Math 1432 - 13209

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Jeff Morgan (651) PGH - 11-noon MWF http://www.math.uh.edu/~jmorgan/Math1432

Read the Syllabus!

Test 1 is available online at CourseWare.

Practice Test 1 is also available and counts as an online quiz.

Homework 1 is posted on the course homepage and due next Wednesday.

EMCF01 is due tomorrow morning at 9am. A help video was posted.

EMCF02 is due on Saturday morning at 9am.

Your first written quiz will be given in lab/workshop on Friday.
Online Quiz 1 is Available on CourseWare.

Poppers start week 3. Get your packet at the UC Book Store.

Access Codes are required to continue to access the online text,
EMCF, quizzes, etc... See the deadline on the course homepage.



CourseWare = http://www.casa.uh.edu

We started discussing inverse functions on Monday. The notes are posted. In addition, I posted a video that might help with EMCF01.

Today.... More Inverse Functions and Logarithms

Make sure you read sections 7.2 and 7.3.

http://www.math.uh.edu/~jmorgan/Math1432

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Read the Syllabus

Use the Discussion Board on CourseWare to get and give help.

Lecture notes/videos, additional help material, course announcements, homework and EMCFs will be posted in the calendar below. Note: Practice Tests count the same as online quizzes.

Course Calendar

Monday	Tuesday	Wednesday	Thursday	Friday	Saturday
14	15	16	17	18	19
all Online Quizzes	Examples from 7.1		EMCF01 due at 9am	Quiz in lab/workshop	EMCF02 due a 9am
20 21 MLK Day No Class	22. Last day to add	23 EMCF03 due at 9am	24 Exam 1 and PT1 close	25 EMCF04 due at 9am	26 Quiz 1 closes (7.1-7.2)
		Homework 1 due in lab/workshop Homework 2 posted		Quiz in lab/workshop	
	14 Notes Exam 1, PT1 and all Online Quizzes are open 21 MLK Day	14 UH events this week all Online Quizzes that will help with EMCF01 21 22. MLK Day Last day to add	14 Notes Last day to add No Class 14 Notes UH events this week Homework 1 posted Homework 1 posted Homework 1 posted Homework 2 21 22. MI.K Day No Class Last day to add Homework 1 due in lab/workshop	14 Notes Exam 1, PT1 and all Online Quizzes are open 21 MI.K Day No Class Last day to add Months of the class of the cla	14

"Review" What were you taught about Logarithms in highschool algebra? (base 10 answers...)

$$\log_{10}(1) = 0$$

$$\log_{10}(10) =$$

$$\log_{10}\left(\frac{1}{10}\right) = -1$$

$$\log_{10}(x) = y$$
 iff $x = 10^{9}$

$$\log_{10}(100) = 2$$

$$\log_{10}\left(10^x\right) = \times$$

Properties: If A and B are positive real "Review" numbers, and r is a real number, then

$$\log_{10}(AB) = \log_{10}(A) + \log_{10}(B)$$

$$\log_{10}\left(\frac{A}{B}\right) = \log_{10}\left(A\right) - \log_{10}\left(B\right)$$

$$\log_{10}(A^r) = \bigcap_{0 \neq 10} (A)$$

$$\log_{10}\left(\frac{1}{A}\right) = -\log_{10}\left(\Re\right)$$

"Review" For arbitrary bases... **Properties:** If A and B are positive real numbers, r is a real number, and n is a positive real number which IS NOT 1, then

$$\log_n(1) = \bigcirc$$

$$\log_n(n^x) = \chi$$



$$\log_{n}(AB) = \log_{n}(A) + \log_{n}(B)$$

$$\log_{n}(AB) = \log_{n}(A) - \log_{n}(B)$$

$$\lim_{x \to n^{y}} \inf_{x = n^{y}}$$

"Review" Change of base:

$$\log_a(b) = \frac{\log_c(b)}{\log_c(a)}$$

a,b,c>0 and $a,c\neq 1$

$$\log_{10}(x) = \frac{\log_{2}(x)}{\log_{2}(10)}$$

The Truth!

The defining property of logarithmic functions:



If
$$n > 0$$
 with $n \ne 1$ and $A, B > 0$ then $\log_n (AB) = \log_n (A) + \log_n (B)$

All other properties follow from this property.

So... We say that a real valued function L defined on the positive real numbers is a logarithmic function if and only if L is not the zero function and

$$L(AB) = L(A) + L(B)$$

(all other properties follow from this one)

Quadra: Dom L'(x) exht for x>0? If so, what is L'(x)?

A: Let
$$x, y > 0$$
. Then
$$L(xy) = L(x) + L(y)$$

$$dy L(xy) = dy \left[L(x) + L(y)\right]$$

$$L'(xy) \cdot x = 0 + L'(y)$$
Subst $y = 1$.
$$L'(x) \cdot x = L'(1)$$

$$\Rightarrow L'(x) = \frac{L'(1)}{x}$$

In fact, we could prove...

If L is a logarithmic function then L is differentiable and there is a constant

C so that

X > 0

$$L'(x) = C \cdot \frac{1}{x}$$

As a result, <u>all</u> logarithmic functions are invertible. Why?

The constant depends upon the base of the logarithm.

Questions:

 $\frac{d}{dx} \int_{-\frac{1}{2}}^{x} dt = \bot$

1. Is there a function whose derivative is $\frac{1}{x}$?

$$L(x) = \int_{1}^{x} dx$$

2. Is this a logarithmic function?

3. Is there any other logarithmic function with this derivative?

Question: How can we show that $L(x) = \int_{1}^{x} \frac{1}{t} dt$ is a logarithmic function?

Answer: We need to show L(AB) = L(A) + L(B)for A, B > 0. $\leq pse$ A > 0 and k > 0. $\frac{d}{dx}L(Ax) = L'(A \times) \cdot A = \frac{1}{A \times} \cdot A = \frac{1}{A \times}$ $\frac{d}{dx}[L(A) + L(x)] = 0 + \frac{1}{A \times}$ $\frac{d}{$

We refer to this special logarithmic function as the natural logarithm, and we denote it as
$$\ln(x)$$
.

$$\ln(x) \text{ satisfies the logarithmic properties and...}$$

$$\ln(x) = \int_{1}^{x} \frac{1}{t} dt, \quad x > 0$$

$$\frac{d}{dx} \ln(x) = \frac{1}{x} \int_{1}^{x} \frac{dt}{t} \ln(x) dt = \frac{1}{x} \int_{1}^{x} \frac{$$

Examples:
$$\frac{d}{dx} \ln(x^2 + 1) = \frac{1}{x^2 + 1} \cdot 2x = \frac{2x}{x^2 + 1}$$

$$\frac{d}{dx} \ln(u(x)) = \frac{1}{u(x)} u(x)$$

$$\int \frac{1}{2x + 3} dx = \frac{1}{2} \int \frac{1}{2x + 3} 2 dx$$

$$\int \frac{1}{2x + 3} dx = \frac{1}{2} \int \frac{1}{2x + 3} 2 dx$$

$$= \frac{1}{2} \ln(|2x + 3|) + C$$

$$\int \frac{x}{3x^2 + 5} dx = \frac{1}{6} \int \frac{1}{3x^2 + 5} \cdot 6 \times dx$$

$$= \frac{1}{6} \ln(|3x^2 + 5|) + C$$

$$= \frac{1}{6} \ln(|3x^2 + 5|) + C$$

$$\leq \ln (2x + 3) + C$$

$$\leq \ln (3x^2 + 5) + C$$

$$\leq \ln (3x^2 + 5) + C$$

$$\leq \ln (3x^2 + 5) + C$$

Example: Solve the equation
$$\ln((3x+3)(x+5)) = 2\ln(x+5)$$

$$\ln\left((3x+3)(x+5)\right) = \ln\left((x+5)^2\right)$$

Note: $x = 5$ is not allowed

in the original equation $b/c \ln a(b)$ disc.

$$3x + 3 = x + 5$$

$$2x = 2 \Rightarrow x = 1$$

$$\ln((3x+3)(x+5)) = 2\ln(x+5)$$
Such $x = 1$.

$$\ln((6x+3)(x+5)) = 2\ln(6)$$

$$2 = 2 \ln(6)$$

$$2 = 3 \ln(6)$$

$$2 = 3 \ln(6)$$

$$3 = 3 \ln(6$$

Example: Give the y-intercept of the tangent line to the graph of
$$f(x) = \ln(3x^2 - 2)$$
 at $x = 1$.

1. Get the tangent line.

Point: $(1, f(1)) = (1, 0)$

slope: $f'(1) = 6$

$$f'(x) = \frac{6x}{3x^2 - 2} \implies 0$$

Equation: $y = (6(x - 1))$
 $y = (6x - 6)$

2. Get y -intercept. $(0, -6)$





