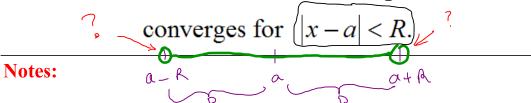
## Information

No Office Hours Today!! Later to day.

		)				
Note: Homework 13 is not due until the 29 <sup>th</sup> !! Please consider taking the time to complete this survey.	I 1	Marc 2 to Pagaire	EMCF39 due at 9am	25	26 EMCF40 due at 9am Quiz in lab/workshop	27 Quiz 13 closes (11.5-11.6) Test 4 starts
28	29 EMCF41 due at 9am Homework 13 due in lab/workshop Last day of class	30 Practice Test 4 Closes	May 1	9	10	4 Quiz 14 closes (11.7-11.8)
	Final Exam Starts					

A power series centered at 
$$a$$
 has the form
$$\sum_{k=0}^{\infty} b_k (x-a)^k + \int_{(k)}^{\infty} \int_{(k)}^{\infty} \int_{(k)}^{(k)} \int_{(k)}^{\infty} \int_{(k)}^{(k)} \int_{(k)$$

the largest value of R so that the power series



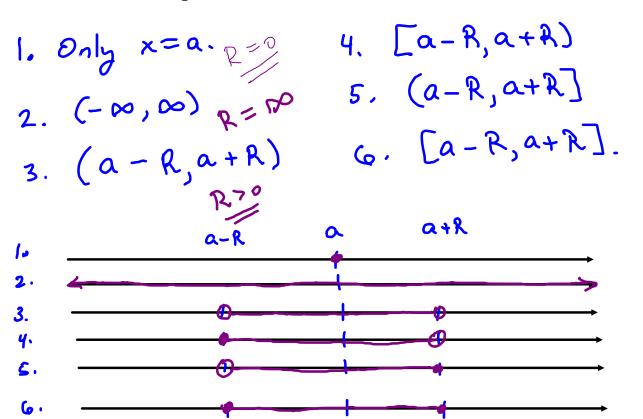
- 1. Absolute convergence determines the radius of convergence.
- 2. If a power series is equal to a function on an interval, then the power series is the Taylor series for the function.
- 3. Power series can be integrated and differentiated in the interior of their interval of convergence, and the power series, the derivative and the antiderivative all have the SAME radius of convergence.

The value(s) of x where

$$\sum_{k=0}^{\infty} b_k \left( x - a \right)^k$$

converges will be one of

Fact: Absolute converges determines the radius of convergence.



## **Example:** Determine the values of x where

 $\sum_{k=0}^{\infty} \frac{(-1)^k}{k+1} (x-1)^k \text{ converges,}$ and give the radius of converges.

and give the radius of convergence.

Get R. Abs. conv. determines the radius of conv.

$$\sum_{k=0}^{\infty} \left| \frac{(-1)^k}{(k+1)} (k-1)^k \right| = \sum_{k=0}^{\infty} \frac{|x-1|^k}{k+1}$$

$$\frac{|x-1|^{k+1}}{|x-1|^{k+1}} = \lim_{k \to \infty} \frac{|x-1|^{k}}{|x-1|^{k}} = \lim_{k \to \infty} \frac{|x-1|^{k}}{|x-1|^{k+1}}$$

Conv. for |x-1| < 1A convergence is

X?

(-1)\*

Y=0: Substitute k=0 into  $\sum_{k=0}^{\infty} \frac{(-1)^k}{k+1} (x-1)^k$ 

$$\sum_{k=0}^{K=0} \frac{(-1)_{k}}{(-1)_{k}} = \sum_{k=0}^{K=0} \frac{(-1)_{k}}{1}$$

Diverges by CT with

 $\chi=2$ : Substitute  $\chi=2$  into  $\sum_{k=0}^{\infty}\frac{(-1)^k}{k+1}(x-1)^k$ .

$$\sum_{k=0}^{\infty} \frac{(-1)^k}{(-1)^k} = \sum_{k=0}^{\infty} (-1)^k \cdot \frac{1}{k+1}$$

Alternating series: Note - 0 1 20

(0,2]

ie. for 0 < x ≤ 2

**Important Fact:** If a power series centered at x = a has a radius of convergence R > 0, then the power series can be differentiated and integrated on (a - R, a + R), and the new series will converge on (a - R, a + R), and maybe at the endpoints.

Popper 31

2. 76

**Example:** Find the interval and radius of convergence for  $f(x) = \sum_{n=0}^{\infty} \frac{x^n}{n^2 + 1}$ . Then give the antiderivative  $F(x) \text{ of this power senes } \dots$ and find f'(x). Finally, give the radius and interval of convergence for each of F(x) and f'(x).

Aside: What is  $f^{(12)}(0)$ ?  $Coef in finite of x^{(12)}(0)$   $F(x) \text{ of this power senes } \dots$   $F(x) \text{$ Ratio Test Summary:  $\sum_{n=0}^{\infty} \frac{x^n}{n^2 + 1}$  has radius of com. 5-1,13.

$$f(x) = \sum_{n=0}^{\infty} \frac{x^n}{n^2 + 1} = \sum_{n=0}^{\infty} \frac{1}{n^2 + 1} \times n$$
Find  $F(x)$  so that  $F'(x) = f(x)$ 

and  $F(0) = 2$ 

$$f(x) = \sum_{n=0}^{\infty} \frac{1}{n^2 + 1} \times n + 1 + C$$

$$F(x) = \sum_{n=0}^{\infty} \frac{1}{(n^2 + 1)(n + 1)} + C$$

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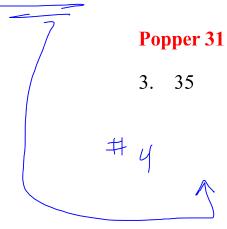
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See the video and video notes for the remainder of this problem.

**Example:** Let 
$$f(x) = \sum_{n=0}^{\infty} \frac{x^n}{n^2 + 1}$$
. Give  $f^{(9)}(0)$ .



**Example:** Give the Taylor series centered at 0 for  $\frac{1}{1-x}$ ,  $\frac{1}{1+x}$ ,  $\ln(1+x)$ ,  $\ln(1+x^3)$ , and  $x^2 \ln(1+x^3)$ . In each case, give the radius of convergence.

## **Next Time**