### Test 2 Review

- Inverse functions
- Logarithmic functions
- Exponential functions
- Logarithmic differentiation
- Exponential growth and decay (word problems)
- Inverse trig functions
- Hyperbolic functions
- Integration by parts
- Integration of powers and products of trig functions

Addition Problems: See the homework, examples given in the class notes, questions from poppers, questions from EMCFs, questions in online quizzes, review problems and videos posted from the lectures page, and questions given on Friday quizzes.

Practice Tes+ 2

#### EMCF06

## Free Friday!!!

- 1. 23.46
- 2. 39.44

Example: Show that 
$$f(x) = x^3 + 4x$$
 is invertible, and give  $(f^{-1})'(5)$ .

$$f'(x) = 3 \times^2 + 4$$
 is always positive.

$$f = x + 7$$
 is invertible.

$$(f^{-1})'(5) = \frac{1}{f'(a)} = \frac{1}{f'(1)} = \frac{1}{7}$$

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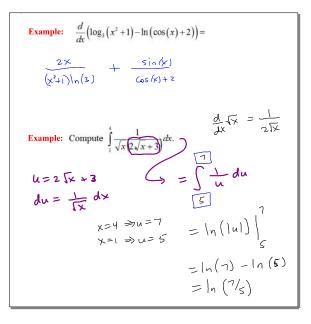
$$(f^{-1})'(7) = \frac{1}{7} = \frac{1}{7}$$

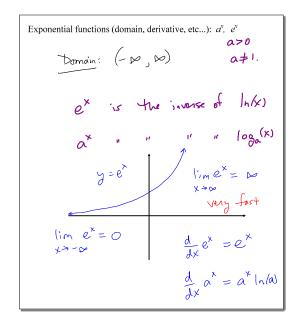
Logarithmic functions (domains, derivatives, etc...): 
$$\log_a(x)$$
,  $\ln(x)$ 

$$y = \ln(x)$$

$$\log_a(x) = \frac{\ln(x)}{\ln(a)}$$

$$\lim_{x \to \infty} \ln(x) = \infty$$





### EMCF06

## Free Friday!!!

- 3. 55555
- 4. 44444

**Example:** 
$$f(x) = 4^{x^2} - (\ln(x))^3$$
. Find  $f'(x)$ 

$$f'(x) = (2x) 4^{x^2} |_{n}(4) - 3(|_{n}(x))^2 \cdot \bot$$

Example: Compute 
$$\int \frac{3^{\tan(x)}}{\cos^2(x)} dx$$
. =  $\int 3^{\tan(x)} \sec^2(x) dx$   
 $u = \tan(x)$   
 $du = \sec^2(x) dx$  =  $\int 3^u du$   
=  $\frac{1}{\ln(3)} 3^u + C$   
=  $\frac{1}{\ln(3)} 3^{\tan(x)} + C$ 

**Example:** 
$$y = (2x+1)^{\sin(x)}$$
. Find  $\frac{dy}{dx}$ .

$$\ln(y) = \sin(x) \ln(2x+1)$$

$$\frac{1}{\sqrt{3}} \cdot \frac{dy}{dx} = \frac{\sin(x)}{2x+1} \cdot \frac{2}{2x+1} + \cos(x) \left[ \frac{2\sin(x)}{2x+1} + \cos(x) \left[ \frac{2\sin(x)}{2x+1} + \cos(x) \left[ \frac{2\cos(x)}{2x+1} + \cos(x) \right] \right] \right]}{\cos(x)}$$

$$\frac{dy}{dx} = (2 \times +1)^{\sin(x)} \left( \frac{2 \sin(x)}{2 \times +1} + \cos(x) \left| n(2 \times +1) \right| \right)$$

# Exponential growth and decay (word problems)

(A quantity changes at a rate proportional to the amount present)

Related to a special diff eq.

$$y' = ky.$$

$$\Rightarrow y = Ce^{kt}$$
The ind. Var.
Then kx
$$Ce^{x}$$

$$y(0)$$

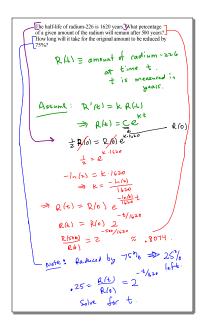
**Example:** A population *P* of insects increases at a rate proportional to the current population. Suppose there are 10,000 insects initially, and 20,000 insects one week later.

(a) Find an expression for the number of insects P(t) at any time t.

(b) How many insects will there be in 1 year? 2 years?

**Example:** The half-life of radium-226 is 1620 years. What percentage of a given amount of the radium will remain after 500 years? How long will it take for the original amount to be reduced by 75%?

**Example:** During the process of inversion, the amount *A* of raw sugar present decreases at a rate proportional to *A*. During the first 10 hours, 1000 pounds of raw sugar have been reduced to 800 pounds. How many pounds will remain after 10 more hours of inversion?



A population P of insects increases at a rate proportional to the current population. Suppose there are  $\frac{10,000 \text{ insects}}{10,000 \text{ insects}}$  initially, and  $\frac{20,000 \text{ insects}}{10,000 \text{ insects}}$  or week later.

(a) Find an expression for the number of insects P(t) at any time t.

(b) How many insects will there be in 1 year? 2 years? P'(t) = kP(t)  $\Rightarrow P(t) = kP(t)$   $\Rightarrow P(t) = 10000$   $\Rightarrow P(t) = 10000 \cdot 2$   $P(t) = 10000 \cdot 2$   $\Rightarrow P(t) = 10000 \cdot 2$   $\Rightarrow P(t) = 10000 \cdot 2$