UH - Math 4377/6308 - Dr. Heier - Fall 2012 HW 5 Due 10/03, at the beginning of class.

Use regular sheets of paper, stapled together. Don't forget to write your name on page 1.

1. (1 point) Section 1.6, Problem 1 (Just say true or false, no further explanation necessary.)

- 2. (1 point) Section 1.6, Problem 5
- **3.** (1 point) Section 1.6, Problem 8
- 4. (1 point) Section 1.6, Problem 11
- 5. (1 point) Section 1.6, Problem 13
- 6. (1 point) Section 1.6, Problem 14
- 7. (1 point) Section 1.6, Problem 16

The next two problems give examples of how the Replacement Theorem 1.10 discussed in class works in concrete situations.

- 8. (1 point) Let $G = \{(1, -1, 0, 1), (1, 0, 1, 0), (1, 2, 2, 2), (0, 2, 2, 2)\}$. Let $L = \{(-1, 4, 2, 0)\}$.
- (a) Show that G spans \mathbb{R}^4 . (Since it has 4 elements, G is then automatically a basis, but we are only interested in the spanning property.)
- (b) Find a subset $H \subset G$ of cardinality 3 such that $H \cup L$ spans \mathbb{R}^4 . Prove the spanning property with an explicit computation.

9. (1 point) Let $L = \{(1, 2, 1, 3), (0, 0, 1, 1)\}$. Let $G = \{v_1 = (1, 2, -2, 0), v_2 = (1, 0, 0, -1), v_3 = (0, 1, 1, 1), v_4 = (1, 2, 2, 4)\}$. You can assume without proof that G spans \mathbb{R}^4 . Find two vectors in G that can be replaced by the two elements of L in such a way that the spanning property is preserved.

- 10. (1 point) Section 1.6, Problem 29
- 11. (1 extra credit point) Section 1.6, Problem 34