Section 2.2 Applications of Linear Programming Problems

Example 1: A company produces two models of clock radios. Each model A requires 15 min of work on assembly line I and 10 min of work on assembly line II. Each model B requires 10 min of work on assembly line I and 12 min of work on assembly line II. At most, 23 hr of assembly time on line I and 22 hr of assembly time on line II are available per work day. It is anticipated that the company will realize a profit of \$12 on each model B. How many clock radios of each model should be produced per day in order to maximize the company's profit?

a. Define your variables.

x= #ofmodelA y= # of model B

b. Construct and fill-in the following table.

ABMAX
HR $atmost \leq$ ASMBLYLINE I15 min10 ming ≤ 23 ms = 1380 minsASMBLYLINE II10 mins12 mins ≤ 22 ms = 1320 minsPROFIT12\$10

c. State the Linear Programming Problem. Do not solve.

Max P(x,y) = 12x +10y subject to : 15x +10y <= 1380 10x +12y <= 1320 X 30 Y 20 Example 2: A manufacturer makes camping tents, a standard model and a deluxe model. Each standard tent requires **1 labor-hour** from the cutting department and **3 labor-hours** from the assembly department. Each deluxe tent requires **2 labor-hours** from the cutting department and **4 labor-hours** from the assembly department. The maximum labor-hours available per week in the cutting department and the assembly department are 32 and 84, respectively. In addition, the distributor, because of demand, will not take more than 12 deluxe tents per week. If the company makes a profit of \$50 on each standard tent and \$80 on each deluxe tent, how many tents of each type should be manufactured each week to maximize the total weekly profit?

y = # Deluxe tents

a. Define your variables.

X=# standard tents

b. Construct and fill-in the following table.

	Standard	Deluxe	Max hr	
Cutting Dept.	Ihr	2 hr	4	32h75
Assembly Dept.	3 hos	-917r S	5	8thrs
Profit	50	\$80		

c. State the Linear Programming Problem. Do not solve.

Max P(x,y) = 50x + 80ySubject to ! $x + 2y \le 32$ $3x + 4y \le 84$ $y \le 12$ x > 0, y > 0 Example 3: You're a dietician in a hospital and must arrange a special diet composed of two foods, Balanced Diet and Nutritional Goods. Each ounce of Balanced Diet contains 30 units of calcium, 10 units of iron, 10 units of vitamin A, and 8 units of cholesterol. Each ounce of Nutritional Goods contains 10 units of calcium, 10 units of iron, 30 units of vitamin A, and 4 units of cholesterol. If the minimum daily requirements are 360 units of calcium, 160 units of iron, and 240 units of vitamin A, how many ounces of each food should be used to meet the minimum requirements and at the same time minimize the cholesterol intake?

a. Define your variables.

X = # ounces of BD

y= # ounces ING

b. Construct and fill-in the following table.

	BD	NG	
Calcium Iron	30	10	7,360
	10	10	7,360 7,160
VitA	10	30	7 240
in chol	8	4	

c. State the Linear Programming Problem. Do not solve.

Example 4: The officers of a high school senior class are planning to rent buses and vans for a class trip. Each bus can transport 40 students, requires 3 chaperones, and costs \$1,200 to rent. Each van can transport 8 students, requires 1 chaperone, and cost \$100 to rent. The officers must plan to accommodate at least 400 students. Since only 36 parents have volunteered to serve as chaperones, the officers must plan to use at most 36 chaperones. How many vehicles of each type should the officers rent in order to minimize the transportation costs? What are the minimal transportation costs?

a. Define your variables.

X= # buses

١

y=#ofvans

c. State the Linear Programming Problem.

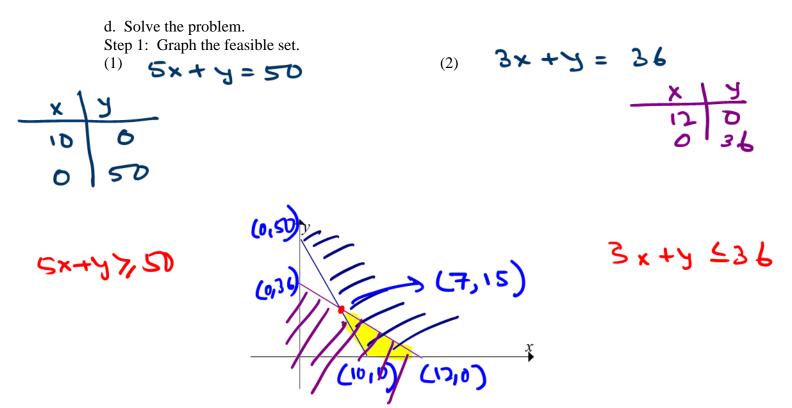
$$Min (C(X, Y)) = 1200 \times +100 \text{ y}$$

$$subject to : 40 \times +8 \text{ y} \times 400 \longrightarrow 5 \times + \frac{1}{3} \times 50$$

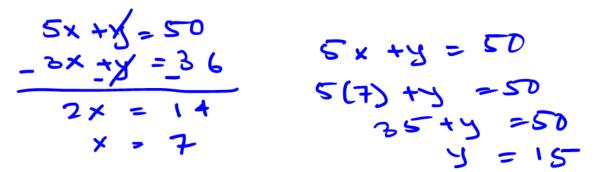
$$3 \times + \frac{1}{3} \leq 36$$

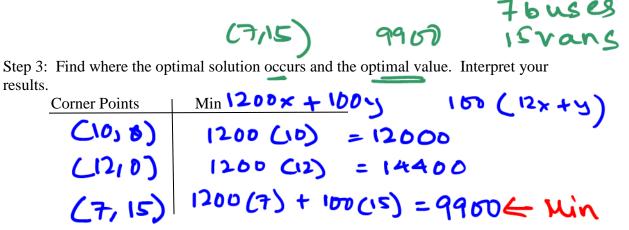
$$\times 7,0$$

$$Y \neq 0$$



Step 2: Find the corner points of the feasible set.





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minimuny

y= grams of N

Example 5: A patient in a hospital is required to have at least 84 units of drug D_1 and at least 120 units of drug D_2 each day (assume that an overdosage of either drug is harmless). Two substances, M and N, contain each of these drugs; however, in addition, both contain an undesirable drug D_3 . Each gram of substance M contains 10 units of drug D_1 , 8 units of drug D_2 and 3 units of drug D_3 . Each gram of substance N contains 2 units of drug D_1 , 4 units of drug D_2 and 1 unit of drug D_3 . How many grams of substances M and N should be mixed to meet the minimum daily requirements and at the same time minimize the intake of drug D_3 ?

a. Define your variables.

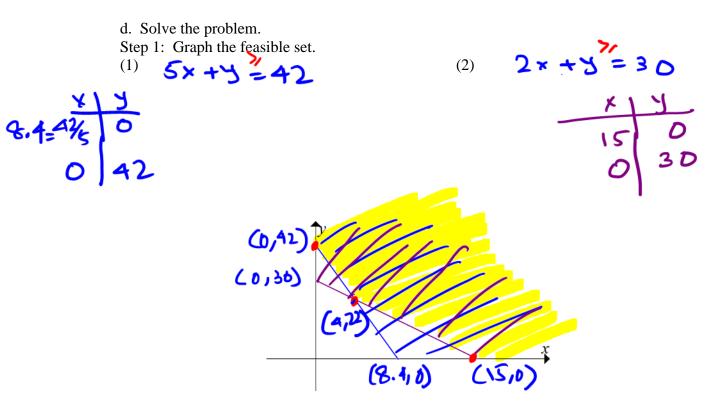
b. Construct and fill-in the following table.

		M	N	
	Ð	١D	2	789
	D_2		4	> 120
Min	Dz	3	١	

c. State the Linear Programming Problem.

Min $D_3(X,Y) = 3x + Y$ Subject to: $10x + 2y \gg 84 = 5x + y = 742$ 8x + 4y > 120 = 2x + y > 302y = 2x + y > 30

>/ min/atleast ' <' max/at most

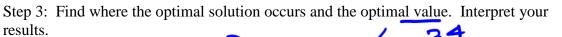


Step 2: Find the corner points of the feasible set.

(0,42) (15,0) (4,22)

5x + y' = 42_ 3D

2x + y = 302(A) + y = 30y = 22



Corner Point	s Min D3 = 3× +)	j < '3 -	Agreen of M
60,42) $3(0) + 42 =$	42	22 grows of N
(15,1) 3(15) +0 :	= 45	
(A122		= 346	Min
(T, 20) 3(5)+20 =	35	7

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