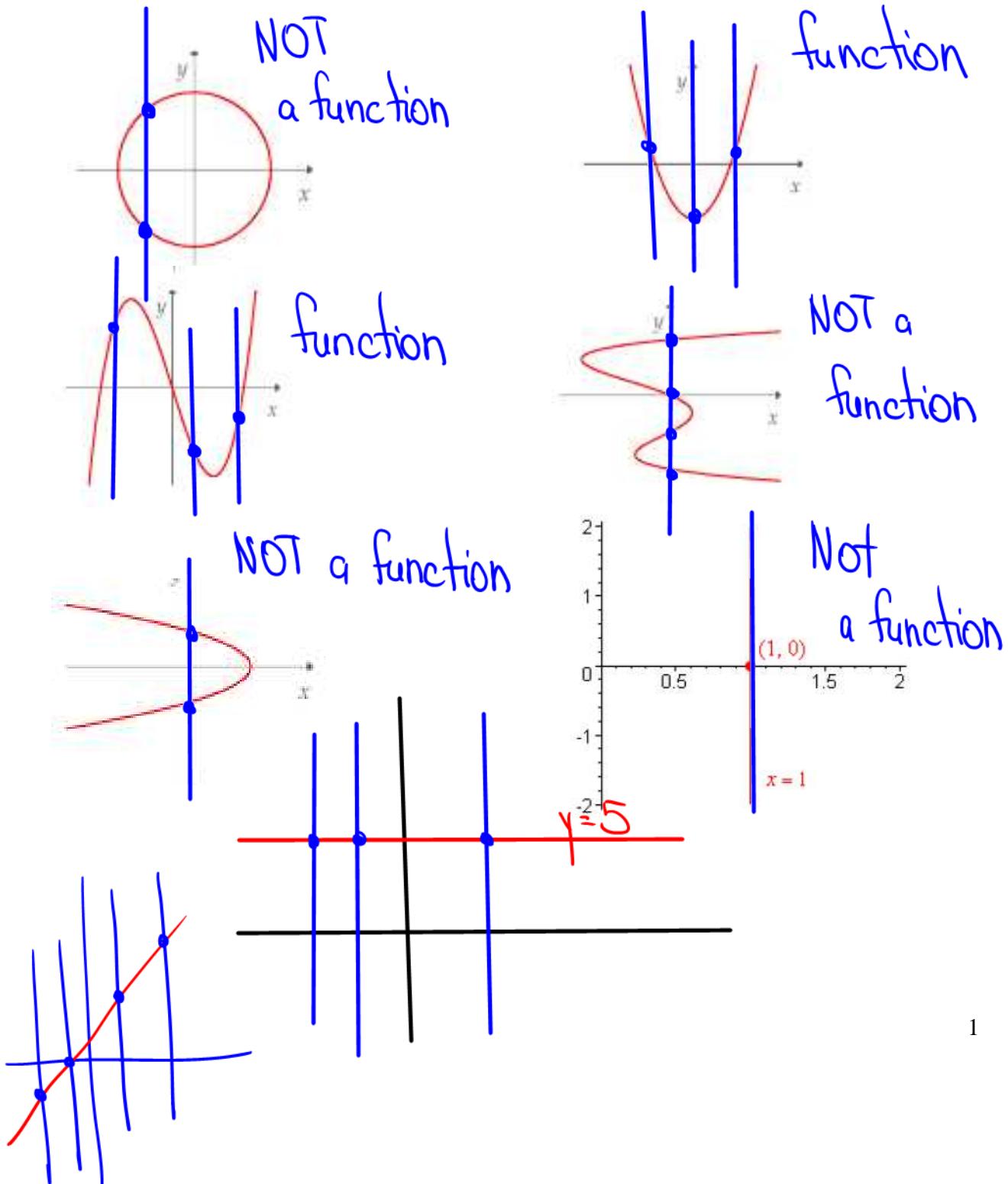


**Functions and Graphs:**

Definition: The graph of a function  $f$  is the set of all points  $(x, y)$  in the coordinate plane where the  $x$ -coordinates are the elements of the domain of  $f$  and where the  $y$ -coordinates are given by  $y = f(x)$ .

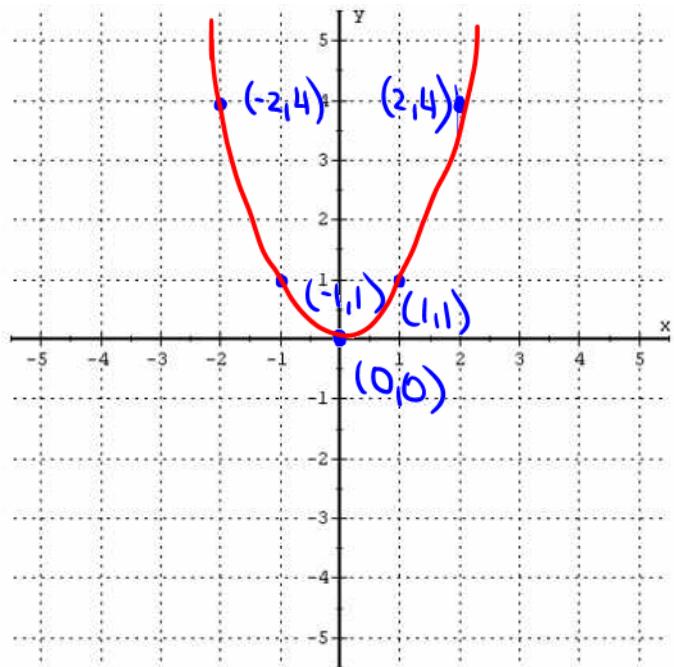
A function can have exactly (only) one  $y$ -value, called  $f(x)$ , per  $x$ -value. One way to test a relation to see if it is a function is by using the vertical line test. That is, a vertical line can intersect a graph of a function at most once.

- State whether the given graph is a function.



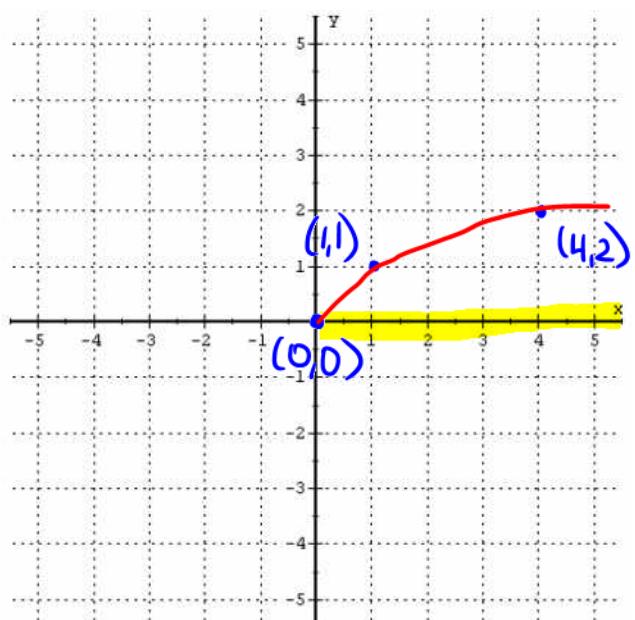
2. Sketch the graph of  $y = x^2$ . What is the domain?

$x$	$y$	Domain:
-2	$(-2)^2 = 4$	$(-\infty, \infty)$
-1	$(-1)^2 = 1$	or
0	$(0)^2 = 0$	$\mathbb{R}$
1	$(1)^2 = 1$	
2	$(2)^2 = 4$	



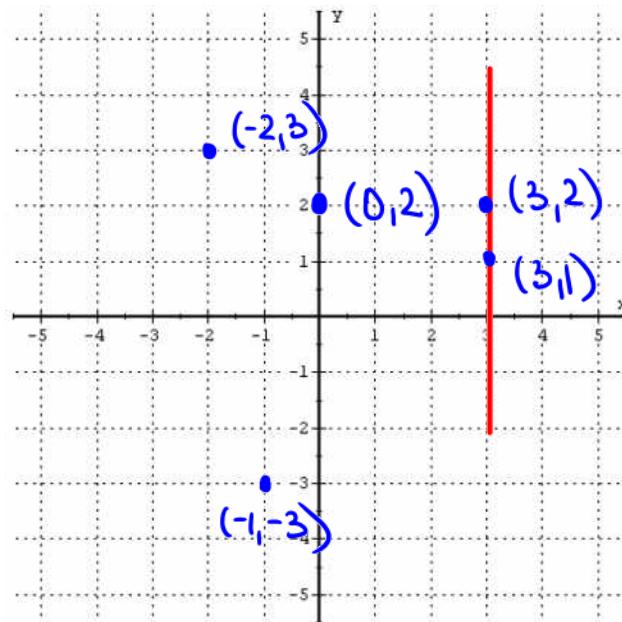
3. Sketch the graph of  $y = \sqrt{x}$ . What is the domain?

$x$	$y$	Domain: $x \geq 0$
0	$\sqrt{0} = 0$	$[0, \infty)$
1	$\sqrt{1} = 1$	
4	$\sqrt{4} = 2$	



4. Graph the set of points  $\{(-1, -3), (-2, 3), (\underline{3}, 1), (\underline{3}, 2), (0, 2)\}$ . Determine whether the set of points represents a function.

NOT a function



5. Given the following graph, find:

Domain:  $[-3, 4]$

Range:  $[-2, 2)$

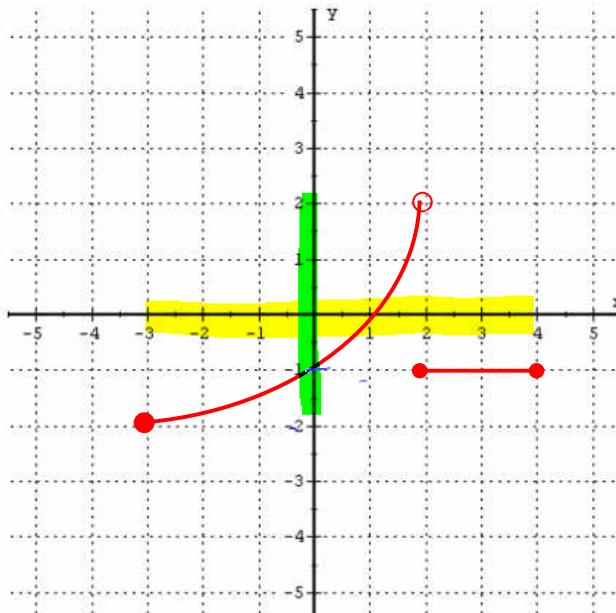
$f(-3) = -2$

$f(0) = -1$

$f(1) = 0$

$f(2) = -1$

$f(3) = -1$



6. Given the following graph, find:

Domain:  $[-4, 4]$

Range:  $[-2, 3]$

$f(-4) = -2$

$f(-3) = 3$

$f(-1) = 1$

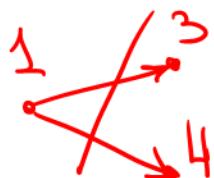
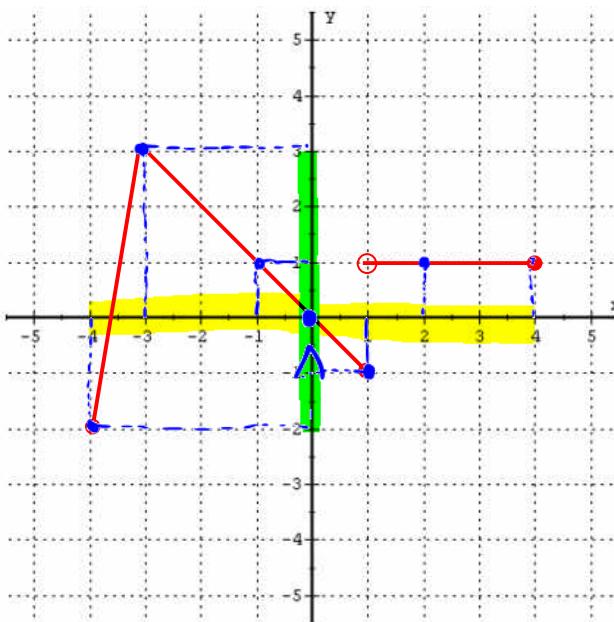
$f(0) = 0$

$f(1) = -1$

$f(2) = 1$

$f(4) = 1$

$f(1) = 3$   
 $f(1) = 4$



7. Solve for  $y$  and determine if the given equation defines  $y$  as a function of  $x$ .

$$2y + 4x = 6$$

$$\cancel{-4x} \quad \cancel{-4x}$$

$$\frac{2y}{2} = \frac{-4x+6}{2}$$

$$y = \cancel{\frac{-4x+6}{2}}$$

$$y = -2x + 3$$

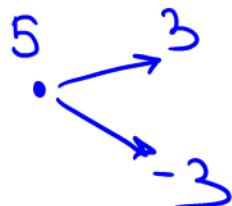
$$y = mx + b$$

Yes, function

8. Solve for  $y$  and determine if the given equation defines  $y$  as a function of  $x$ .

$$\sqrt{y^2} = \sqrt{x+4}$$

$$y = \pm \sqrt{x+4}$$



$$x = 5 \quad y = \pm \sqrt{5+4}$$

$$= \pm \sqrt{9}$$

$$= \pm 3$$

Not a function