MATH 1314

Section 3.4

(We do Not Cour Section 3.3)

Transforming Functions

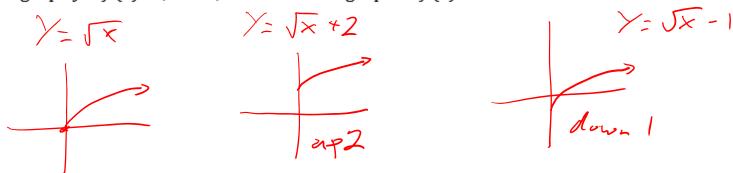
In future courses, you will need to be able to sketch the graph of a function quickly and accurately. You can use transformations to do this. There are two types of transformations:

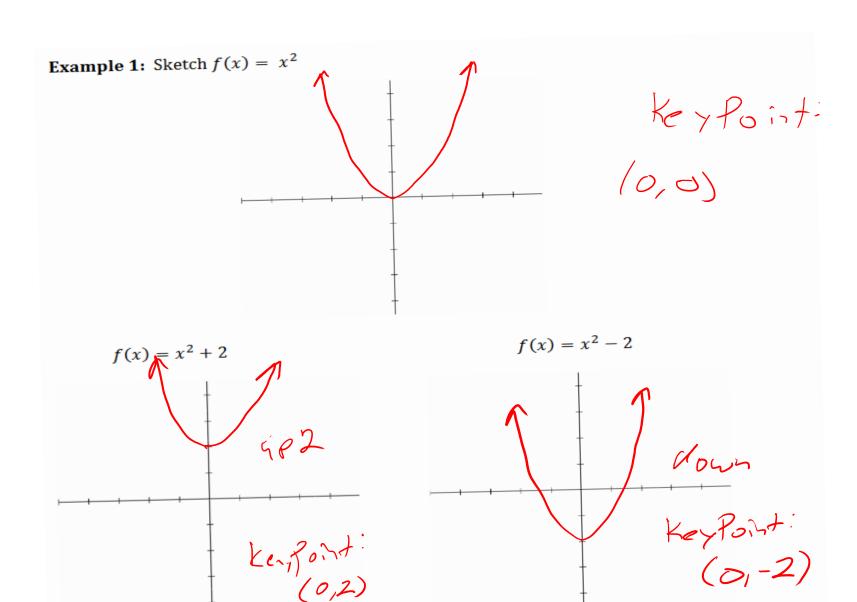
- Translation
- · Reflections

We'll start with **translations**. To **translate** a graph means to shift it horizontally, vertically or both.

Vertical shifting:

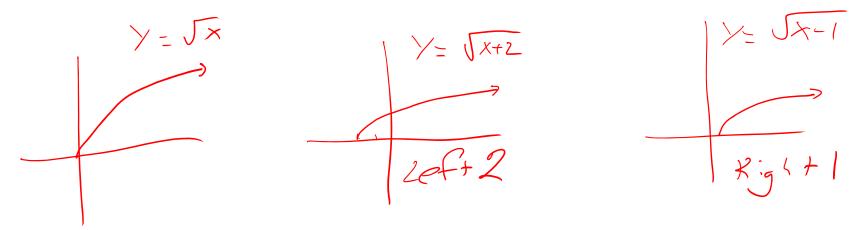
To graph y = f(x) + c, c > 0, start with the graph of f(x) and shift it upward c units. To graph y = f(x) - c, c > 0, start with the graph of f(x) and shift it downward c units.





Horizontal shifting:

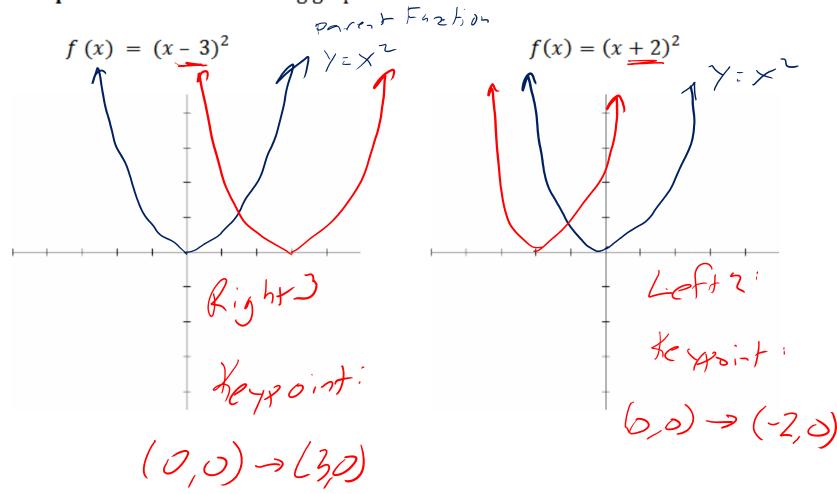
To graph y = f(x + c), c > 0, start with the graph of f(x) and shift it left c units. To graph y = f(x - c), c > 0, start with the graph of f(x) and shift it right c units.

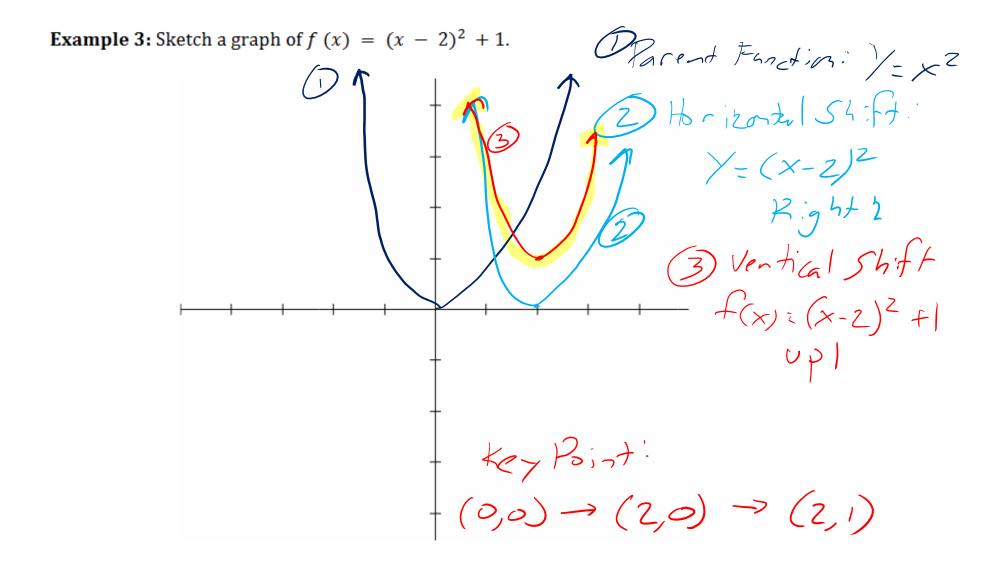


* Note: Horizontal shifting is the opposite
of the direction it appears to be

(+ -> left; - -> right)

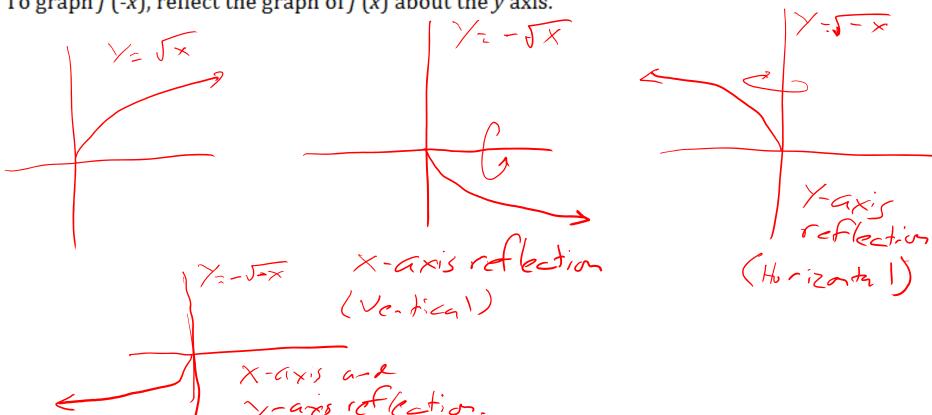
Example 2: Sketch the following graphs



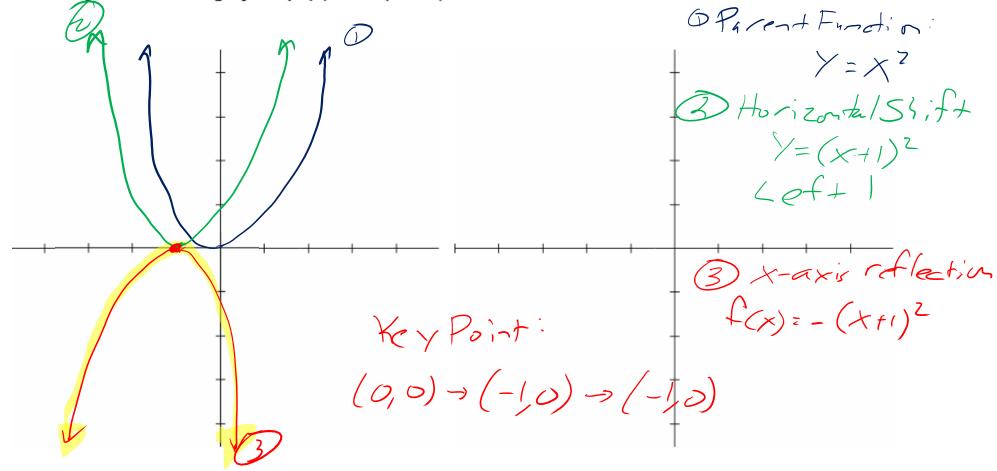


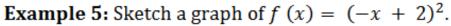
We can also reflect a function. A reflection of a function is its mirror image about the x axis or the y axis.

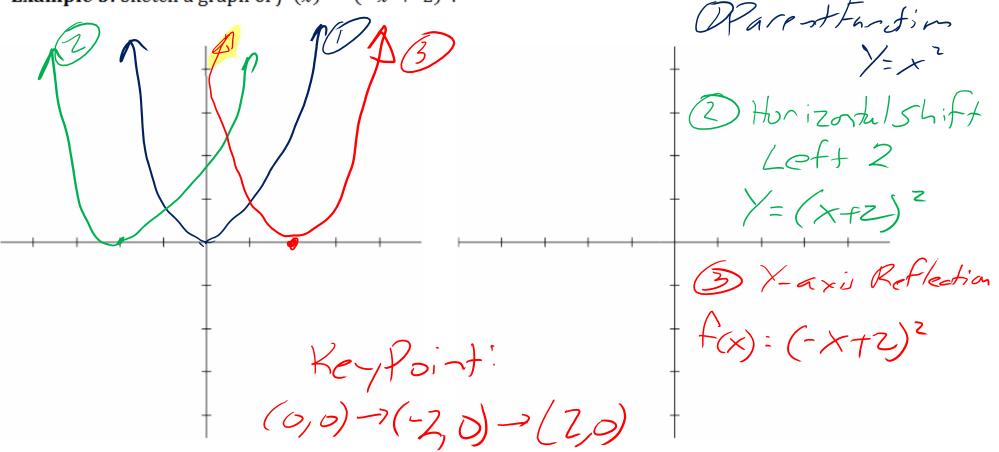
To graph -f(x), reflect the graph of f(x) about the x axis. To graph f(-x), reflect the graph of f(x) about the y axis.



Example 4: Sketch a graph of $f(x) = -(x + 1)^2$.







Popper 12: $f(x) = -\sqrt{x+2} - 5$

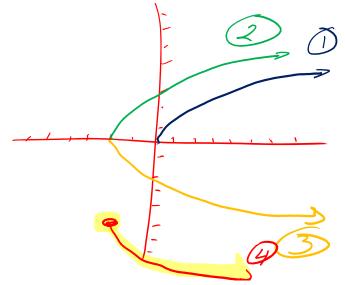


- a. Linear b. Quadratic
 - c. Rational

- $\frac{1}{2} = \frac{1}{2} = \frac{1}$
 - a. up 5
- b. up 2
- c. down 5

- d. down 2
- 3. Is there a horizontal (y-axis) reflection? b. No a. Yes
- 4. Is there a vertical (x-axis) reflection? $= \sqrt{\times}$
 - a. Yes

b. No



d. Radical