

## Section 2.2

### Sets and Venn Diagrams

A **set** is a collection of objects. Two sets are equal if they contain the same elements.

The **Universal set** is the set of interest in a particular discussion.

Set  $A$  is a **subset** of set  $B$  if every element that is in set  $A$  is also in set  $B$ . The notation for this is  $A \subseteq B$ .

Set  $A$  is a **proper subset** of set  $B$  if every element that is in set  $A$  is also in set  $B$  and there is at least one element in set  $B$  that is not in set  $A$ . The notation for this is  $A \subset B$ .

The **union** of  $A$  and  $B$ , which is written as  $A \cup B$ , is the set of all elements that belong either to set  $A$  or to set  $B$  or to both  $A$  and  $B$ . *Key words in word problems will be: “or” or “either and or both”*

The **intersection** of  $A$  and  $B$ , which is written as  $A \cap B$ , is the set of all elements that belong to both set  $A$  and set  $B$ . *Key words in word problems will be: “and”, “both”, “but”, “nor”*

If the intersection of two sets is empty (the empty set is denoted by  $\emptyset$ ), then the sets are **disjoint** or **mutually exclusive** and we write  $A \cap B = \emptyset$ .

*Examples of disjoint sets: Choosing a King and a Queen from a deck of cards,  
Rolling a pair of six-sided dice and getting an even and an odd number*

The **complement of set  $A$** , which is written as  $A^c$ , is the set of all elements that are in the universal set but are not in set  $A$ . *Key word in word problems will be: “not”*

#### Some Useful Properties

$$U^c = \emptyset \qquad \emptyset^c = U \qquad (A^c)^c = A$$

$$(A \cup B)^c = A^c \cap B^c \qquad (A \cap B)^c = A^c \cup B^c$$

Example 1: Let  $A = \{2,4,6\}$ ,  $B = \{3,6,9\}$ ,  $C = \{0,6,7\}$ , and  $U = A \cup B \cup C$

a. Find  $A^c$ .

b. Find  $A \cap C$ .

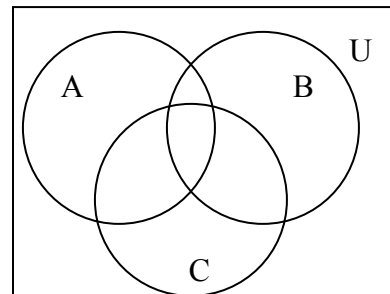
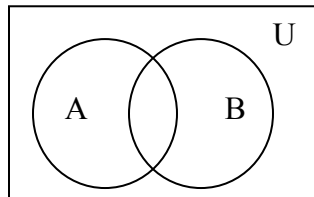
c. Find  $(A \cup C)^c$

d. Is  $C \subset U$ ?

e. Find  $C \cap (A \cup B^c)^c$

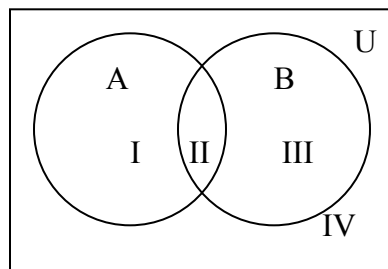
A **Venn diagram** is a visual representation of sets.

Some look like:

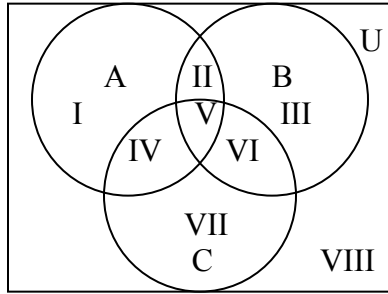


Example 2: Use shading to state the region(s) that represent(s) the given set. (Assume the given sets are not disjoint. This is obvious from the Venn diagrams.)

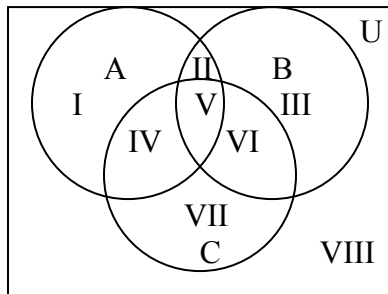
a.  $(A \cap B^c)$



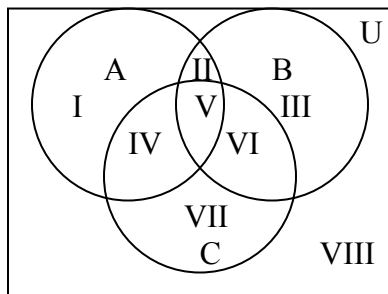
b.  $(A \cup B)^c$



c.  $(A^c \cup (B \cap C))$



d.  $(A \cap (B \cup C))$



Example 3: In a survey of 374 coffee drinkers it was found that 227 take sugar, 245 take cream, and 163 take sugar and cream with their coffee. Use a Venn diagram to answer the following questions.

a. How many take sugar but not cream with their coffee?

b. How many take sugar or cream?