

MATH 1314

Section 2.1

Solving Linear Equations

Definition: To solve an equation in the variable x using the **algebraic method** is to use the rules of algebra to isolate the unknown x on one side of the equation.

Definition: To solve an equation in the variable x using the **graphical method** is to move all terms to one side of the equation and set those terms equal to y . Sketch the graph to find the values of x where $y = 0$.

- ① Isolate the variable on one side of the equal sign
- ② Opposite operations (apply PEMDAS inverse order)
- ③ Simplify the left and right side of the equation
- ④ Variable on one side only
- ⑤* Whatever you do on the left side, must be done on the right side.

Example 1: Solve the following equation algebraically.

$$5y + 6 = -18 - y$$

$$\begin{array}{r} +y \\ +x \end{array}$$

$$6y + 6 = -18$$

$$\begin{array}{r} +6 \\ -6 \end{array}$$

$$\begin{array}{r} 6y = -24 \\ \\ \\ \end{array}$$

$$\boxed{y = -4}$$

Check ($y = -4$)

$$5(-4) + 6 = -18 - (-4)$$

$$-20 + 6 = -18 + 4$$

$$-14 = -14 \checkmark$$

Example 2: Solve following equation algebraically.

$$7 + 2(3 - 8x) = 4 - 6(1 + 5x)$$

$$7 + 6 - 16x = 4 - 6 - 30x$$

$$13 - 16x = -2 - 30x$$

$+30x$ $+30x$

$$3 + 14x = -2$$

-13 -13

$$14x = -15$$

14 14

$$x = \frac{-15}{14}$$

Example 3: Solve following equation algebraically. Fraction = Fraction \rightarrow Cross Multiply

$$\frac{2}{5}(x-1) = \frac{7}{3}$$

~~$$\frac{2(x-1)}{5} = \frac{7}{3}$$~~

$$3 \cdot 2(x-1) = 5 \cdot 7$$

$$6(x-1) = 35$$

$$6x - 6 = 35$$

$$+6 \quad +6$$

$$6x = 41$$

~~$$\frac{6x}{6} = \frac{41}{6}$$~~

$$x = \frac{41}{6}$$

Example 4: Solve following equation algebraically. LCD: $24x$

$$-\frac{3}{8x} + \frac{1}{12x} = \frac{2}{1}$$

$$\frac{-3}{8x} \cdot \frac{3}{3} + \frac{1}{12x} \cdot \frac{2}{2} = \frac{2}{1} \cdot \frac{24x}{24x}$$

$$\frac{-9}{24x} + \frac{2}{24x} = \frac{48x}{24x}$$

$$-9 + 2 = 48x$$

$$\frac{-7}{48} = \frac{48x}{48}$$

$$x = \frac{-7}{48}$$

(y=0)

(x=0)

Example 5: Find the x-intercept and y-intercept of the following equation. Express the answers in coordinate point form.

a. $-7x + 8y - 63 = 0$

x-int:

$$-7x + 8(0) - 63 = 0$$

$$-7x - 63 = 0$$

$$\begin{array}{r} +63 \\ +63 \end{array}$$

$$-7x = 63$$

$$\begin{array}{r} -7x = 63 \\ \hline -7 \quad -7 \end{array}$$

$$x = -9$$

$$(-9, 0)$$

y-int:

$$-7(0) + 8y - 63 = 0$$

$$8y - 63 = 0$$

$$\begin{array}{r} +63 \\ +63 \end{array}$$

$$\frac{8y = 63}{8} \quad y = \frac{63}{8}$$

$$(0, \frac{63}{8})$$

b. $x^2 - y - 16 = 0$

x-int:

$$x^2 - 0 - 16 = 0$$

$$x^2 - 16 = 0$$

$$\begin{array}{r} +16 \\ +16 \end{array}$$

$$x^2 = 16$$

$$\Rightarrow \sqrt{x^2} = \pm\sqrt{16}$$

$$x = \pm 4$$

$$\left. \begin{array}{l} (4, 0) \\ (-4, 0) \end{array} \right\} (\pm 4, 0)$$

y-int:

$$0^2 - y - 16 = 0$$

$$(0, -16)$$

$$-y - 16 = 0$$

$$\begin{array}{r} +16 \\ +16 \end{array}$$

$$\frac{-y = 16}{-1} \rightarrow y = -16$$

$$\rightarrow y = -16$$

c. $4x^2 - y^2 - 81 = 0$

x-int

$$4x^2 - \cancel{0} - 81 = 0$$

$$4x^2 - 81 = 0$$

$$+81 \quad +81$$

$$\frac{4x^2}{4} = \frac{81}{4}$$

$$\sqrt{x^2} = \sqrt{\frac{81}{4}}$$

$$x = \pm \frac{9}{2}$$

$(\pm \frac{9}{2}, 0)$

y-int

$$4(\cancel{0})^2 - y^2 - 81 = 0$$

$$-y^2 - 81 = 0$$

$$+81 \quad +81$$

$$\frac{-y^2}{-1} = \frac{81}{-1}$$

$$\sqrt{y^2} = \sqrt{-81}$$

$$y = \pm \sqrt{-81} \quad \begin{matrix} \text{uh} \\ \text{oh} \end{matrix}$$

No y-intercept.

