

**Homework** is posted.

**Poppers started Monday!!**

**You must have the correct popper form.**

**Finish Quiz 2 and Start Quiz 3 asap.**

**Test 2 registration starts at 12:01am Thursday.**

# Math 1432 - 13209

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## Read the **Syllabus**

Use the **Discussion Board on CourseWare** to get and give help.

Lecture notes/videos, additional help material, course announcements, homework and EMCFs will be posted in the calendar below. **Note:** Practice Tests count the same as online quizzes.

### Course Calendar

Sunday	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday
<b>January 13</b> <b>Note:</b> Practice Test 1 counts the same as an online quiz. Exam 1 counts as a major exam.	<b>14</b> <b>Notes</b> <b>Exam 1, PT1 and all Online Quizzes are open</b>	<b>15</b> <b>UH events this week</b> <b>Examples from 7.1 that will help with EMCF01</b>	<b>16</b> <b>Notes: pg, 4per</b> <b>Vid notes: pg, 4per</b> <b>Video</b> <b>Homework 1 posted</b>	<b>17</b> <b>EMCF01 due at 9am</b> <b>Note:</b> Use a graphing calculator to solve a complicated equation.	<b>18</b> <b>Notes: pg, 2per</b> <b>Vid notes: pg, 2per</b> <b>Video</b> <b>Quiz in lab/workshop</b>	<b>19</b> <b>EMCF02 due at 9am</b>
<b>20</b>	<b>21</b> <b>MLK Day</b> <b>No Class</b>	<b>22</b> <b>UH events this week</b> <b>Last day to add</b>	<b>23</b> <b>Notes, video notes, video</b> <b>EMCF03 due at 9am</b> <b>Homework 1 due in lab/workshop</b> <b>Homework 2 posted</b>	<b>24</b> <b>Exam 1 and PT1 close</b>	<b>25</b> <b>EMCF04 due at 9am</b> <b>Notes, video notes, video</b> <b>Quiz in lab/workshop</b>	<b>26</b> <b>Quiz 1 closes (7.1-7.2)</b>
<b>27</b> <b>Free Access ends today!! Purchase your Access Code!!</b>	<b>28</b> <b>EMCF05 due at 9am</b> <b>Notes – page, 4-per</b> <b>video notes, video</b> <b>Homework 2 due in lab/workshop</b>	<b>29</b> <b>UH events this week</b>	<b>30</b> <b>EMCF06 due at 9am</b> <b>Blank slides: page, 4-per</b> <b>Homework 3 posted</b> <b>Last day to drop without receiving a W</b>	<b>31</b> <b>Register on CourseWare for Exam 2</b>	<b>February 1</b> <b>EMCF07 due at 9am</b> <b>Quiz in lab/workshop</b>	<b>2</b> <b>Quiz 2 closes (7.3-7.5)</b> <b>Help with selected problems in 7.7 and 7.8.</b>



Please tell you high school friends  
and former teachers about our  
**High School Mathematics Contest**

**February 9th**  
**University of Houston**

**<http://mathcontest.uh.edu>**

*Free*

**Review:** What is the solution to  $y' = ky$ ?

$$y = \underline{C} e^{kt}$$

$\swarrow$  constant

$\nwarrow$   $y(0)$

Give the solution to  $u'(t) + 3u(t) = 0, u(0) = 2.$

diff.  
eq.

initial  
data

initial value  
problem

$$u'(t) = -3u(t)$$

$$u(t) = C e^{-3t}$$

$$2 = C$$

$$\Rightarrow u(t) = 2e^{-3t}$$

# Popper P02

Popper  
Spring 2013  
Math 1432 13209



2012-2-13596-1-2-1

Use a No. 2 Pencil. Do Not Write Outside of This Box.

1

2

3

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9

10

11

your  
ID  
#

Last Name \_\_\_\_\_  
First Name \_\_\_\_\_

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## Popper P02

1. Find the solution to the initial value problem  $y' + 2y = 0$ ,  $y(0) = 15$ .  
Give the value of  $y(1)$ .

$$2. \int_0^1 2^{3x} dx = \frac{1}{3 \ln(2)} 2^{3x} \Big|_0^1 = \frac{1}{3 \ln(2)} [8 - 1] = \frac{7}{3 \ln(2)}$$

3. Give the slope of the tangent line to  $f(x) = \arctan(2x)$  at  $x = 1$ .

## Recall:

Chain Rule Derivative Formulas

$$\frac{d}{dx} \arcsin(u) = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$$

$$\frac{d}{dx} \arctan(u) = \frac{1}{1+u^2} \frac{du}{dx}$$

Consequences

$$\int \frac{1}{\sqrt{1-u^2}} du = \arcsin(u) + C$$

$$\int \frac{1}{1+u^2} du = \arctan(u) + C$$

## Aside on inverse trig integration formulas...

Assume  $a > 0$ .

$$\int \frac{1}{a^2 + u^2} du = \int \frac{1}{a^2 \left(1 + \frac{u^2}{a^2}\right)} du = \frac{1}{a^2} \int \frac{1}{1 + \left(\frac{u}{a}\right)^2} du$$

"looks like"  $\int \frac{1}{1+u^2} du$

$$w = \frac{u}{a}$$
$$dw = \frac{1}{a} du$$
$$= \frac{1}{a} \arctan\left(\frac{u}{a}\right) + C$$

$$\int \frac{1}{\sqrt{a^2 - u^2}} du = \text{similar}$$
$$= \arcsin\left(\frac{u}{a}\right) + C$$



## Examples:

$$\int \frac{1}{4+x^2} dx = \int \frac{1}{2^2+x^2} dx = \frac{1}{2} \arctan\left(\frac{x}{2}\right) + C$$

$$\int \frac{\cos(x)}{\sqrt{3-\sin^2(x)}} dx = \int \frac{1}{\sqrt{3-u^2}} du$$

$$u = \sin(x)$$

$$du = \cos(x) dx$$

$$= \int \frac{1}{\sqrt{(\sqrt{3})^2 - u^2}} du$$

$$= \arcsin\left(\frac{u}{\sqrt{3}}\right) + C$$

$$= \arcsin\left(\frac{\sin(x)}{\sqrt{3}}\right) + C$$

New

## Hyperbolic Functions

Definitions

$$\cosh(x) = \frac{e^x + e^{-x}}{2}$$

"hyperbolic cosine"

$$\sinh(x) = \frac{e^x - e^{-x}}{2}$$

"hyperbolic sine"

$$\tanh(x) = \frac{\sinh(x)}{\cosh(x)} \quad \coth(x) = \frac{\cosh(x)}{\sinh(x)}$$

$$\operatorname{sech}(x) = \frac{1}{\cosh(x)} \quad \operatorname{csch}(x) = \frac{1}{\sinh(x)}$$

$\cosh(x)$  = hyperbolic cosine of  $x$

$\sinh(x)$  = hyperbolic sine of  $x$

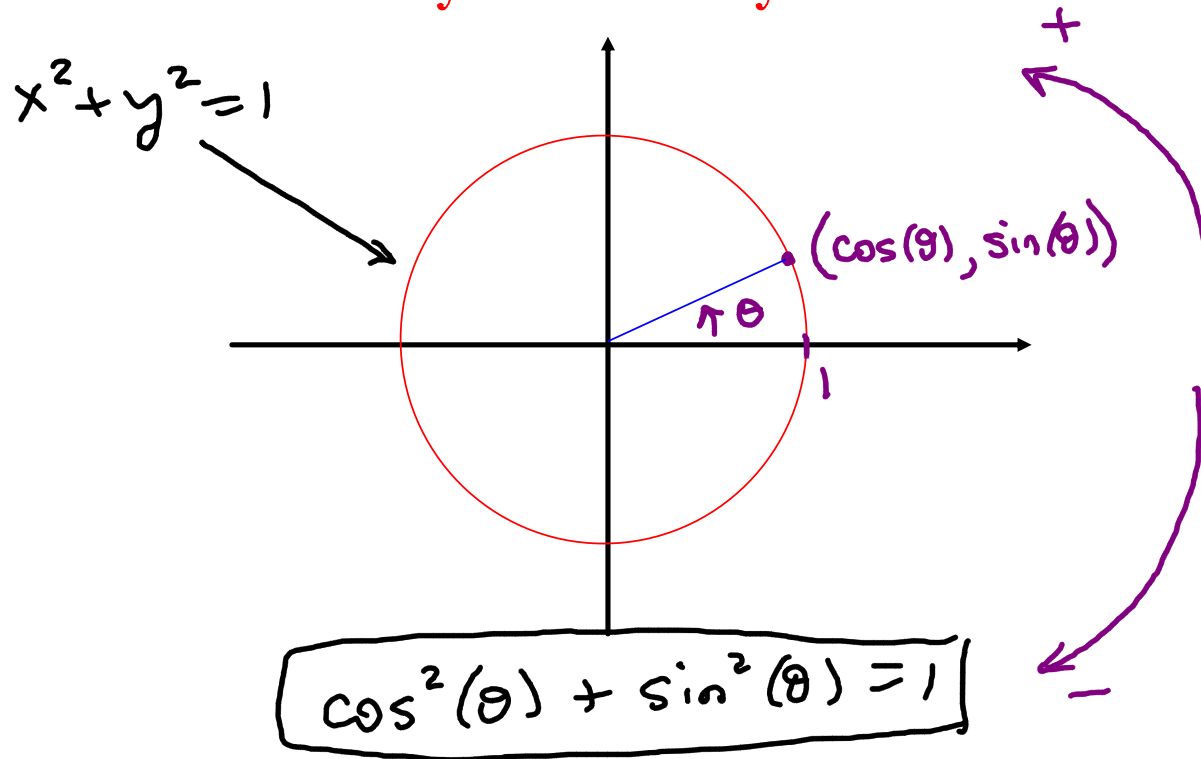
$\tanh(x)$  = hyperbolic tangent of  $x$      $\coth(x)$  = hyperbolic cotangent of  $x$

$\operatorname{sech}(x)$  = hyperbolic secant of  $x$      $\operatorname{csch}(x)$  = hyperbolic cosecant of  $x$

**Where do these names come from?**

First, recall that sine and cosine are called circular functions.

Do you recall why?



**Now let's do some computations  
with cosh and sinh.**

$$\cosh^2(t) = \left[ \frac{1}{2} (e^t + e^{-t}) \right]^2 = \frac{1}{4} (e^{2t} + 2 + e^{-2t})$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$\sinh^2(t) = \left[ \frac{1}{2} (e^t - e^{-t}) \right]^2 = \frac{1}{4} (e^{2t} - 2 + e^{-2t})$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$\cosh^2(t) - \sinh^2(t) = \frac{2}{4} - \frac{-2}{4} = 1$$

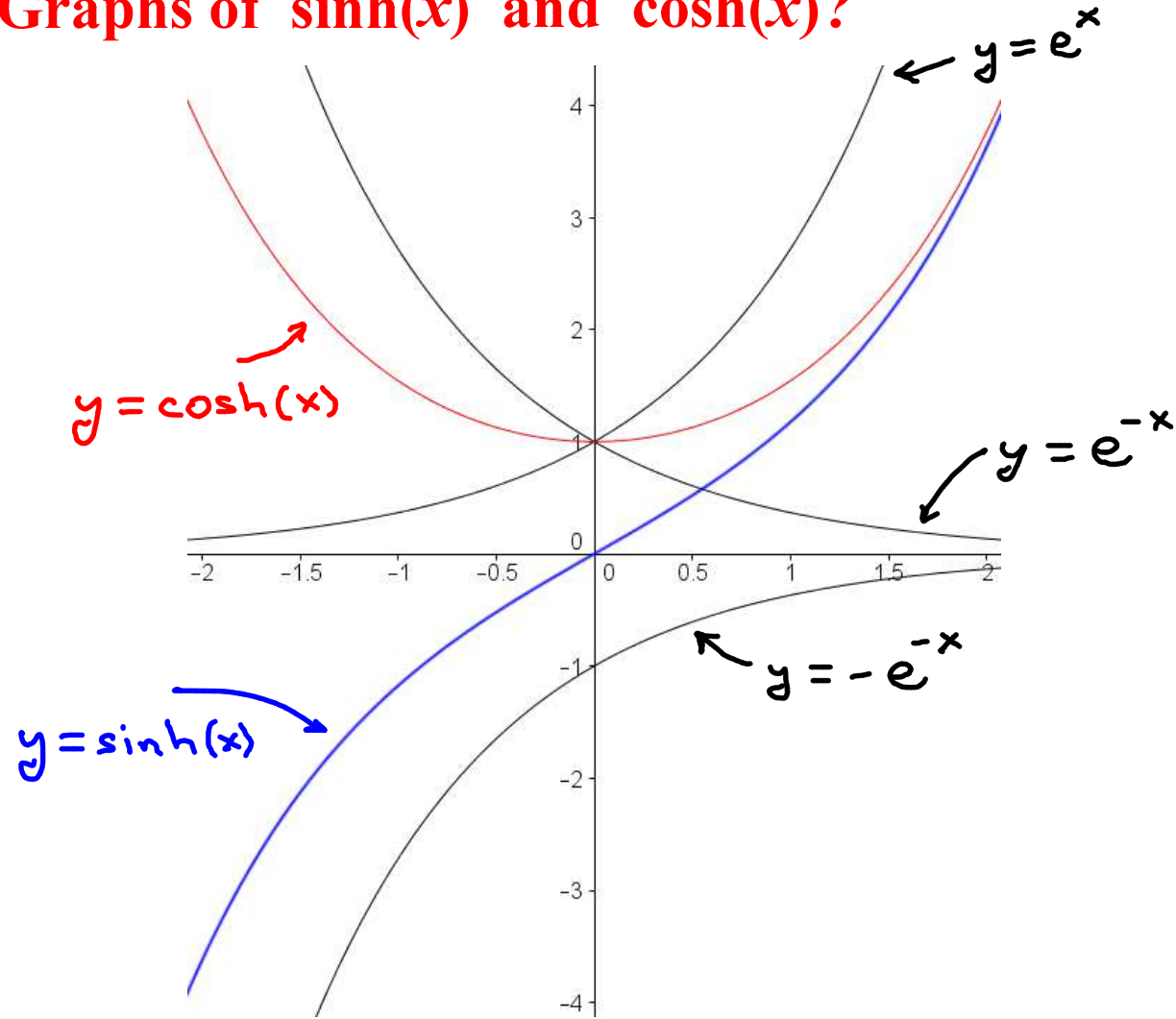
## Hyperbolic Identity

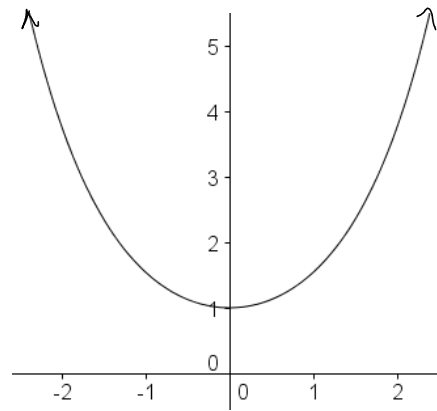
$$\cosh^2(t) - \sinh^2(t) = 1$$

$$x = \cosh(t) \quad , \quad y = \sinh(t)$$

$$x^2 - y^2 = 1$$

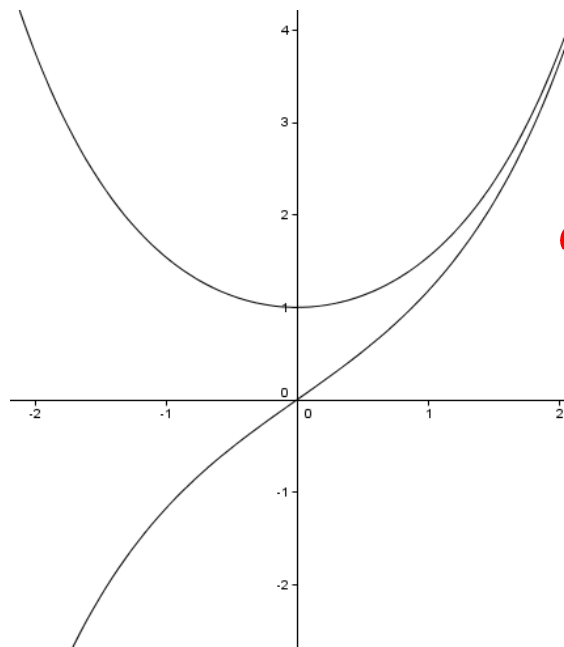
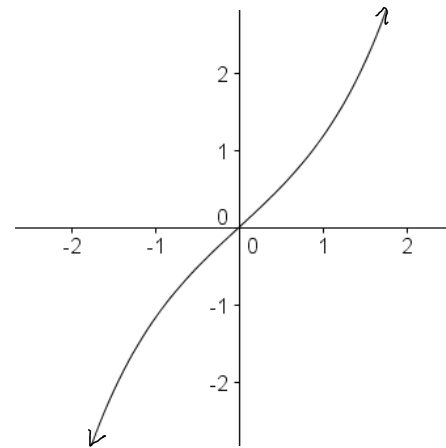
## Graphs of $\sinh(x)$ and $\cosh(x)$ ?





$$y = \cosh(x)$$

$$y = \sinh(x)$$



**Graphed together!!**



## Derivatives

$$\begin{aligned}\frac{d}{dx} \cosh(x) &= \frac{d}{dx} \left( \frac{1}{2} e^x + \frac{1}{2} e^{-x} \right) = \frac{1}{2} e^x - \frac{1}{2} e^{-x} \\ &= \sinh(x)\end{aligned}$$

$$\begin{aligned}\frac{d}{dx} \sinh(x) &= \frac{d}{dx} \left( \frac{1}{2} e^x - \frac{1}{2} e^{-x} \right) = \frac{1}{2} e^x + \frac{1}{2} e^{-x} \\ &= \cosh(x)\end{aligned}$$

## Chain Rule Formula and Consequences

$$\frac{d}{dx} \cosh(u) = \sinh(u) \frac{du}{dx} \quad \left| \quad \int \cosh(u) du = \sinh(u) + C \right.$$

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$$\frac{d}{dx} \sinh(u) = \cosh(u) \frac{du}{dx} \quad \left| \quad \int \sinh(u) du = \cosh(u) + C \right.$$

**Learn the derivative formulas  
for tanh, coth, sech and csch!!**

**Example:** Compute  $\frac{d}{dx} \cosh(\underbrace{\ln(\exp(x) + 2x)}_u)$

$$= \sinh(u) \boxed{\frac{du}{dx}}$$

$$= \sinh(\ln(e^x + 2x)) \cdot \frac{1}{e^x + 2x} \cdot (e^x + 2)$$

## Popper P02

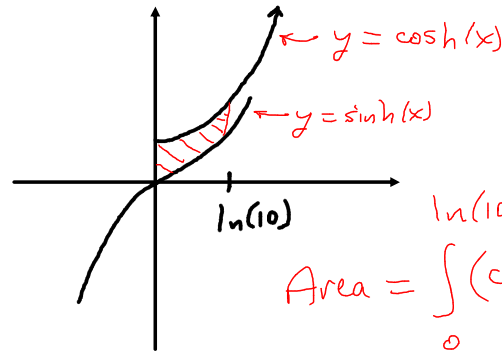
4. Give the slope of the tangent line to  $f(x) = \cosh(2x) + \sinh(-3x)$  at  $x = 0$ .

4.

5. The answer is  $1/2$ .

6. The answer is  $-13/7$ .

**Example:** Find the area bounded by the graphs of  $f(x) = \cosh(x)$  and  $g(x) = \sinh(x)$  for  $0 \leq x \leq \ln(10)$ .



$$\text{Area} = \int_0^{\ln(10)} (\cosh(x) - \sinh(x)) dx$$

$$= (\sinh(x) - \cosh(x)) \Big|_0^{\ln(10)}$$

$$= -e^{-x} \Big|_0^{\ln(10)}$$

$$= -\left(e^{-\ln(10)} - e^0\right)$$

$$= -e^{\ln\left(\frac{1}{10}\right)} + 1$$

$$= -\frac{1}{10} + 1 = \frac{9}{10}.$$

$$\sinh(x) = \frac{1}{2}e^x - \frac{1}{2}e^{-x}$$

$$\cosh(x) = \frac{1}{2}e^x + \frac{1}{2}e^{-x}$$