

**Info...**

3 hrs

**Final Exam Review Problems  
Are Posted**

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**Take time to submit your teacher  
evaluation on *CourseWare*.**

21	22	23	24	25	26	27
Note: Homework 13 is not due until the 29 <sup>th</sup> !! Please consider taking the time to complete this survey.	EMCF38 due at 9am Blank Slides: page, 4-per, video notes, video	Complete the Online Teacher Evaluation by May 3 to Receive 5 Bonus Points	EMCF39 due at 9am Notes: page, 4-per	Final Exam Review Video (3 hours) Notes	EMCF40 due at 9am Notes: page, 4-per (in-class partial review for test 4) The 3 hour Video Review posted on the 20 <sup>th</sup> works through all of these problems, and more. Quiz in lab/workshop	Quiz 13 closes (11.5-11.6) Test 4 starts
28	29	30	May 1	2	3	4
	EMCF41 due at 9am – All answers are C. Blank Slides: page, 4-per Homework 13 due in lab/workshop Last day of class	Practice Test 4 Closes	Final Exam Review Video (3 hours) Notes	Complete the Online Teacher Evaluation by May 3 to Receive 5 Bonus Points	There are 20 questions on the final exam. More than half of them will be written.  Good Luck!!!	Quiz 14 closes (11.7-11.8)
5	6	7	8	9	10	11
	Final Exam Starts		Practice Final Exam Closes			

Consider giving something back!



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Give the interval of convergence and radius of convergence

for the power series  $\sum_{n=1}^{\infty} \frac{(x+1)^n}{2^n (n+1)}$ . *Centered at -1.*

To get the radius of convergence, check

ABS conv. ;  $\sum_{n=1}^{\infty} \left| \frac{(x+1)^n}{2^n (n+1)} \right|$

$$= \sum_{n=1}^{\infty} \frac{|x+1|^n}{2^n (n+1)}$$

$$= \sum_{n=1}^{\infty} \left( \frac{|x+1|}{2} \right)^n \cdot \frac{1}{(n+1)}$$

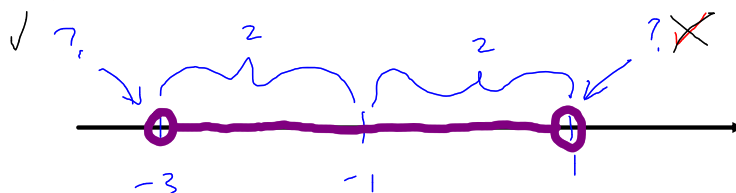
root ;  $\lim_{n \rightarrow \infty} \left( \frac{|x+1|^n}{2^n (n+1)} \right)^{1/n}$

$$= \lim_{n \rightarrow \infty} \frac{|x+1|}{2} \cdot \frac{1}{(n+1)^{1/n}} = \frac{|x+1|}{2}$$

Thought: Probably  
 $\frac{|x+1|}{2} < 1$   
 $|x+1| < 2$

∴ the root test implies we have abs. conv. for  $\frac{|x+1|}{2} < 1$

i.e.  $|x+1| < 2$ . Radius of conv is 2.



$x = -3$ : Subst  $x = -3$  into the original series

$$\sum_{n=1}^{\infty} \frac{(-3+1)^n}{2^n (n+1)} = \sum_{n=1}^{\infty} \frac{(-1)^n}{n+1}$$

Conv. alt. series.  
(Do it)

$x = 1$ : Subst  $x = 1$  into the original series.

$$\sum_{n=1}^{\infty} \frac{(1+1)^n}{2^n (n+1)} = \sum_{n=1}^{\infty} \frac{1}{n+1}$$

Diverges by LCT  
with  $\sum \frac{1}{n}$ .

∴ The radius of conv. is 2 and  
the interval of conv. is

$$\underline{\underline{[-3, 1)}}.$$

Let  $f(x) = \sum_{n=1}^{\infty} \frac{(x+1)^n}{2^n(n+1)}$ . Give the value for  $f^{(6)}(-1)$ .

T.S. for  $f(x)$  centered at -1.

$$\begin{aligned} \rightarrow f(-1) + f'(-1)(x+1) + \frac{f''(-1)}{2}(x+1)^2 + \frac{f'''(-1)}{6}(x+1)^3 \\ + \dots + \frac{f^{(6)}(-1)}{6!}(x+1)^6 + \dots \end{aligned}$$

From above,  $\frac{1}{2^6(6+1)} = \frac{f^{(6)}(-1)}{6!}$

$$\Rightarrow f^{(6)}(-1) = \frac{6!}{2^6 \cdot 7}$$

## Popper 33

Give the radius of convergence for each power series. If your answer is  $\infty$ , then input 999.

This is a popper grade, and in addition, the score will replace your lowest popper grade.

1

1.  $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} x^n}{n}$

1/3

2.  $\sum_{n=1}^{\infty} 3^{n+1} x^n$

1/2

3.  $\sum_{n=1}^{\infty} \frac{2^n}{n^2 + 1} x^n$

1

4.  $\sum_{n=1}^{\infty} \frac{(-1)^n}{n^2 + 1} x^n$

1/2

5.  $\sum_{n=1}^{\infty} \frac{(-2)^n}{n^2 + 1} x^n$

6.  $\sum_{n=0}^{\infty} \frac{x^n}{2n+1}$  1

7.  $\sum_{n=0}^{\infty} \frac{x^n}{2^n + 1}$  2

8.  $\sum_{n=0}^{\infty} \frac{x^n}{n!} = e^x$

$\infty$

cos(x)

9.  $\sum_{n=0}^{\infty} \frac{(-1)^n x^{2n}}{(2n)!}$

$\infty$

sin(x)

10.  $\sum_{n=0}^{\infty} \frac{(-1)^n x^{2n+1}}{(2n+1)!}$

$\infty$