

Definition: A circle is the set of all points in a plane that are at a fixed distance from a given point known as the center.

Definitions:

radius - a segment that has one endpoint at the center of a circle and the other endpoint on the circle. Its measure is $\frac{1}{2}$ the measure of the diameter.

diameter - a chord that contains the center of a circle. Two (2) radii make up the diameter.

chord - a segment that has endpoints that lie on the circle. The diameter is considered a chord.

Formulas:

$$r = \frac{d}{2} \qquad d = 2r \qquad (r = \text{radius}, d = \text{diameter})$$

The circumference of a circle (that is...the measure around the circle) is represented by the formula:

$$C = 2\pi r \quad \text{or} \quad C = d\pi$$

When asked to find the EXACT circumference - leave the π in your answer (do not multiply it through).

Example 1:

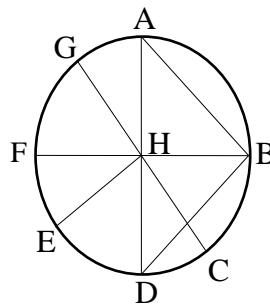
For the given circle name all the:

center:

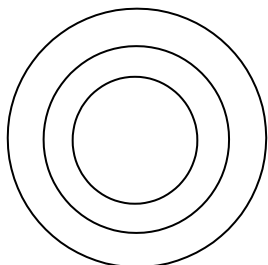
diameters:

chords :

radii:



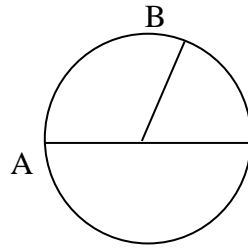
Definition: Concentric circles are coplanar circles that have a common center.



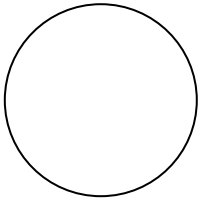
Semi-circle

Minor arc

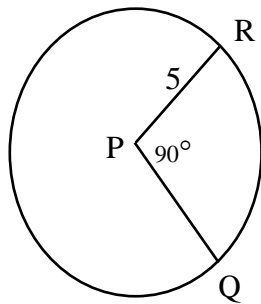
Major arc



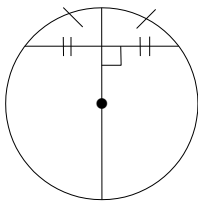
Definition: A central angle of a circle is an angle whose vertex is the center of the circle whose sides are radii.

**Example 2:**

Given the circle below, find the *length* of PQ and arc RQ

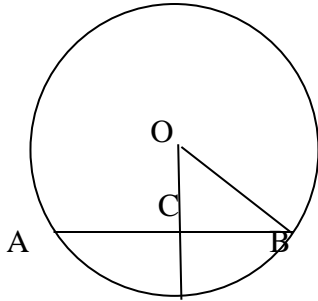


Theorem 6.1.1: A radius that is perpendicular to a chord bisects the chord.

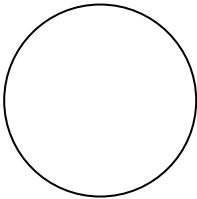


Example 3:

Given $\overline{OD} \perp \overline{AB}$ at point C. If $AB = 8$ and $OB = 5$, find OC .



Postulate 16: (Central Angle Postulate) In a circle, the degree measure of a central angle is equal to the degree measure of its intercepted arc.

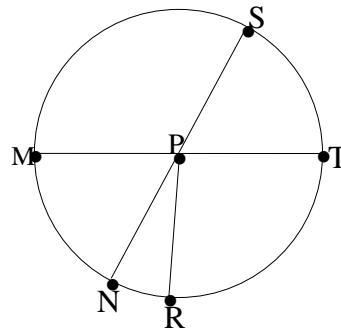


Note: the sum of the measures of consecutive arcs that form a circle is exactly 360° .

Example 4:

If \overline{SN} and \overline{MT} are diameters with $m\angle SPT = 51$ and $m\angle NPR = 29$, determine whether each arc is a minor arc, a major arc, or a semicircle. Then find the **degree measure** of each arc.

1. $m\text{NR}$
2. $m\text{ST}$
3. $m\text{TRS}$
4. $m\text{MST}$



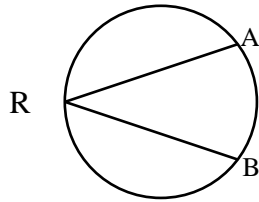
Definition: In a circle or congruent circles, congruent arcs with equal measures.

Postulate 17: (Arc –Addition postulate) If B lies between circle A and C on a circle, then measure of arc AB + the measure of arc BC = the measure of arc ABC.

Definition: An inscribed angle of a circle is an angle whose vertex is a point on the circle and whose sides are chords of the circle.

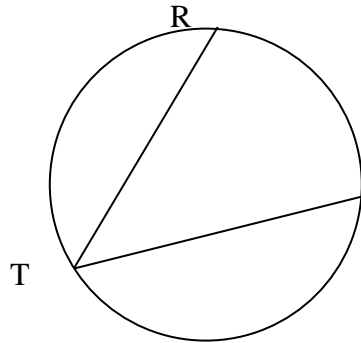
Theorem 6.1.2: The measure of an inscribed angle of a circle is one half the measure of its intercepted arc.

Inscribed Angle - an angle whose vertex is on the circle (not in the center of the circle) and whose sides contain chords.



$m\overset{\frown}{AB} = 40$ So $m\angle ARB = 20^\circ$

Example 5: Find the measure of arc RS if the $m\angle T = 30^\circ$

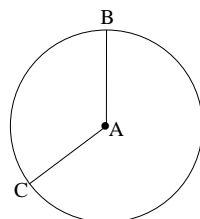


Example 6:

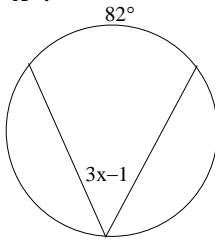
Given center A. Find the indicated information to the nearest tenth.

A. $m\overset{\frown}{BC} =$ _____

a. $m\angle BAC = 110$

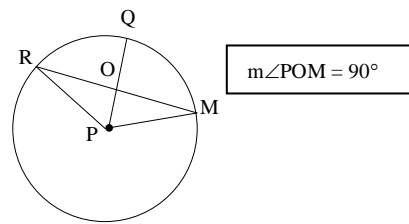


b. Find "x".



b. $x =$ _____

c. If $PR=13$ and $RM=24$, find PO .



Note: Theorems 6.1.3-6.1.10 please read over.