

## Section 5.2 Correlation

The strength and direction association between two variables can be measured. This measure is called the **correlation coefficient** and is denoted by  $r$  (for a sample and  $R$  for a population).

### Facts about Correlation:

1.  $-1 \leq r \leq 1$
2. Positive  $r$  indicates positive association. Negative  $r$  indicates negative association.
3. The closer  $|r|$  is to 1, the stronger the association. A weak association will have an  $r$  close to 0.
4. Correlation is strongly influenced by outliers. *Recall: Outliers are observations that are “distant” from the rest of the data.*

Example 1: Recall the following example from Section 5.1, Example 2:

The bivariate data given below relate the high temperature reached on a given day and the number of water bottles sold from a particular vending machine.

Temperature (in degrees)	Bottled Water (16 oz)
90	30
91	32
88	29
93	33
92	31
89	29
90	30
91	31
92	32
94	34

- a. Find the correlation for the data.

*In R, we created two lists:*

```
>temp=c(90,91,88,93,92,89,91,92,94)
>bottles=c(30,32,29,33,31,29,30,31,32,34)
```

The command for correlation is `cor(x,y)`.

Command:

Answer:

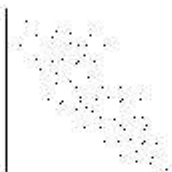
- b. Does the data have a strong positive linear association?

## Scatter Diagram Correlation

**Strong Negative Correlation**



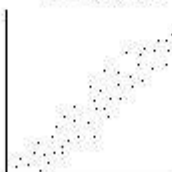
**Weak Negative Correlation**



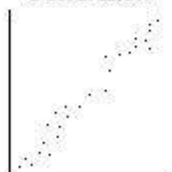
**No Correlation**



**Weak Positive Correlation**



**Strong Positive Correlation**



Example 2: Estimate the correlation coefficient for each scatter plot. Choose from:

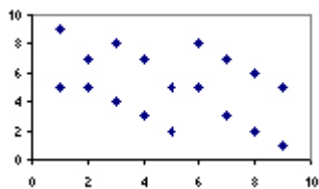
$r = -1$

$r = -0.43$

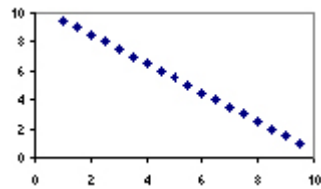
$r = 0$

$r = 0.71$

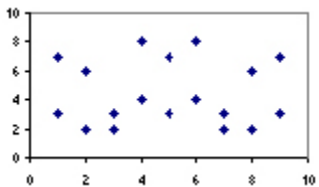
a.



b.



c.



d.

