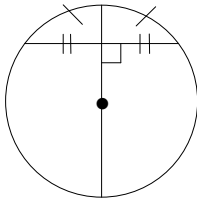


**Math 1312**  
**Section 6.3**  
**Line and Segment Relationships in the Circle**

**Theorem 1:** If a line is drawn through the center of a circle perpendicular to a chord, then it bisects the chord and its arc.

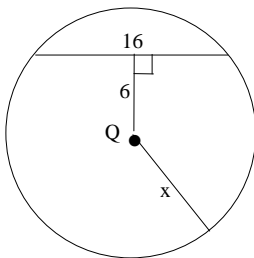
**Example 1:**



**Theorem 2** (converse of Theorem 1): If a line through the center of a circle bisects a chord other than a diameter, then it is perpendicular to that chord.

**Theorem 3:** The perpendicular bisector of a chord contains the center of the circle.

**Example 2:** Find the value of “x”.



**Definitions:**

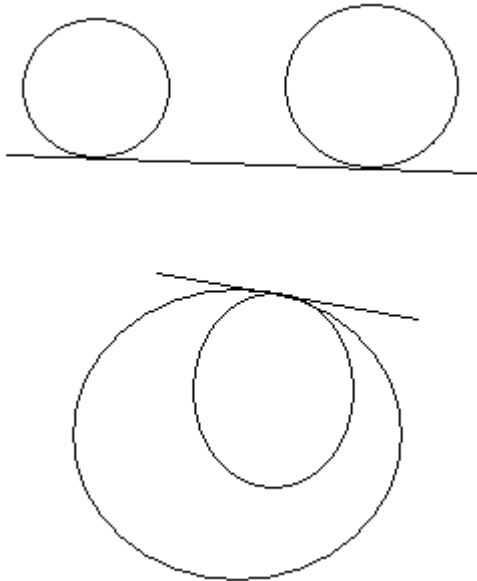
A **tangent** is a line that intersects a circle at exactly one point.

A line (or line segment) that is tangent to two circles is called a **common tangent** for these circles.

If a common tangent *does not* intersect the line of centers, it is a **common external tangent**.

If a common tangent *does* intersect the line of centers, it is a **common internal tangent**.

**Example 3:**



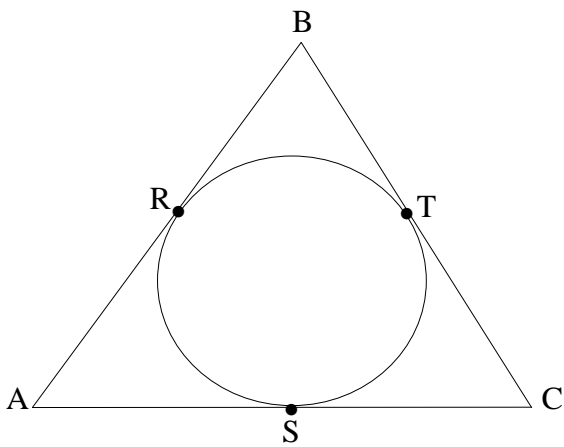
**Example 4:** Draw two circles that have exactly 3 common tangents.

**Theorem 4:** The tangent segments to a circle from the same external point are congruent.

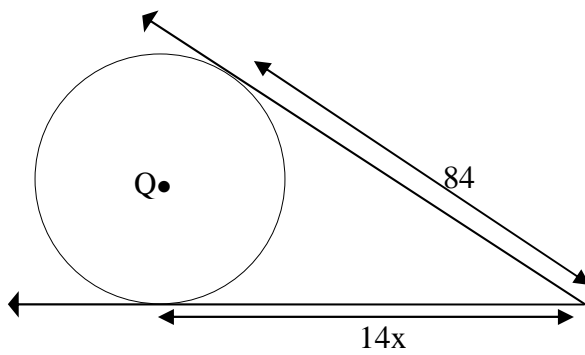
**Example 5:**



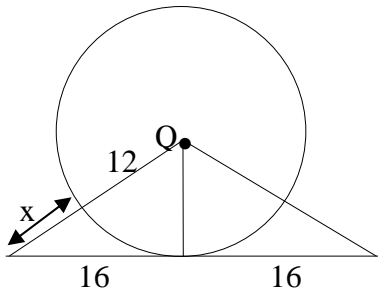
**Example 6:**



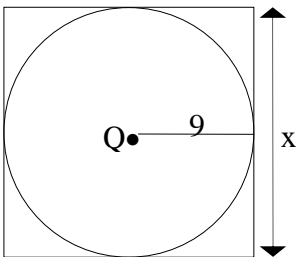
**Example 7:**



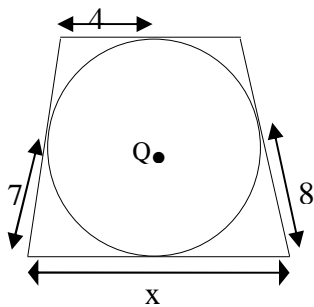
**Example 8:**



**Example 9:**

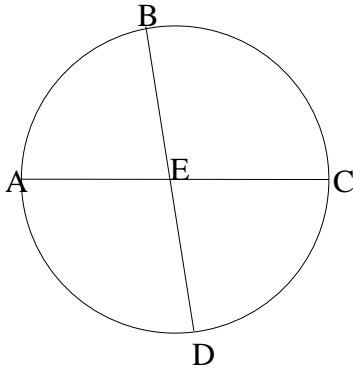


**Example 10:**



**Theorem 5:** If two chords intersect within a circle, then the product of the lengths of the segments (parts) of one chord is equal to the product of the lengths of the segments of the other chord.

**Example 11:**

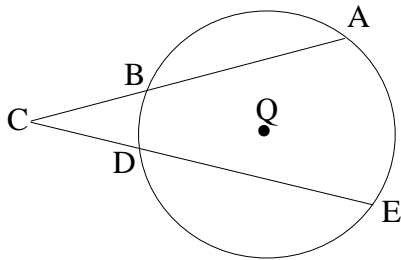


$$AE \times EC = BE \times ED$$

( *part*  $\times$  *part* )

**Theorem 6:** If two secant segments are drawn to a circle from an external point, then the products of the lengths of each secant with its external segment are equal.

**Example 11:**

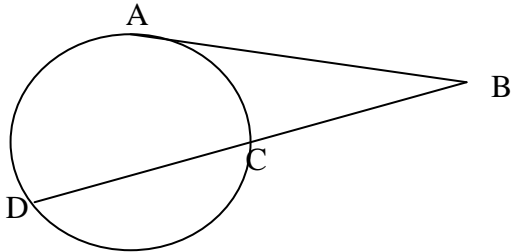


$$CA \times CB = CE \times CD$$

( *whole*  $\times$  *exterior* )

**Theorem 6:** If a tangent segment and a secant segment are drawn to a circle from an exterior point, then the square of the length of the tangent segment is equal to the product of the length of the secant with its external segment.

**Example 12:**



$$AB^2 = BD \times BC$$

**Example 13:** In the circle below,  $\overline{AB}$  and  $\overline{CD}$  are chords intersecting at  $E$ . If  $AE = 5$ ,  $BE = 12$ , and  $CE = 6$ , what is the length of  $\overline{DE}$ ?

