

PROBLEM: Show that the only integer values in the set

$$\left\{ \frac{a^2 + b^2}{ab + 1} \mid a, b \in \mathbb{Z}, a, b \geq 0 \right\}$$

are the perfect squares.