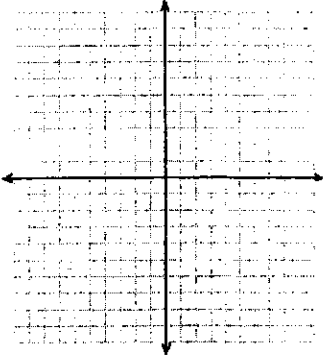
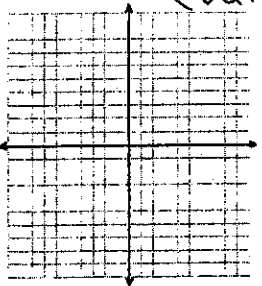


Stuff You Must Know Cold – Algebra 1

<p>Powers</p> $13^2 = 169$ $14^2 = 196$ $15^2 = 225$ $16^2 = 256$ $17^2 = 289$ $18^2 = 324$ $19^2 = 361$ $20^2 = 400$ $21^2 = 441$ $22^2 = 484$ $23^2 = 529$ $24^2 = 576$ $25^2 = 625$ $2^3 = 8$ $3^3 = 27$ $4^3 = 64$ $5^3 = 125$ $6^3 = 216$ $7^3 = 343$ $8^3 = 512$ $9^3 = 729$ $10^3 = 1000$ $11^3 = 1331$ $12^3 = 1728$ $2^4 = 16$ $3^4 = 81$ $4^4 = 256$ $5^4 = 625$ $6^4 = 1296$ $7^4 = 2401$ $8^4 = 4096$ $9^4 = 6561$ $10^4 = 10,000$	<p>Powers</p> $2^5 = 32$ $3^5 = 243$ $4^5 = 1024$ $5^5 = 3125$ $2^6 = 64$ $2^7 = 128$ $2^8 = 256$ $2^9 = 512$ $2^{10} = 1024$ $2^{11} = 2048$ $2^{12} = 4096$	<p>Quadratic Equations</p> <p>Parent Function: $y = x^2$</p> <p>Standard Form: $y = a(x-h)^2 + k$</p> <p>Intercept Form: $y = a(x-p)(x-q)$</p> <p>Vertex: (h, k)</p> <p>Axis of Symmetry: $x = \frac{-b}{2a}$</p> <p>Quadratic Formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$</p> <p>Graph $y =$ (varies)</p> 
	<p>Factorials</p> $1! = 1$ $2! = 2$ $3! = 6$ $4! = 24$ $5! = 120$ $6! = 720$ $7! = 5040$	<p>Inequality Meanings</p> $<$ less than \leq less than or equal to $>$ greater than \geq greater than or equal to
	<p>Linear Equations</p> <p>Parent Function: $y = x$</p> <p>Standard Form: $ax + by = c$</p> <p>Slope-Intercept Form: $y = mx + b$</p> <p>Point-Slope Form: $y - y_1 = m(x - x_1)$</p> <p>Slope: $\frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x} = \frac{\text{rise}}{\text{run}}$</p> <p>Graph $y =$ (varies)</p> 	<p>Three ways to solve a system of equations</p> <ol style="list-style-type: none"> 1. Graphing 2. Substitution 3. Elimination

Stuff You Must Know Cold - Algebra 1

<p>Order of Operations</p> <ol style="list-style-type: none"> 1. () 2. Exponents 3. Multiplication / Division L → R 4. Addition / Subtraction L → R 	<p>Properties (use a, b, c)</p> <p>Commutative Addition: $a + b = b + c$</p> <p>Multiplication: $a \cdot b = b \cdot c$</p> <p>Associative Addition: $a + (b + c) = (a + b) + c$</p> <p>Multiplication: $a \cdot (b \cdot c) = (a \cdot b) \cdot c$</p> <p>Distributive: Addition $a \cdot (b + c) = ab + ac$</p>	<p>Distance Formula</p> $d = \sqrt{(\Delta x)^2 + (\Delta y)^2}$ <p>Midpoint Formula</p> $(m_1, m_2) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$
<p>Absolute Value $a \geq 0$</p> <p>$a = a$</p> <p>$-a = a$</p>	<p>Measures of Central Tendency</p> <p>Mean: arithmetic mean or average</p> <p>Median: the middle number when a set of numbers are put in order</p> <p>Mode: the number that occurs the most often in a list</p> <p>Range: the difference between the largest and smallest numbers</p>	<p>Parallel and Perpendicular Lines</p> <p>If $y = mx + b$</p> <p>Parallel line slope: $m_1 = m_2$</p> <p>Perpendicular line slope:</p> $m_1 = -\frac{1}{m_2}$
<p>Function Definitions</p> <p>Domain: the set of all possible input values (usually x)</p> <p>Range: the set of all possible output values (usually y)</p> <p>Function: the relation for which each element of the domain corresponds to exactly one element of the range</p> <p>Direct Variation: a relationship between two variables in which one is a constant multiple of the other $y = kx$</p> <p>Indirect Variation: a relationship between two variables in which the product is a constant $y = \frac{k}{x}$</p> <p>Roots: A number at which a polynomial has the value zero; where the graph crosses the x-axis</p>		<p>Dimensional Analysis ($^{\circ}C \Leftrightarrow ^{\circ}F$, in \Leftrightarrow cm, ft \Leftrightarrow mi, etc.)</p> <p>Convert (varies)</p>

Stuff You Must Know Cold - Geometry

Area Formulas:

Square: s^2

Rectangle: $l \cdot w$

Parallelogram: $b \cdot h$

Trapezoid: $\frac{1}{2}(b_1 + b_2)h$

Circle: πr^2

Right Triangle: $\frac{1}{2}bh$

Any Triangle (Heron's Formula):

$$\sqrt{s(s-a)(s-b)(s-c)}$$

Equilateral Triangle:

$$\frac{s^2\sqrt{3}}{4}$$

Regular Polygon:

$$\frac{1}{2}ap$$



Surface Area Formulas:

Cube: $6s^2$

Sphere: $4\pi r^2$

Cylinder: $2\pi r^2 + 2\pi rh$

Angles:

is an acute angle

is an obtuse angle

Complementary angles add up to 90°

Supplementary angles add up to 180°

Volume Formulas:

Cube: s^3

Prism: $B \cdot h$

Cylinder: $\pi r^2 \cdot h$

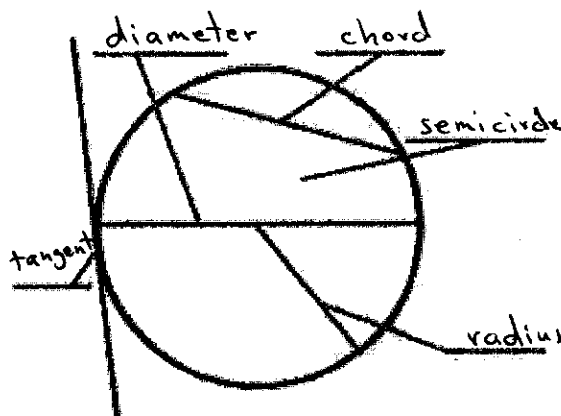
Pyramid: $\frac{1}{3}B \cdot h$

Cone: $\frac{1}{3}\pi r^2 \cdot h$

Sphere: $\frac{4}{3}\pi r^3$

Volume is measured in cubic units

Parts of a Circle:



Polygon Interior Angle Sums:

Triangle: 180°

Quadrilateral: 360°

Regular Polygon: $180^\circ(n-2)$

Arc and Sector

Arc Length: $s = \theta \cdot r$
↑
radians

Sector Area: $\frac{1}{2}r^2\theta$

Roots to Know:

$\sqrt{2} \approx 1.4$

$\sqrt{3} \approx 1.7$

Polygon Names:

Sides: Name:

3 triangle

4 quadrilateral

5 pentagon

6 hexagon

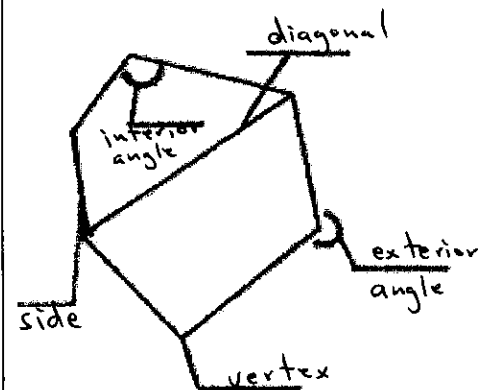
7 heptagon

8 octagon

9 nonagon

10 decagon

Polygon Parts:



Lines:

is a line segment

is a ray

= parallel lines

$Y = \frac{2}{3}x + 4$

Give a equation of a line
 Parallel: $y = \frac{2}{3}x + b$

Give a line Perpendicular:
 $y = -\frac{3}{2}x + b$

Stuff You Must Know Cold – Geometry

Pythagorean Theorem:

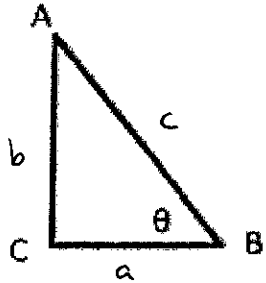
$$a^2 + b^2 = c^2$$

Trigonometry:

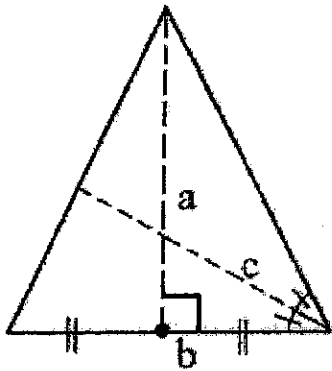
$$\sin \theta = \frac{b}{c}$$

$$\cos \theta = \frac{a}{c}$$

$$\tan \theta = \frac{b}{a}$$



Parts of a Triangle:



a: altitude or height

b: base

c: bisector

Similarity

Ratio of sides a:b

Ratio of perimeters a:b

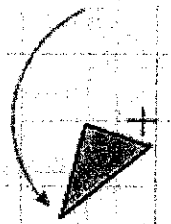
Ratio of areas $a^2 : b^2$

Ratio of volumes $a^3 : b^3$

Triangle Congruence:

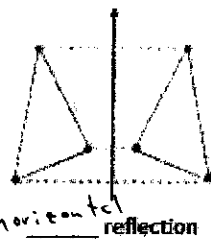
1. SSS
2. AAS
3. SAS
4. ASA
5. HL

Transformations
Translations:

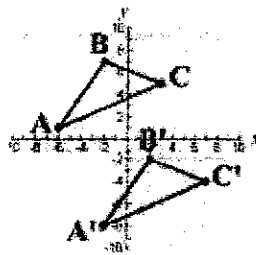
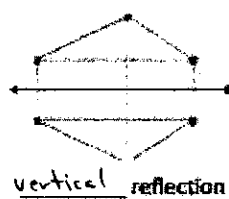


is a rotation

Line of Reflection



Line of Reflection



is a translation

Logic

Conditional Statement: (varies)
 $P \rightarrow Q$

Converse: $Q \rightarrow P$

Inverse: $\sim P \rightarrow \sim Q$

Contrapositive: $\sim Q \rightarrow \sim P$

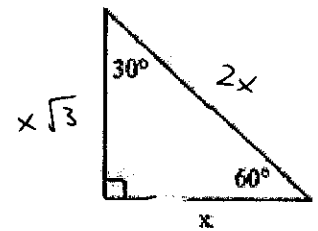
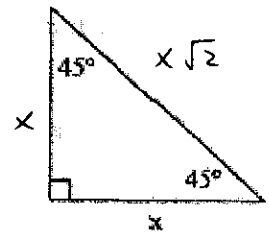
Perimeter Formulas:

Square: $4s$

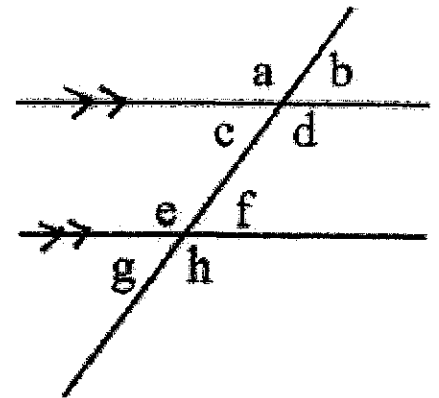
Rectangle: $2l + 2w$

Circumference of a Circle:
 $2\pi r$

Special Right Triangles:



Parallel Lines:



a is congruent to: d, e, h

a is supplementary to:
c, b, f, g

Name:

Date:

Number:

Stuff You Must Know Cold – Algebra II

Arithmetic Series

$$t_n = t_1 + d(n-1)$$

$$S_n = \frac{n}{2} (2t_1 + d)$$

$$= \frac{n}{2} (t_1 + t_n)$$

Geometric Series

$$t_n = t_1 r^{n-1}$$

$$S_n = \frac{t_1 (1 - r^n)}{1 - r}$$

$$S = \frac{t_1}{1 - r}$$

Probability and Statistics

$${}_n P_r = \frac{n!}{(n-r)!}$$

$${}_n C_r = \binom{n}{r} = \frac{n!}{(n-r)! (r!)}$$

Basic Counting Principle with m, n , and l different items =

$$m \cdot n \cdot l$$

Transformations ($a, b, h, k > 0$)

$$y = f(x) - k \text{ down } k \text{ units}$$

$$y = f(x - h) \text{ right } k \text{ units}$$

$$y = -f(x) \text{ reflect over } x\text{-axis}$$

$$y = f(-x) \text{ reflect over } y\text{-axis}$$

$$y = f^{-1}(x) \text{ inverse}$$

$$y = af(x) \text{ vertical expansion/compression}$$

$$y = f(bx) \text{ horizontal expansion/compression}$$

Fractions

$$\frac{0}{\#} = 0$$

$$\frac{0}{0} = \text{indeterminant}$$

$$\frac{\#}{0} = \text{undefined}$$

Conjugate

of $a + b$ is $a - b$

$$(a-b)(a+b) = a^2 - b^2$$

Horizontal Asymptote Rules:

$$y = \frac{ax^m + \dots}{bx^n + \dots}$$

$$1. m > n, \text{ no HA}$$

$$2. m < n, y = 0$$

$$3. m = n, y = \frac{a}{b}$$

Vertical Asymptote Rules:

- simplify
- set denominator = 0
- roots are VA

Imaginary Numbers:

$$\sqrt{-1} = i$$

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$

Arithmetic Operations

$$ab + ac = a(b+c)$$

$$\frac{a}{b} + \frac{c}{d} = \frac{ad+bc}{bd}$$

$$\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c}$$

$$\left(\frac{a}{b}\right) = \frac{ad}{bc}$$

$$\left(\frac{c}{d}\right) = \frac{ad}{bc}$$

$$\left(\frac{a}{b}\right) = \frac{a}{bc}$$

$$\frac{a}{a} = \frac{a \cdot c}{b}$$

$$\left(\frac{b}{c}\right) = \frac{ab}{c}$$

$$\frac{a}{1} \left(\frac{b}{c}\right) = \frac{ab}{c}$$

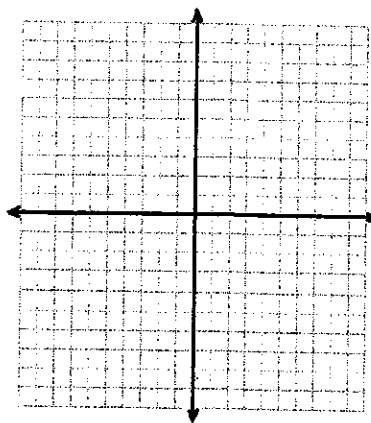
$$\frac{a-b}{c-d} = \frac{b-a}{d-c}$$

$$\frac{ab+ac}{a} = b+c$$

Parent Functions

Graph

$$y = (\text{varies})$$



Name:

Date:

Number:

Stuff You Must Know Cold – Algebra II

Exponents and Radicals

$$a^0 = 1, a \neq 0$$

$$(ab)^n = a^n b^n$$

$$a^x a^y = a^{x+y}$$

$$\sqrt{a} = a^{1/2}$$

$$\frac{a^x}{a^y} = a^{x-y}$$

$$\sqrt[n]{a} = a^{1/n}$$

$$\left(\frac{a}{b}\right)^x = \frac{a^x}{b^x}$$

$$\sqrt[n]{a^m} = a^{m/n}$$

$$a^{-x} = \frac{1}{a^x}$$

$$\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b}$$

$$(a^x)^y = a^{(x \cdot y)}$$

$$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$$

Interest/Half-Life

Compound Interest:

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

Continuously Compounded:

$$A = Pe^{rt}$$

Half-Life:

$$A_t = A_0 \left(\frac{1}{2}\right)^{\frac{t}{t_{1/2}}}$$

Logarithm Rules

Change from log to exponential

$$\log_b y = x$$

$$y = b^x$$

$$\ln y = x$$

$$y = e^x$$

$$\log y = x$$

$$y = 10^x$$

Change from exponential to log

$$b^x = y$$

$$x = \log_b y$$

More log rules

$$\log_a a = 1$$

$$\log_a 1 = 0$$

$$\log_a a^n = n \cdot \log_a a = \boxed{n}$$

$$\log_b(mn) = \log_b m + \log_b n$$

$$\log_b\left(\frac{m}{n}\right) = \log_b m - \log_b n$$

$$\log_b m^n = n \log_b m$$

Change of base formula

$$\log_c a = \frac{\log a}{\log c}$$

Intercepts

To find the x-intercept of any function:

set $y = 0$, solve for x

To find the y-intercept of any function:

set $x = 0$, solvefor y

Conics (standard forms)

Circle:

$$(x-h)^2 + (y-k)^2 = r^2$$

Parabola

Vertical:

$$(x-h)^2 = 4p(y-k)$$

Horizontal:

$$(y-k)^2 = 4p(x-h)$$

Ellipse

 $a > b$

Vertical:

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

Horizontal:

$$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$$

Hyperbola

Vertical:

$$-\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$$

Horizontal:

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

Complete the Square:

(varies)

Factoring

Difference of Squares

$$a^2 - b^2 = (a-b)(a+b)$$

Difference of Cubes

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

Sum of Cubes

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

Perfect Square Trinomial

$$a^2 - 2ab + b^2 = (a-b)^2$$

$$a^2 + 2ab + b^2 = (a+b)^2$$

Grouping

$$ac + ad + bc + bd =$$

$$a(c+d) + b(c+d) = (a+b)(c+d)$$

Name:

Date:

Number:

Stuff You Must Know Cold – Pre-Cal

Even – Odd Functions

If $f(x)$ is even, then
 $f(-x) = f(x)$

If $f(x)$ is odd, then
 $f(-x) = -f(x)$

Composite Functions

$f(x) =$ (varies)

$g(x) =$

$f(g(x)) =$

Triangles

Law of Cosines:

$$c^2 = a^2 + b^2 - 2ab \cos C$$

Law of Sines:

$$\frac{\sin A}{a} = \frac{\sin B}{b}$$

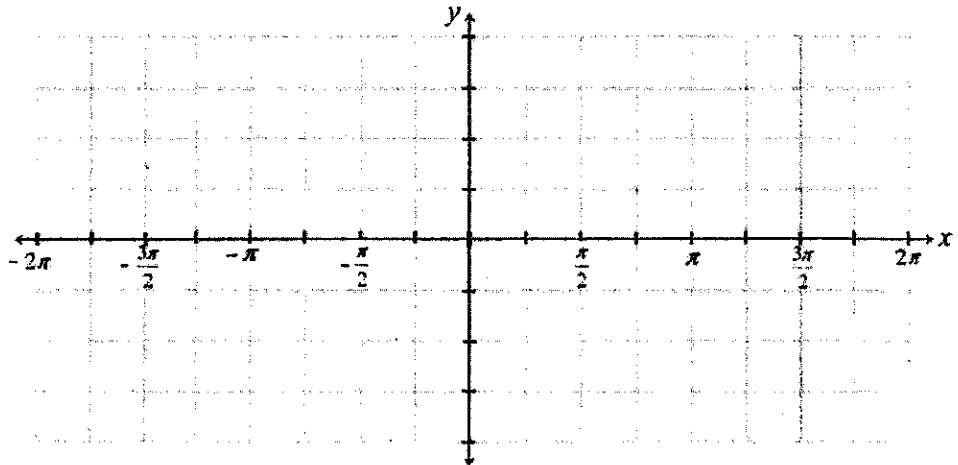
Values of Trigonometric Functions for Common Angles

θ	$\sin \theta$	$\cos \theta$	$\tan \theta$
0°	0	1	0
$\frac{\pi}{6}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	1
$\frac{\pi}{3}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$
$\frac{\pi}{2}$	1	0	und. ∞
π	0	-1	0

Know both the inverse trig and the trig values. E.g. $\tan^{-1}(1)$

Trig Graph

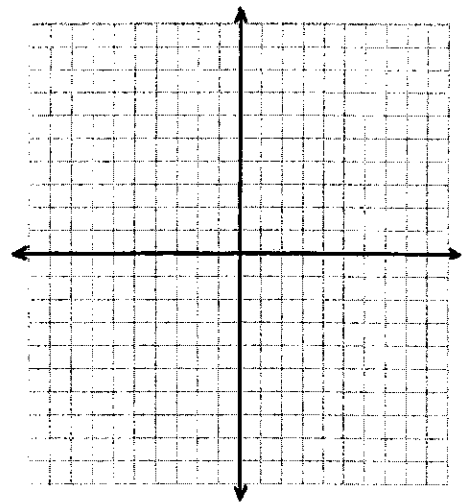
$y =$ (varies)



Parametric Equations

Graph
 $x(t) =$ (varies)

$y(t) =$



Polar Equations

Standard Formulas

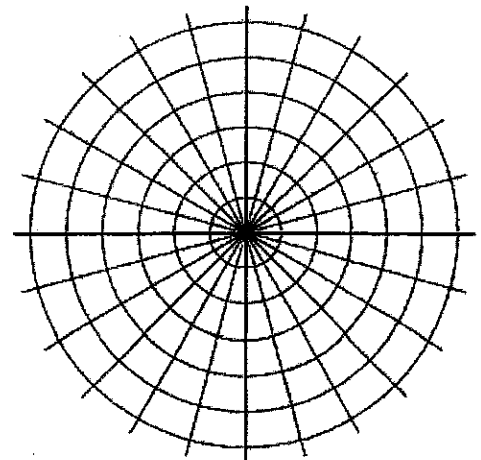
$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$\tan \theta = \frac{y}{x}$$

$$x^2 + y^2 = r^2$$

Graph
 $r =$ (varies)



Name:

Date:

Number:

Stuff You Must Know Cold – Pre-Cal

Trig Identities

Double Angle

$$\sin(2x) = 2 \sin x \cos x$$

$$\cos(2x) = \cos^2 x - \sin^2 x$$

$$= 2 \cos^2 x - 1$$

$$= 1 - 2 \sin^2 x$$

Power Reduction

$$\sin^2 x = \frac{1 - \cos 2\theta}{2}$$

$$\cos^2 x = \frac{1 + \cos 2\theta}{2}$$

Pythagorean

$$\sin^2 x + \cos^2 x = 1$$

$$1 + \tan^2 x = \sec^2 x$$

$$\cot^2 x + 1 = \csc^2 x$$

Reciprocal

$$\sec x = \frac{1}{\cos x}$$

$$\cos x \sec x = 1$$

$$\csc x = \frac{1}{\sin x}$$

$$\sin x \csc x = 1$$

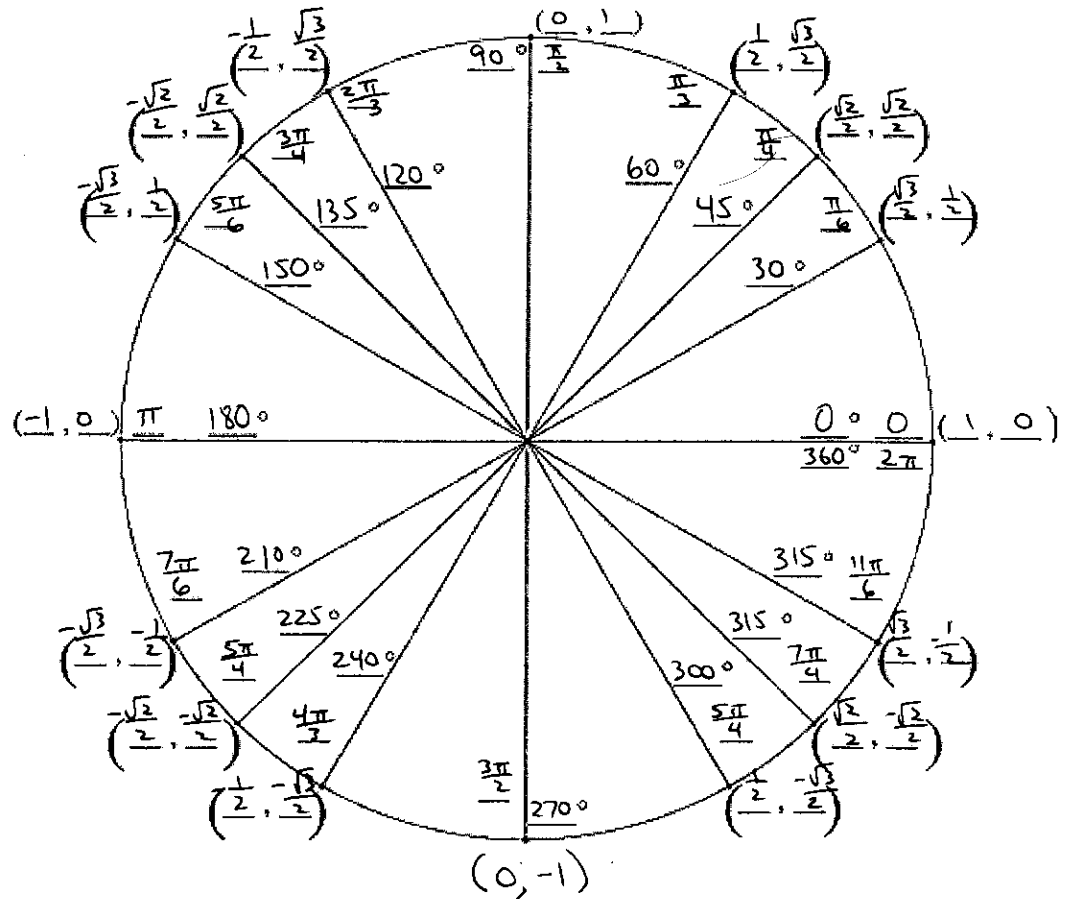
Even/Odd

$$\sin(-x) = -\sin x$$

$$\cos(-x) = \cos x$$

$$\tan(-x) = -\tan x$$

Trig Unit Circle



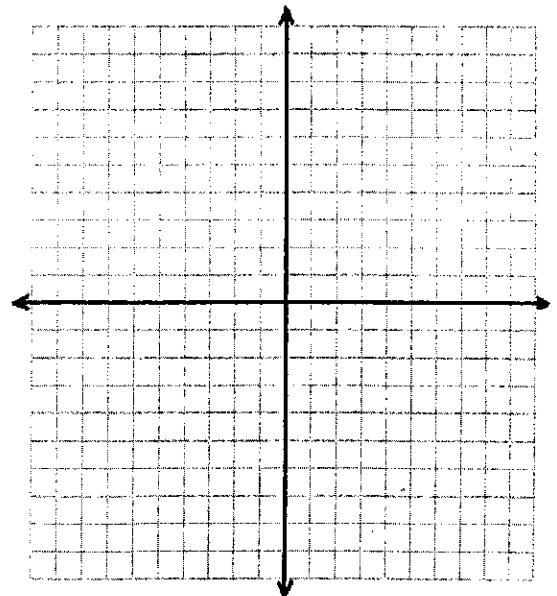
Vectors

(varies)

$$\vec{u} = \langle \quad , \quad \rangle$$

$$\|\vec{u}\| =$$

Graph \vec{u}



Name:

Date:

Number:

Stuff You Must Know Cold - Cal AB/BC

Limits

Notation for:

Limit from the left of $f(x)$ as $x \rightarrow a$

$$\lim_{x \rightarrow a^-} f(x)$$

Limit from the right of $f(x)$ as

$$\lim_{x \rightarrow a^+} f(x)$$

Theorems:

$$\lim_{x \rightarrow a} f(x) = F \text{ and } \lim_{x \rightarrow a} g(x) = G$$

$$\lim_{x \rightarrow a} (f(x) + g(x)) = F + G$$

$$= \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} (f(x) - g(x)) = F - G$$

$$= \lim_{x \rightarrow a} f(x) - \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} (f(x) \cdot g(x)) = F \cdot G$$

$$= \left[\lim_{x \rightarrow a} f(x) \right] \cdot \left[\lim_{x \rightarrow a} g(x) \right]$$

$$\lim_{x \rightarrow a} (f(x))^n = F^n$$

$$= \left[\lim_{x \rightarrow a} f(x) \right]^n$$

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \frac{F}{G}$$

$$= \left[\lim_{x \rightarrow a} f(x) \right] \div \left[\lim_{x \rightarrow a} g(x) \right]$$

$$\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$$

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$

Definition of Continuity:

A function is continuous at the point $x=a$ if and only if:

- $f(a)$ is defined
- $\lim_{x \rightarrow a^-} f(x) = \lim_{x \rightarrow a^+} f(x)$
- $f(a) = \lim_{x \rightarrow a} f(x)$

Extreme Value Theorem

continuous on $[a, b]$
 $a < c < b, a < d < b$

$$f(d) \leq f(x) \leq f(c)$$

Curve Sketching and Analysis

Critical Points: $f'(x) = 0$ or $\frac{\#}{0}$
 look at endpoints

Global Min: check critical points
 $f''(x) > 0$

Global Max: check critical points
 $f''(x) < 0$

Point of Inflection: check $f''(x) = 0$ or $\frac{\#}{0}$
 concavity changes

Derivatives

Definition of Derivative

$$\frac{d}{dx}(f(x)) = \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x}$$

Alternate Form of Def. of Derivative

$$\frac{d}{dx}(f(x)) \text{ at } x=a = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

Chain Rule

$$\frac{d}{dx}[f(u)] = f'(u) \cdot u'$$

Product Rule

$$\frac{d}{dx}(uv) = uv' + vu'$$

Quotient Rule

$$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{vu' - uv'}{v^2}$$

Where u and v are functions of x

More Derivatives

Where u is a function of x and a is a constant

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(\sin u) = \cos u (u')$$

$$\frac{d}{dx}(\cos u) = -\sin u (u')$$

$$\frac{d}{dx}(\tan u) = \sec^2 u (u')$$

$$\frac{d}{dx}(\cot u) = -\csc^2 u (u')$$

$$\frac{d}{dx}(\sec u) = (\sec u)(\tan u)u'$$

$$\frac{d}{dx}(\csc u) = -(\csc u)(\cot u)u'$$

$$\frac{d}{dx}(\ln u) = \frac{u'}{u}$$

$$\frac{d}{dx}(e^u) = e^u \cdot u'$$

$$\frac{d}{dx}(\sin^{-1} u) = \frac{u'}{\sqrt{1-u^2}}$$

$$\frac{d}{dx}(\cos^{-1} u) = \frac{-u'}{\sqrt{1-u^2}}$$

$$\frac{d}{dx}(\tan^{-1} u) = \frac{u'}{1+u^2}$$

$$\frac{d}{dx}(\cot^{-1} u) = \frac{-u'}{1+u^2}$$

$$\frac{d}{dx}(a^u) = a^u \cdot \ln a \cdot u'$$

$$\frac{d}{dx}(\log_a u) = \frac{d}{dx}\left(\frac{\ln u}{\ln a}\right) = \frac{1}{\ln a} \cdot \frac{u'}{u}$$

Intermediate Value Theorem

continuous $[a, b]$
 there is at least one number $x=c$ in the open interval (a, b) such that

$$f(c) = y$$

Name:

Date:

Number:

Stuff You Must Know Cold - Cal AB/BC

The Mean Value Theorem(derivatives) continuous $[a, b]$

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

Rolle's Theorem continuous $[a, b]$

if $f(a) = f(b)$, then there is at least one number $x = c$ in (a, b) such that $f'(c) = 0$

The Fundamental Theorem of Calculus

$$\int_a^b f(x) dx = F(b) - F(a)$$

where $F'(x) = f(x)$ **Corollary to FTC**

$$\frac{d}{dx} \int_a^{g(x)} f(t) dt =$$

$$f(g(x)) \cdot g'(x)$$

Trapezoidal Rule

add up the trapezoidal area in each subinterval

Mean Value Theorem for Integrals(Average Value) continuous $[a, b]$ $x = c$ on (a, b)

$$f(c) = \frac{\int_a^b f(x) dx}{b - a}$$

Solids of Revolution and Friends

Disk Method

$$V = \pi \int_a^b [R(x)]^2 dx$$

Washer Method

$$V = \pi \int_a^b ([R(x)]^2 - [r(x)]^2) dx$$

General volume equation

$$V = \int_a^b \text{Area}(x) dx$$

Arc Length (rectangular)

$$L = \int_a^b \sqrt{1 + [f'(x)]^2} dx$$

Distance, Velocity, and Acceleration

$s(t)$ is the position function,
 $\langle x(t), y(t) \rangle$ is the position in parametric

$$\text{velocity} = s'(t)$$

$$\text{acceleration} = v'(t) = s''(t)$$

$$\text{velocity vector} = \langle x'(t), y'(t) \rangle$$

$$\text{acceleration vector} = \langle x''(t), y''(t) \rangle$$

speed (rectangular and parametric) =

$$|v| = \sqrt{(x'(t))^2 + (y'(t))^2}$$

$$\text{displacement} = \int_a^b v dt$$

distance (rectangular and parametric) =

$$\int_a^b |v| dt$$

$$\int_a^b \sqrt{(x')^2 + (y')^2} dt$$

average velocity =

$$\frac{\Delta s}{\Delta t}$$

L'Hôpital's Rule (Bernoulli's Rule)

$$\text{If } \frac{f(a)}{g(a)} = \frac{0}{0} \text{ or } \frac{\infty}{\infty}$$

$$\text{then } \lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

Euler's Method

$$x_{\text{new}} = x_{\text{old}} + \Delta x$$

$$y_{\text{new}} = y_{\text{old}} + \frac{dy}{dx} \Big|_{(x_{\text{old}}, y_{\text{old}})} \cdot \Delta x$$

Integration by Parts

$$\int u dv = uv - \int v du$$

Logistics

$$\frac{dP}{dt} = kP(c - P)$$

Parametric Equations

$$\frac{dy}{dx} = \frac{\frac{dy}{dt}}{\frac{dx}{dt}}$$

$$\frac{d^2y}{dx^2} = \frac{\frac{d}{dt} \left(\frac{dy}{dx} \right)}{\frac{dx}{dt}}$$

Polar Curves

$$\text{Area} = \int_a^b \frac{1}{2} r^2 d\theta$$

$$\text{Slope} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}}$$

Taylor Series centered at $x = a$

$$f(x) \approx f(a) + f'(a)(x-a) + \frac{f''(a)}{2!}(x-a)^2 + \dots + \frac{f^{(n)}(a)}{n!}(x-a)^n$$

Maclaurin Seriesabout $x = 0$

$$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$$

$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$$

$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$$

$$\frac{1}{1-x} = 1 + x + x^2 + x^3 + \dots$$

$$\ln(x+1) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$$

Series Tests/Error Bound

(varies)