

Alternate 3

Directions: Answer the questions below. Then log into CourseWare at <http://www.casa.uh.edu> and submit your answers using the EMCF entitled **Alternate03**.

1. A linear second-order differential equation of the form $y'' + py' + qy = f$ is said to be homogeneous if and only if $f = 0$.
 - a. True
 - b. False
2. The term f in a linear second-order differential equation of the form $y'' + py' + qy = f$ is called a forcing term.
 - a. True
 - b. False
3. The Wronskian of two solutions of $y'' + py' + qy = f$ is always nonzero.
 - a. True
 - b. False
4. If f , q and p are continuous functions, and b , m and x_0 are real numbers, then the initial value problem $y'' + py' + qy = f$, $y(x_0) = b$, $y'(x_0) = m$ has a unique solution.
 - a. True
 - b. False
5. If f , q and p are continuous functions, then the initial value problem $y'' + py' + qy = f$ always has two linearly independent solutions.
 - a. True
 - b. False
6. The reduced form of the linear second-order differential equation $y'' + py' + qy = f$ is $y'' + py' + qy = 0$.
 - a. True
 - b. False
7. If y_1 and y_2 are any pair of solutions to $y'' + py' + qy = 0$ then the general solution has the form $y = c_1y_1 + c_2y_2$ where c_1 and c_2 are arbitrary constants.
 - a. True
 - b. False

8. The Wronskian of $\cos(x)$ and $-\sin(x)$ is -1.
- True
 - False
9. The Wronskian of any 2 solutions to $y'' + 2y' + \sin(x)y = 0$ has to have the form Ce^{-2x} for some constant C .
- True
 - False
10. The Wronskian of any 2 solutions to $y'' + \cos(x)y' + \sin(x)y = 0$ has to have the form $Ce^{\sin(x)}$ for some constant C .
- True
 - False
11. The key to finding solutions to $y'' + ay' + by = 0$ where a and b are constants is to look for roots of the characteristic polynomial.
- True
 - False
12. Suppose a and b are constants. The characteristic equation for $y'' + ay' + by = 0$ is $r^2 + ar + b = 0$.
- True
 - False
13. Suppose a and b are constants. If the characteristic equation for $y'' + ay' + by = 0$ is $(r - r_1)(r - r_2) = 0$ for some distinct real numbers r_1 and r_2 , then the general solution always has the form $y = c_1e^{r_1x} + c_2e^{r_2x}$ for some constants c_1 and c_2 .
- True
 - False
14. Suppose a and b are constants. The general solution to $y'' + ay' + by = 0$ has different forms depending upon whether the characteristic equation has distinct real roots, a repeated real root, or complex roots.
- True
 - False
15. The general solution to $y'' + py' + qy = f$ has the form $y = c_1y_1 + c_2y_2 + z$ where y_1 and y_2 are linearly independent solutions to the reduced equation, c_1 and c_2 are arbitrary constants, and z is a particular solution to $y'' + py' + qy = f$.
- True
 - False
16. If f , q and p are continuous functions, then *variation of parameters* can always be used to find a particular solution to $y'' + py' + qy = f$.
- True
 - False

17. A fundamental set of solutions to $y'' + py' + qy = 0$ is given by any pair of solutions to the differential equation.
- True
 - False
18. If a and b are real numbers, then the method of undetermined coefficients can always be used to find a particular solution to $y'' + ay' + by = f$.
- True
 - False
19. Suppose q and p are continuous functions. The method of *reduction of order* can be used to find a second linearly independent solution to $y'' + py' + qy = 0$ provided one nontrivial solution is known.
- True
 - False
20. There will be at least one problem on the midterm exam that asks students to use reduction of order.
- True
 - False