

Info...

- Complete quizzes 6, 7 and 8 asap.
- Homework is due on Monday.
- Next week's EMCF's and Homework are posted.

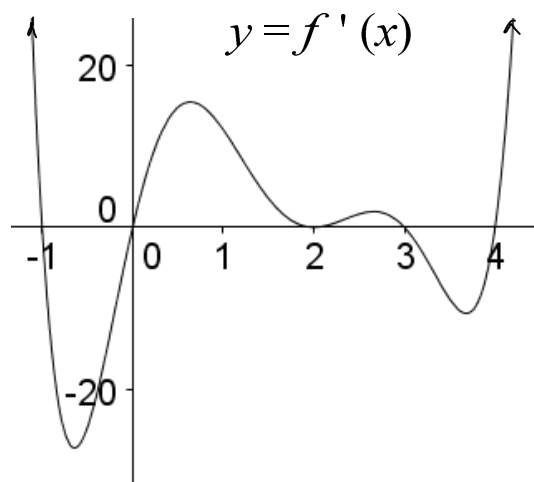
Popper P15

1. The graph of the derivative of $f(x)$ is given. Give the smallest value of x where a local minimum occurs.

2. The graph of the derivative of $f(x)$ is given. Give the largest value of x where a local minimum occurs.

3. The graph of the derivative of $f(x)$ is given. Give the smallest value of x where a local maximum occurs.

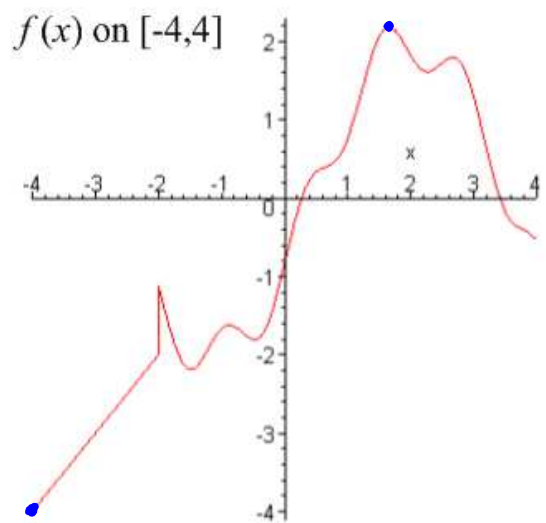
4. The graph of the derivative of $f(x)$ is given. Give the largest value of x where a local maximum occurs.



Recall: How do we determine the absolute extreme values of a continuous function on a closed bounded interval?

Answer:

1. Evaluate the function at the endpoints.
2. Evaluate the function at any critical numbers in the interval.
3. Compare these function values. The largest value is the absolute maximum value of the function, and the smallest value is the absolute minimum value of the function.



Example: Give the absolute maximum and absolute minimum values for $f(x) = -x^3 + 6x^2 + 15x - 2$ on the interval $[-2, 1]$.

Process for finding the absolute maximum and absolute minimum values of a function on a closed bounded interval.

1. Evaluate the function at the endpoints.
2. Evaluate the function at any critical numbers in the interval.
3. Compare these function values. The largest value is the absolute maximum value of the function, and the smallest value is the absolute minimum value of the function.

$$f(x) = -x^3 + 6x^2 + 15x - 2 \quad \text{on } [-2, 1]$$

polynomial $\Rightarrow f$ is continuous

1. $f(-2) = 8 + 24 - 30 - 2 = 0$.

$$f(1) = -1 + 6 + 15 - 2 = 18$$
 .

2. $f'(x) = -3x^2 + 12x + 15$

polynomial $\Rightarrow f'(x)$ exists for all x .

Set $f'(x) = 0$. $-3x^2 + 12x + 15 = 0$

$$x^2 - 4x - 5 = 0$$

$$(x-5)(x+1) = 0$$

~~$x=5$~~ , $x=-1$

only c.n. in $[-2, 1]$.

$$f(-1) = 1 + 6 - 15 - 2 = -10$$
 .

3. Compare: The abs max value of f on $[-2, 1]$ is 18, and it occurs at $x=1$.

The abmin value of f on $[-2, 1]$ is -10, and it occurs at $x=-1$.

Question: Would classifying critical values using a slope chart lead to the same answer in the previous problem?

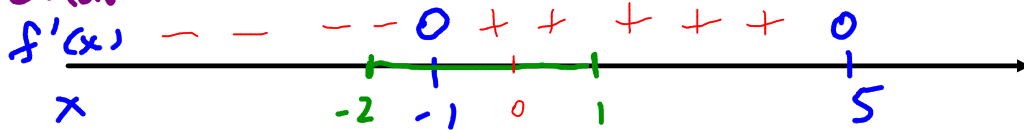
Give the absolute maximum and absolute minimum values for $f(x) = -x^3 + 6x^2 + 15x - 2$ on the interval $[-2, 1]$.

Yes. But it requires more work.

$$f'(x) = -3x^2 + 12x + 15$$

$$f'(x) = 0 \dots x = -1, x = 5$$

slope chart



$$f'(-2) = -$$

$$f'(0) = +$$

which is larger



abs. min
at $x = -1$

rough
shape
for f

Popper P15

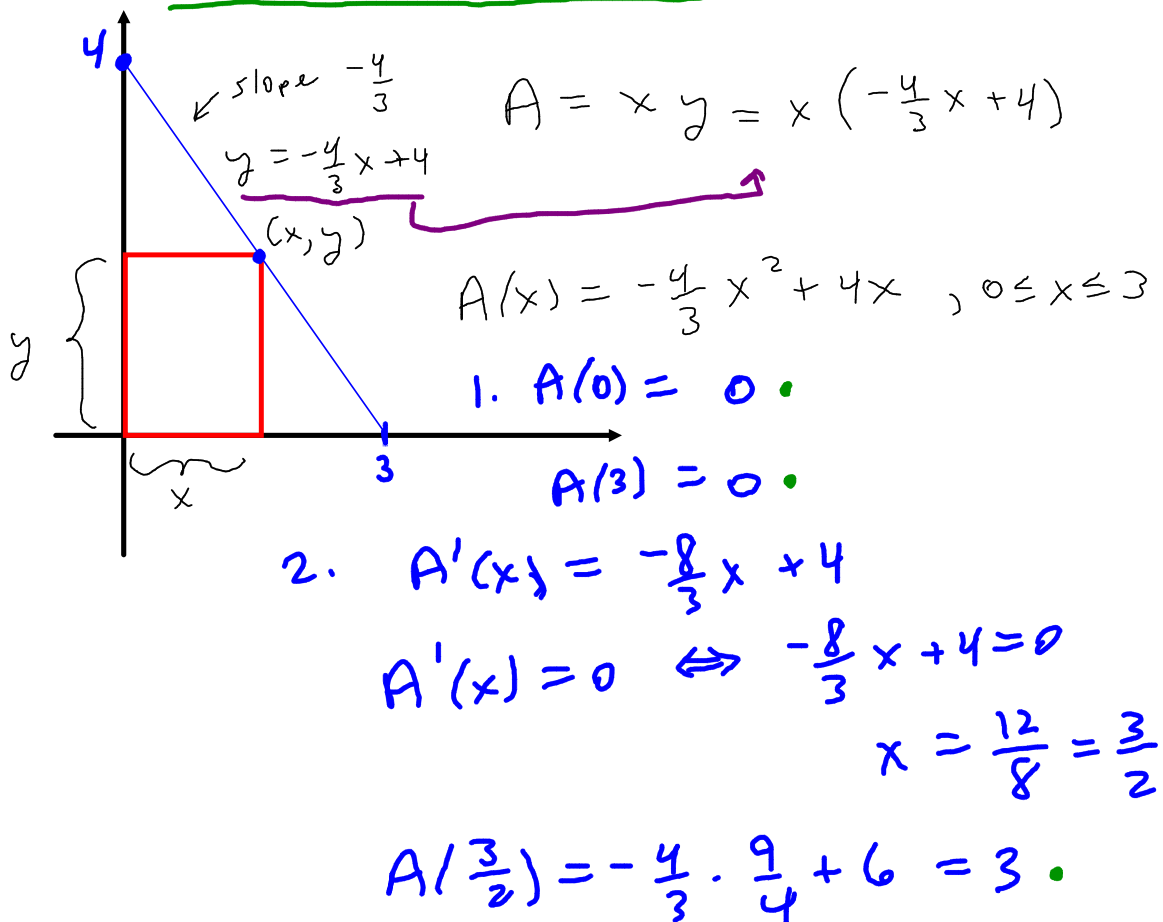
5. Give the absolute minimum value of $f(x) = -x^3 + 6x^2 + 15x - 2$ on the interval $[-1,2]$.

6. Give the absolute maximum value of $f(x) = -x^3 + 6x^2 + 15x - 2$ on the interval $[-1,2]$.

Some Max/Min Word Problems... (section 4.5)

This is what we have already been doing, except now we have a word problem that must be translated into mathematical terms before we can find the answer.

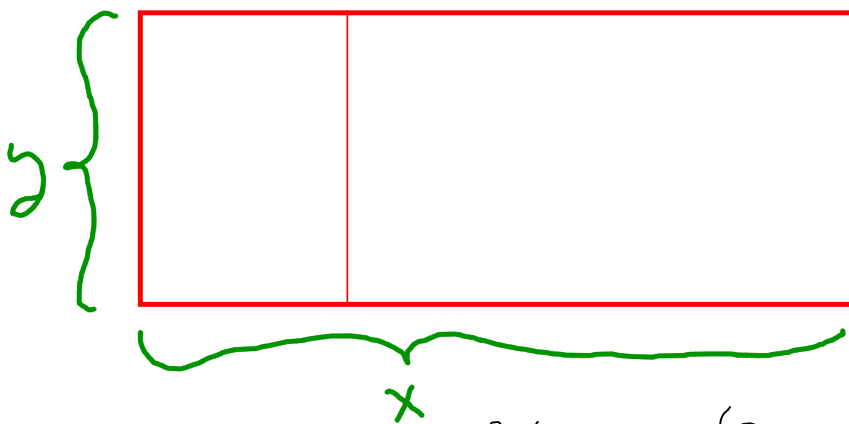
Example: A rectangle sits in the first quadrant with its base on the x -axis and its left side on the y -axis. Its upper right hand corner is on the line passing through the points $(0,4)$ and $(3,0)$. What is the largest possible area of this rectangle?



3. Compare.

The largest possible area is 3.

Example: A rectangular playground is to be fenced off and divided into two parts by a fence parallel to one side of the playground. Six hundred feet of fencing is used. Find the dimensions of the playground that will enclose the greatest total area.



$$A = xy$$

$$2x + 3y = 600$$

$$\rightarrow y = 200 - \frac{2}{3}x$$

$$A(x) = x \left(200 - \frac{2}{3}x \right), \quad 0 \leq x \leq 300$$

$$A(x) = 200x - \frac{2}{3}x^2, \quad 0 \leq x \leq 300$$

you finish it.

See video.