}\right)$
c) Asymptote $x=-\frac{3}{7}$, Domain $=\left(-\frac{3}{7}, \infty\right)$
d) Asymptote $x=\frac{3}{7}$, Domain $=\left(\frac{3}{7}, \infty\right)$
e) Asymptote $x=9$, Domain $=(-\infty, 9)$
f) None of the above

## Question 27

Which of the following functions corresponds to the graph?

a) $f(x)=-2^{x+1}-1$
b) $f(x)=-2^{x+1}+1$
c) $f(x)=-2^{x-1}-1$
d) $f(x)=2^{x-1}+1$
e) $f(x)=-2^{x-1}+1$
f) None of the above

## Question 28

Find the function, whose graph is shown below

a) $\quad f(x)=\log _{4}(x-3)$
b) $f(x)=\log _{4}(x-4)$
c) $f(x)=\log _{3}(x-4)$
d) $f(x)=\log _{4}(x+3)$
e) $f(x)=\log _{3}(x+4)$
f) None of the above

## Question 29

Suppose $a>1$. Simplify

$$
\log _{a}\left(\frac{1}{a^{3}}\right)
$$

a) 3
b) 2
c) -2
d) -3
e) -1
f) None of the above

Question 30

Simplify the following expression:

$$
\log _{4}(192)-\log _{4}(12)
$$

a) 3
b) 2
c) -4
d) -2
e) 4
f) None of the above

