

# PRINTABLE VERSION

## Practice Test 4

### Question 1

Let A and B be events in a sample space S such that  $P(A) = 1/5$ ,  $P(B) = 11/25$ , and  $P(A \cap B) = 7/50$ . Find  $P(B | A^c)$ .

a) ☐ 0.4545

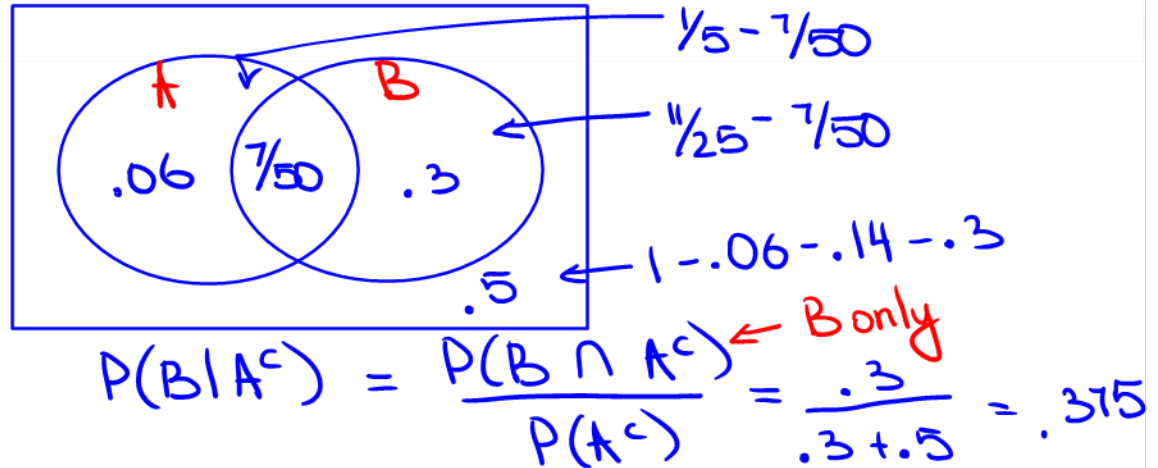
b) ☐ 0.5500

c) ☐ 0.6818

d) ☐ 0.1750

e) ☒ 0.3750

f) ☐ None of the above.



### Question 2

Two cards are drawn without replacement from a well-shuffled deck of 52 playing cards. What is the probability that the first card drawn is a 4 and the second card drawn is a 5?

a) ☐ 0.1554

b) ☐ 0.0045

c) ☐ 0.1569

d) ☒ 0.0060

e) ☐ 0.0059

f) ☐ None of the above.

$$\frac{4}{52} \cdot \frac{4}{51}$$

### Question 3

A pair of fair dice is cast. What is the probability that the sum of the numbers falling uppermost is 9, given that at least one of the numbers falling uppermost is a 3?

a) ☐ 0.5000

$$(1,3) (2,3) (3,3) (4,3) (5,3) (6,3) \\ (3,1) (3,2) (3,4) (3,5) (3,6)$$

$$\frac{2}{11}$$

- b) ☐ 0.3056
- c) ☐ 0.1111
- d) ☒ 0.1818
- e) ☐ 0.0556
- f) ☐ None of the above.

#### Question 4

A recording company obtains the blank CDs used to produce its labels from three compact disk manufacturers: I, II, and III. The quality control department of the company has determined that 5% of the compact disks produced by manufacturer I are defective, 3% of those produced by manufacturer II are defective, and 1% of those produced by manufacturer III are defective. Manufacturers I, II, and III supply 10%, 35%, and 55%, respectively, of the compact disks used by the company. What is the probability that a randomly selected label produced by the company will contain a defective compact disk?

- a) ☒ 0.0210

- b) ☐ 0.0105

- c) ☐ 0.0050

- d) ☐ 0.0900

- e) ☐ 0.0055

- f) ☐ None of the above.

Handwritten calculations for Question 4:

Manufacturer I:  $.1$  (supply),  $.05$  (defective),  $.95$  (good),  $.05$  (defective)

Manufacturer II:  $.35$  (supply),  $.03$  (defective),  $.97$  (good),  $.03$  (defective)

Manufacturer III:  $.55$  (supply),  $.01$  (defective),  $.99$  (good),  $.01$  (defective)

Formula:  $.1(.05) + (.35)(.03) + .55(.01)$

#### Question 5

There are three colored cookie jars. One jar is blue, another green and the last one pink. The blue jar contains 15 chocolate chip and 13 sugar cookies. The green jar contains 11 chocolate chip, 14 sugar and 5 peanut butter cookies. The pink jar contains 6 chocolate chip, 8 sugar and 12 peanut butter cookies.

One of the three cookie jars is chosen at random. The probabilities that the blue jar, green jar, or pink jar will be chosen are  $1/2$ ,  $1/4$ , and  $1/4$  respectively. A cookie is then chosen at random from the chosen jar.

What is the probability that the pink jar was chosen, if it is known that the cookie was a sugar cookie?

- a) ☐ 0.3077

- b) ☒ 0.1807

- c) ☐ 0.2484

Handwritten calculations for Question 5:

Jar Probabilities:  $1/2$  (Blue),  $1/4$  (Green),  $1/4$  (Pink)

Cookie Counts:

- Blue Jar: 15 Ch, 13 S
- Green Jar: 11 Ch, 14 S, 5 Peanut
- Pink Jar: 6 Ch, 8 S, 12 Peanut

Formula:

$$P(\text{Pink} | \text{Sugar}) = \frac{P(\text{Pink} \cap \text{Sugar})}{P(\text{Sugar})}$$

$$= \frac{1/4 \cdot 8/26}{1/2(13/28) + 1/4(14/30) + 1/4(8/26)}$$

~~12/26~~ S  
Peanut

- d) ☐ 0.1026
- e) ☐ 0.0769
- f) ☐ None of the above.

### Question 6

John is interested in purchasing a multi-office building containing five offices. The current owner provides the following probability distribution indicating the probability that the given number of offices will be leased each year.

| Number of Lease Offices | 0    | 1   | 2   | 3   | 4    | 5    |
|-------------------------|------|-----|-----|-----|------|------|
| Probability             | 5/28 | 1/4 | 1/7 | 2/7 | 1/28 | 3/28 |

If each yearly lease is \$12,000, how much could John expect to collect in yearly leases for the whole building in a given year?(in dollars)

- a) ☐  $E(X) = \$24,797.14$
- b) ☐  $E(X) = \$24,887.14$
- c) ☐  $E(X) = \$24,777.14$
- d) ☐  $E(X) = \$24,787.14$
- e) ☒  $E(X) = \$24,857.14$
- f) ☐ None of the above.

$$E(X) = 12000 \left( 0 \cdot \frac{5}{28} + 1 \cdot \frac{1}{4} + 2 \cdot \frac{1}{7} + 3 \cdot \frac{2}{7} + 4 \cdot \frac{1}{28} + 5 \cdot \frac{3}{28} \right)$$

### Question 7

A probability distribution has a mean of 22 and a standard deviation of 2. Use Chebychev's inequality to estimate the probability that an outcome of the experiment lies between 12 and 32.

- a) ☐ 0.2000
- b) ☐ 0.0400
- c) ☐ 0.0083
- d) ☒ 0.9600
- e) ☐ 0.9917
- f) ☐ None of the above.

$$\mu = 22 \quad \sigma = 2$$

$$P(12 < X < 32) \geq 1 - \frac{1}{5^2} = .96$$

$$P(\mu - k\sigma < X < \mu + k\sigma) \geq 1 - \frac{1}{k^2}$$

$$P(22 - 2k < X < 22 + 2k)$$

$$22 - 2k = 12 \quad 32 = 22 + 2k$$

$$-2k = -10 \quad 10 = 2k$$

$$k = 5 \quad \leftrightarrow \quad k = 5$$

**Question 8**

If the racetrack publishes that the odds in favor of a horse winning a race are 4 to 9, what is probability that the horse will not win the race?

a) ☐ 0.1111b) ☐ 0.2500c) ☐ 0.0278d) ☐ 0.3077e) ☒ 0.6923f) ☐ None of the above.

$$\frac{9}{4+9} = \frac{9}{13} = .6923$$

**Question 9**

The probability distribution of a random variable X is given below.

|          |       |      |      |      |      |
|----------|-------|------|------|------|------|
| x        | 3     | 4    | 6    | 7    | 9    |
| P(X = x) | 10/29 | 2/29 | 6/29 | 4/29 | 7/29 |

Given the following mean

$$\mu = 5.69$$

Find the variance (Var(X)) and the standard deviation, respectively.

a) ☒ [5.59, 2.37]b) ☐ [1101.00, 33.18]c) ☐ [1828.91, 42.77]d) ☐ [22.86, 4.78]e) ☐ [44.92, 6.70]f) ☐ None of the above.

$$\begin{aligned} \text{Var} &= \frac{10}{29} (3 - 5.69)^2 + \frac{2}{29} (4 - 5.69)^2 \\ &+ \frac{6}{29} (6 - 5.69)^2 + \frac{4}{29} (7 - 5.69)^2 \\ &+ \frac{7}{29} (9 - 5.69)^2 \end{aligned}$$

**Question 10**

Consider the following binomial experiment. The probability that a green jelly bean is chosen at random from a large package of jelly beans is  $1/8$ . If Sally chooses 13 jelly beans, what is the probability that at most two will be green jelly beans?

0 or 1 or 2

$$n = 13 \quad p = \frac{1}{8} \quad q = \frac{7}{8}$$

a) ☐ 0.7781b) ☐ 0.5000c) ☐ 0.2800d) ☒ 0.7841e) ☐ 0.2159f) ☐ None of the above.

$$C(13,0) \left(\frac{1}{8}\right)^0 \left(\frac{7}{8}\right)^{13} + C(13,1) \left(\frac{1}{8}\right)^1 \left(\frac{7}{8}\right)^{12} + C(13,2) \left(\frac{1}{8}\right)^2 \left(\frac{7}{8}\right)^{11}$$

**Question 11**

Consider the following binomial experiment: A company owns 6 copiers. The probability that on a given day any one copier will break down is 0.63. What is the probability that at least 4 copiers will break down on a given day?

$$n = 6 \quad p = .63 \quad q = .37 \quad 4 \text{ or } 5 \text{ or } 6$$

a) ☐ 0.5438b) ☐ 0.0002c) ☐ 0.4227d) ☐ 0.3297e) ☒ 0.6063f) ☐ None of the above.

$$C(6,4) (.63)^4 (.37)^2 + C(6,5) (.63)^5 (.37)^1 + C(6,6) (.63)^6 (.37)^0$$

**Question 12**

Consider the following binomial experiment: A company owns 15 copiers. The probability that on a given day any one copier will break down is  $\frac{2}{25}$ . Find the mean number of copiers that will break down on any given day.

$$n = 15 \quad p = \frac{2}{25}$$

$$\mu = np = 15 \left(\frac{2}{25}\right) = 1.2$$

a) ☐ 0.12b) ☐ 1.88c) ☐ 0.80d) ☐ 1.50e) ☒ 1.20

f) ☐ None of the above.

### Question 13

Let  $Z$  be a standard normal variable. Find  $P(Z < 0.19)$ .

a) ☐ 0.5398

b) ☐ 0.4602

c) ☐ 0.4247

d) ☒ 0.5753

e) ☐ 0.5793

f) ☐ None of the above.

*z-Table*

### Question 14

Let  $Z$  be a standard normal variable. Find  $P(-0.86 < Z < 2.25)$ .

a) ☐ 0.1980

b) ☐ 0.7898

c) ☒ 0.7929

d) ☐ 0.7884

e) ☐ 0.7742

f) ☐ None of the above.

$$= P(Z < 2.25) - P(Z < -.86)$$

*z-Table*

$$= .9878 - .1949$$

### Question 15

Let  $Z$  be a standard normal variable. Find the value of  $z$  if  $z$  satisfies  $P(-z < Z < z) = 0.8788$ .

a) ☐ 1.17

b) ☐ -1.10

c) ☐ 1.54

d) ☐ 1.50

$$P(Z < z) = \frac{1}{2} (1 + P(-z < Z < z))$$

$$\frac{1}{2} (1 + .8788) = .9394$$

e) ☒ 1.55

f) ☐ None of the above.

### Question 16

Let  $Z$  be a standard normal variable. Find the value of  $z$  if  $z$  satisfies  $P(Z < z) = 0.9970$ .

a) ☐ 3.00

b) ☐ -2.69

c) ☒ 2.75

d) ☐ 2.70

e) ☐ -2.75

f) ☐ None of the above.

*z-Table*

### Question 17

Suppose  $X$  is a normal random variable with

$$\mu = 35$$

and

$$\sigma = 10$$

Find  $P(3.6 < X < 53.5)$ .

a) ☐ 0.0346

b) ☐ 0.0314

c) ☐ 0.0349

d) ☒ 0.9670

e) ☐ 0.9604

f) ☐ None of the above.

$$P(3.6 < X < 53.5)$$

$$P\left(\frac{3.6 - 35}{10} < Z < \frac{53.5 - 35}{10}\right)$$

$$P(-3.15 < Z < 1.85)$$

$$= P(Z < 1.85) - P(Z < -3.15)$$

*z-Table*

$$= .9678 - .0008$$

### Question 18

Endure All, a manufacturer of batteries claims that the lifetime of their batteries is normally distributed

with a mean of 500 hours and a standard deviation of 40 hours. What is the probability that an Endure All battery selected at random will last more than 550 hours?

a) ☒ 0.1056

b) ☐ 0.1151

c) ☐ 0.8849

d) ☐ 0.8944

e) ☐ 0.1587

f) ☐ None of the above.

$$\begin{aligned}
 &P(X > 550) \\
 &P\left(Z > \frac{550 - 500}{40}\right) \\
 &P(Z > 1.25) \\
 &1 - P(Z < 1.25) = 1 - .8944 \\
 &\quad \quad \quad \uparrow \\
 &\quad \quad \quad \text{Z-Table} \quad \quad \quad = .1056
 \end{aligned}$$

### Question 19

Use the normal distribution to approximate the following binomial distribution. You claim that 73% of the voters in your district will vote for you. If the district has 350 voters, what is the probability that at least 273 will actually vote for you?

a) ☐ 0.9798

b) ☐ 0.0207

c) ☒ 0.0202

d) ☐ 0.0228

e) ☐ 0.9772

f) ☐ None of the above.

$$\begin{aligned}
 &n = 350 \quad p = .73 \quad q = .27 \\
 &\mu = np = 350(.73) = 255.5 \\
 &\sigma = \sqrt{npq} = \sqrt{350(.73)(.27)} = 8.3057 \\
 &P(X \geq 273) \\
 &= P(X > 272.5) = P\left(Z > \frac{272.5 - 255.5}{8.3057}\right) \\
 &= P(Z > 2.05) = 1 - P(Z < 2.05) \\
 &\quad \quad \quad \uparrow \\
 &\quad \quad \quad \text{Z-Table} \\
 &= 1 - .9798 = .0202
 \end{aligned}$$

### Question 20

Use the normal distribution to approximate the following binomial distribution: A convenience store owner claims that 55% of the people buying from her store, on a certain day of the week, buy coffee during their visit. A random sample of 35 customers is made. If the store owner's claim is correct, what is the probability that fewer than 24 customers in the sample buy coffee during their visit on that certain day of the week?

a) ☐ 0.9525

b) ☐ 0.9332

$$\begin{aligned}
 &n = 35 \quad p = .55 \quad q = .45 \\
 &\mu = np = 35(.55) = 19.25 \\
 &\sigma = \sqrt{npq} = \sqrt{35(.55)(.45)} = 2.9432
 \end{aligned}$$



c) ☐ 0.9463d) ☐ 0.8980e) ☒ 0.9251f) ☐ None of the above.

$$\begin{aligned} & P(X < 24) \\ &= P(X \leq 23.5) \\ &= P(X < 23.5) \\ &= P\left(Z < \frac{23.5 - 19.25}{2.9432}\right) \\ &= P(Z < 1.44) = .9251 \end{aligned}$$