MATH 1314
Section 6.1, 6.2

## Solving $2 \times 2$ Linear Systems

To solve a system of two linear equations

$$
\left\{\begin{array}{l}
a x+b y=c \\
d x+e y=f
\end{array}\right\}
$$

means to find values for $x$ and $y$ that satisfy both equations.
The system will have exactly one solution, no solution, or infinitely many solutions.

1. Exactly one solution, will look like:

2. Infinitely many solutions, will look like:



Example 1: Solve the following systems of linear equations by the substitution method.

$$
\begin{aligned}
& 2 x-y=5 \\
& 5 x+2 y=8
\end{aligned}
$$

Example 2 : Solve the following systems of linear equations by the substitution method

$$
x-2 y=3
$$

$$
2 x-4 y=7
$$

Example 3: Solve the following systems by the Elimination Method.

$$
\begin{aligned}
& 2 x+3 y=-16 \\
& 5 x-10 y=30
\end{aligned}
$$

Example 4: Solve the following systems by the Elimination Method.

$$
\begin{aligned}
& x+4 y=10 \\
& \frac{1}{2} x+2 y=5
\end{aligned}
$$

$$
\begin{aligned}
& x^{2}+y=120 \\
& x^{2}-y=80
\end{aligned}
$$

## Application Question:

Two integers have a sum of 35 . The difference when subtracting the larger from twice the smaller is 10 . What are the two numbers?

A parking garage for a concert venue needs to report to the local safety board the percent of motorcycles that were parked in the garage on the night a certain event. That night, the garage sold parking passes to a total of 340 vehicles (included cars: charged $\$ 10$ each, seating 4; motorcycles: charged $\$ 5$ each, seating 1 ; and busses: charged $\$ 25$ each, seating 20 ). The parking garage earned $\$ 3275$ for selling parking tags that evening, and was able to accommodate 1355 ticket holders. What percent of vehicles parked were motorcycles?

Create an equation [Eq 1] for the total number of vehicles parked?
Create an equation [Eq 2] for the total money earned by the garage?
Create an equation [Eq 3] for the total number of ticket holders?

Solve Eq 3 for m.

Substitute your answer to Question 4 into Eq 1 and Eq 2 and simplify.

Solve Eq 2 for c.

Substitute your answer to Question 6 into Eq 1 and simplify.

Solve Eq 1 for b.

Solve for c and m .

What number should be reported to safety board, round to the nearest whole number, calculator is acceptable? (Look back at the original equation)

